

Type Ia Supernovae:

Three Not So Easy Pieces

Ignition

Propagation

Light Curve

Progenitor

Hoyle and Fowler (1960)

Arnett (1968, 1969)

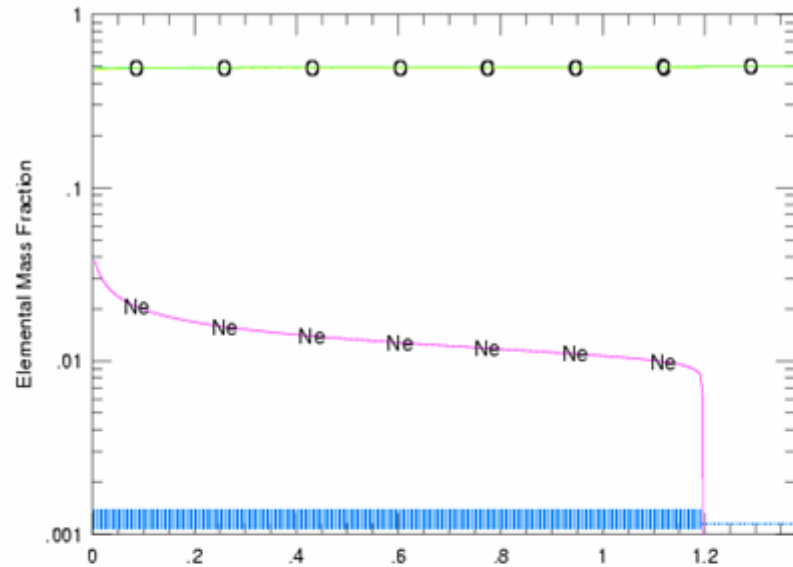
Nomoto, Sugimoto, & Neo (1976)

Ignition occurs as the *highly screened* carbon fusion reaction begins to generate energy faster than neutrino losses can carry it away.

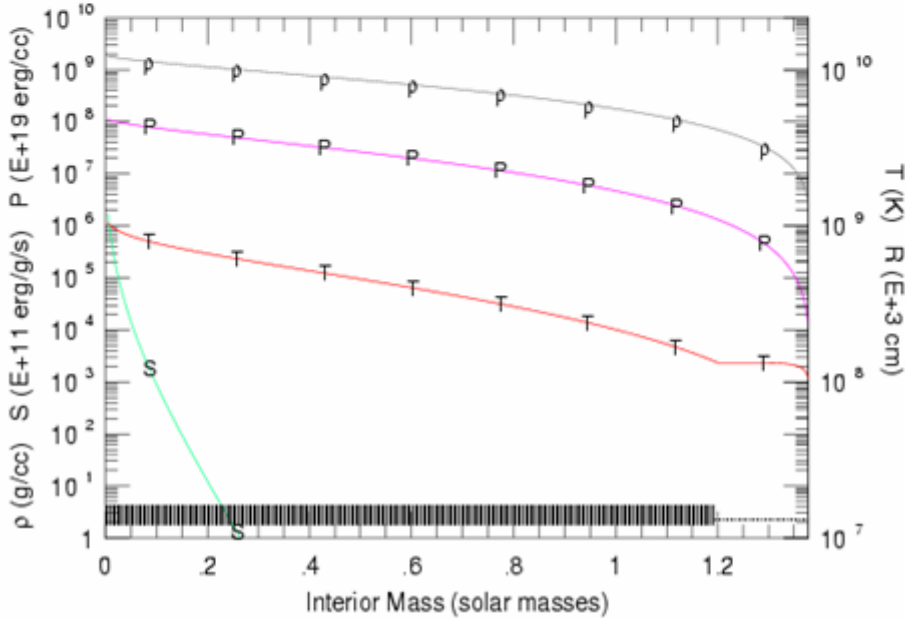
At a given temperature, the plasma neutrino losses first rise with density and then decline when $\hbar\omega_p > kT$.

$$\text{As } \rho \rightarrow 3 \times 10^9 \text{ gm cm}^{-3}; \quad T \approx 3 \times 10^8 \text{ K}$$

$$S_{\text{nuc}} (^{12}\text{C} + ^{12}\text{C}) \geq S_{\nu}(\text{plasma}); \quad M \approx 1.38 M_{\text{sun}}$$

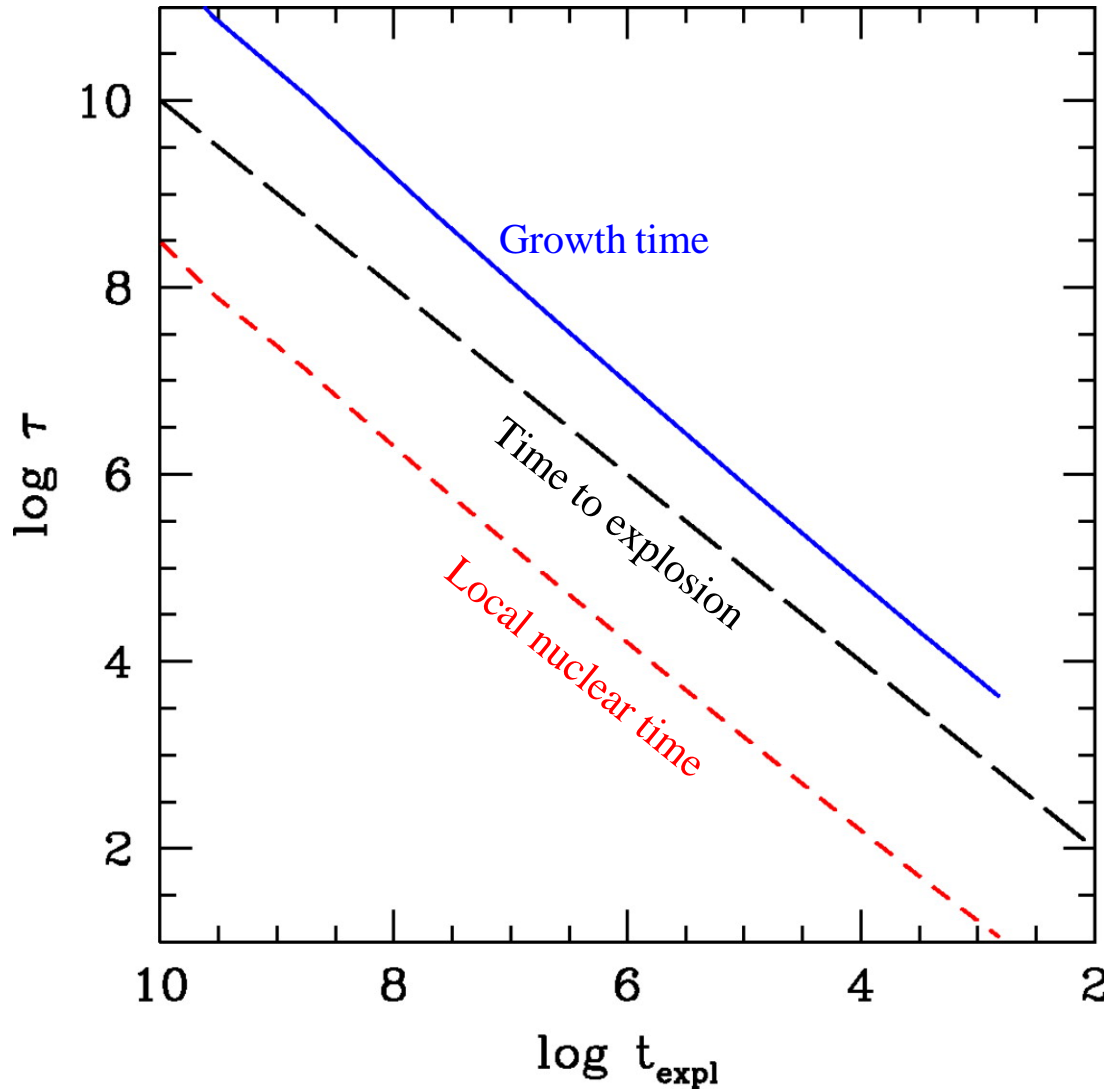


Conditions in a Chandrasekhar Mass white dwarf as its center runs away – following about a century of convection.



Vertical bars denote convective regions

Pulsational Stability



- White dwarf is pulsationally unstable throughout carbon burning (500 years)
- Pulsational period 2 s
- $\Gamma = 4/3$, $\epsilon_{\text{nuc}} = CT^{23}$
- Most of energy goes into heating the white dwarf
- ***Growth time of the pulsations never catches up with the runaway time***
- Would have interesting consequences if it did.

Ignition Conditions

Last "good convective model" is when the central temperature has risen to $7 - 8 \times 10^8 \text{ K}$

Pressure scale height: 400 km Convective speed: 50 km s^{-1}

Nuclear time scale: $\sim 10^2 \text{ s}$ Binding energy: $4 \times 10^{50} \text{ erg}$

Convective time scale: $\sim 10^2 \text{ s}$ Density: $2.5 \times 10^9 \text{ g cm}^{-3}$

In 1D

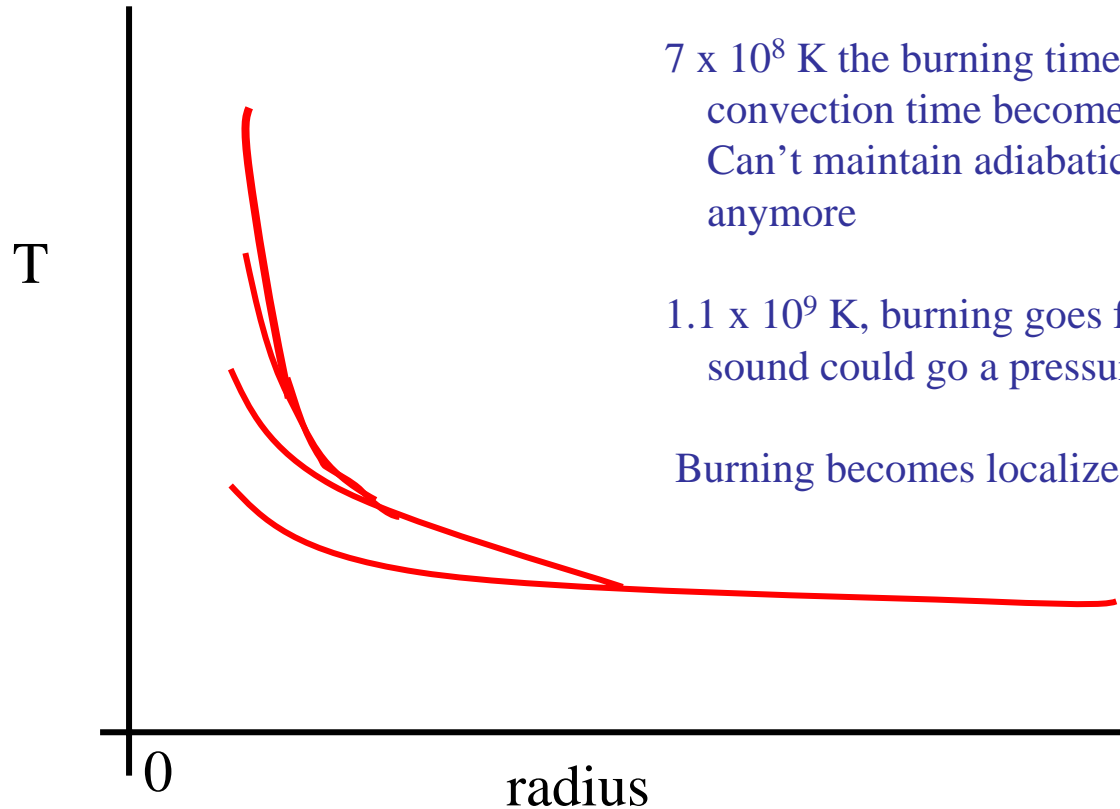
Convection for 100 years, then formation of a thin flame sheet.

Note that at:

7×10^8 K the burning time and
convection time become equal.
Can't maintain adiabatic gradient
anymore

1.1×10^9 K, burning goes faster than
sound could go a pressure scale height

Burning becomes localized



$$S_{nuc} \propto T^{23}$$

Ignition

The crucial unsolved problem in modeling Type Ia supernovae.

- One point or many (how many?)
- One side or isotropic?
- One time or continuous for 1 second?

Key physics:

- The probability density function for the temperature fluctuations and the spatial and temporal correlation functions
- The symmetry of convection with a point energy source
- How things scale as the Rayleigh number approaches infinity
- The role of rotation

Energy Generation Rate

$$S_{nuc} \approx 2.8 \times 10^{13} \left(\frac{T_8}{7} \right)^{23} \left(\frac{\rho_9}{2} \right)^{3.3} \text{ erg g}^{-1} \text{ s}^{-1}$$

Heat Capacity

$$C_p = 9.1 \times 10^{14} + \frac{8.6 \times 10^{13} T_8}{\rho_9^{1/3}} + \frac{3.0 \times 10^9 T_8^3}{\rho_9} \text{ erg g}^{-1} (10^8 \text{ K})^{-1}$$

ionselectronsradiation

Adiabatic Temperature Gradient

$$T(r) \approx T_o \left(1 - 0.0185 \left(\frac{\rho_{o,9}}{2} \right)^{2/3} r_7^2 \right)$$

Luminosity

$$L \approx 5.0 \times 10^{44} \text{ erg s}^{-1} \left(\frac{\rho_{o,9}}{2} \right)^{4.3} \left(\frac{T_{o,8}}{7} \right)^{23}$$

mostly goes into heating the star, the rest into expansion

Dimensionless expansion coefficient

$$\delta_P = - \left(\frac{\partial \ln \rho}{\partial \ln T} \right)_P \approx 0.019 \frac{T}{\rho} \approx 0.007$$

gas must get very hot to expand just a little

From Mixing Length Theory

$$v_{ML} \approx \left(\frac{2g \Delta\rho}{\rho} \right)^{1/2} \approx \left(\frac{4G\delta_P L}{3C_P T} \right) \approx 40 \text{ km s}^{-1} \left(\frac{T_{o,8}}{7} \right)^7 \left(\frac{\rho_9}{2} \right)^{1.4}$$

Temperature fluctuations to carry L

$$\left(\frac{\Delta T}{T}\right) \approx \frac{v_{ML}^2}{2gl\delta_P} \approx 0.005 \left(\frac{\rho_9}{2}\right)^{2.1} \left(\frac{T_{o,8}}{7}\right)^{14} \quad \frac{\Delta\rho}{\rho} \approx 4 \times 10^{-5}$$

Dimensionless Measures

$$Ra = \frac{gl^3 C_P \delta_P \Delta T}{T\eta\sigma} \approx 10^{25}$$

Dimensionless temperature gradient

$$Pr = \frac{C_P \eta}{\sigma} \approx 4 \times 10^{-3}$$

momentum transport/heat conduction

$$Re = \frac{\rho v_{ML} l}{\eta} \approx 10^{14}$$

inertial forces/viscous forces

$$Nu = \frac{\phi l}{\sigma \Delta T} \approx 3 \times 10^{11}$$

total heat transport/conduction

$$L_{Kol} = l Re^{-3/4} \approx 3 \times 10^{-4} \text{ cm}$$

$\eta = \text{viscosity}$

$\sigma = \text{conductivity}$

If ignition occurs for matter flowing through the stellar center with speed v ignition will occur when the integral

$$\int \left[\left(\frac{dT}{dr} \right)_{\text{exp}} + \frac{S_{\text{nuc}}}{C_P v} \right] dr$$

nb. diverges at $r = 0$ if $v(0) = 0$. i.e., it ignites in the center.

diverges. Here, from the adiabatic approximation for the temperature gradient

$$\left(\frac{dT}{dr} \right)_{\text{exp}} \approx -0.037 T_c \left(\frac{\rho_9}{2} \right)^{2/3} r_7$$

The solution depends on the assumed velocity structure in the core but for v between 50 and 100 km s⁻¹, ignition will occur when the average central temperature is in the range

$$T_{\text{ign}} = 7.7 - 7.9 \times 10^8 \text{ K.}$$

at $r \sim 100 \text{ km}$

*Woosley, Wunsch, and Kuhlen (2003)
Wunsch and Woosley (2004)*

Three-Dimensional Models of Ignition

Kuhlen, Woosley, and Glatzmaier (2003)

Use Kepler 1D model as a first approximation to the background state. Follow perturbations using anelastic hydrodynamics in 3D

(Glatzmaier, 1984, J. Comp. Phys).

238 Chebyshev polynomials in r direction

85 spherical harmonics in θ

42 spherical harmonics in ϕ

inner boundry at 55 km, about 0.001 solar masses

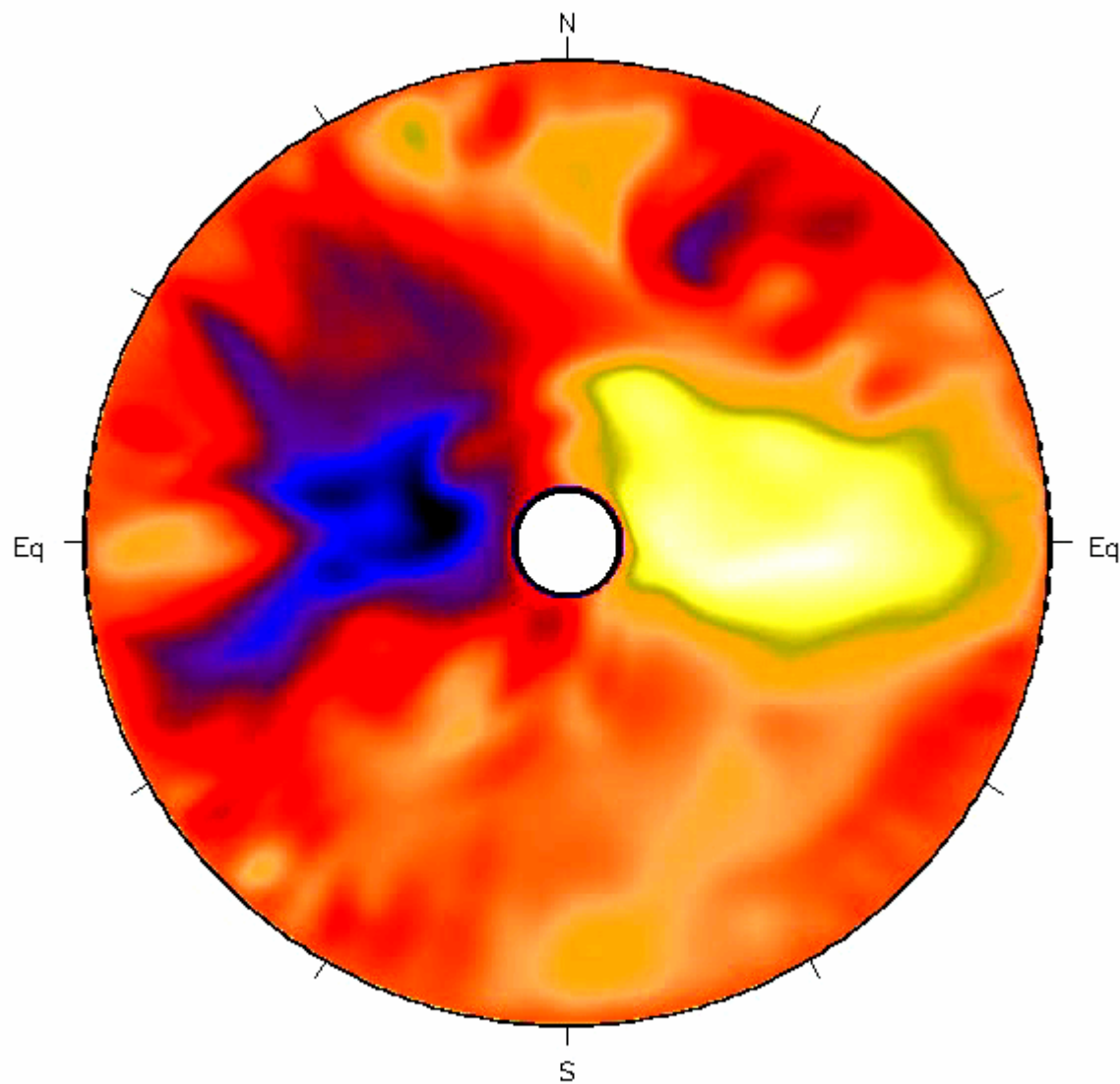
outer boundry at 500 km, approximate extent of convection

central density $2.5 \times 10^9 \text{ g cm}^{-3}$

central temperature $7.0 \times 10^8 \text{ K}$

highest velocity on grid 180 km s^{-1}

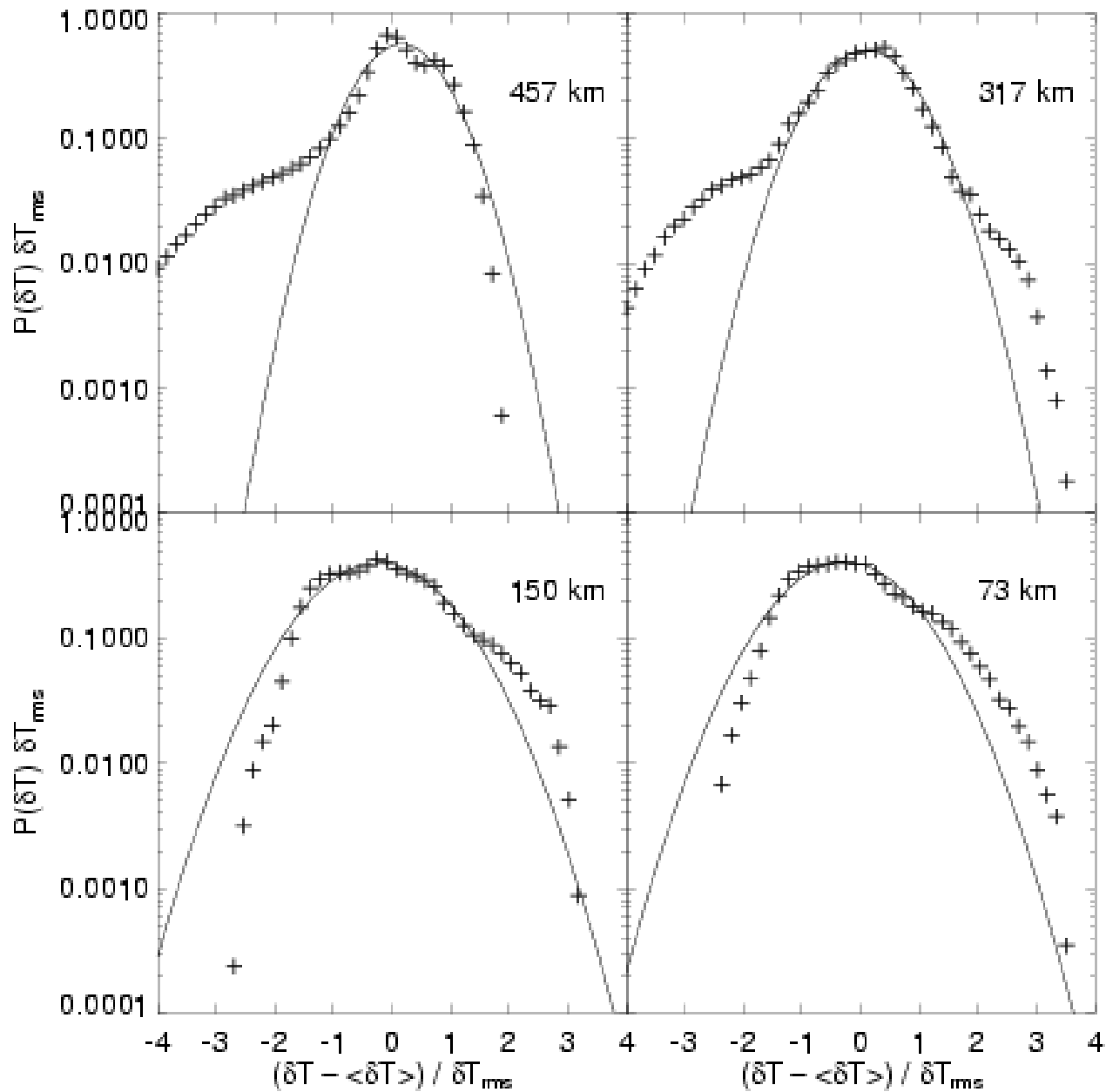
radial velocity



meridional slice

[km/s]

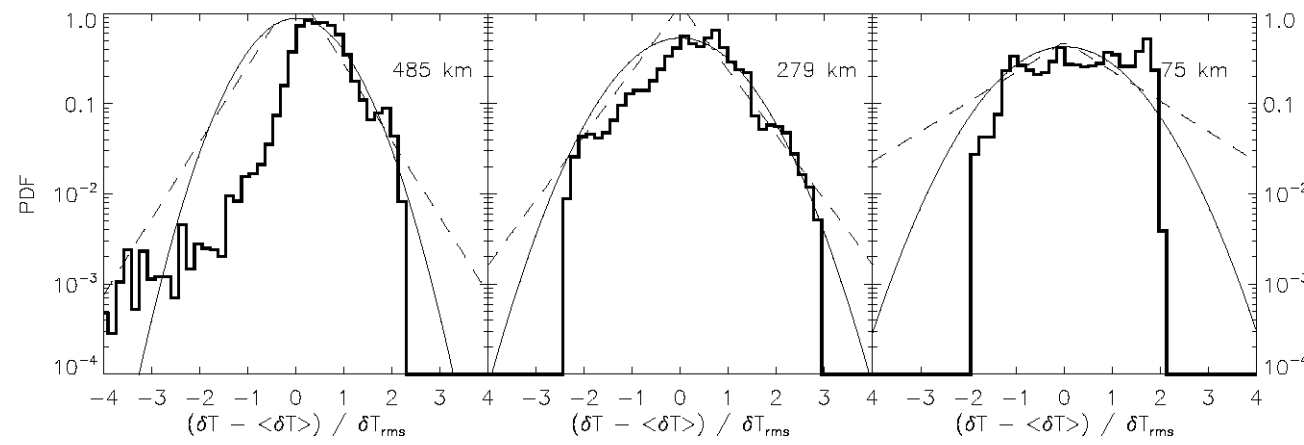




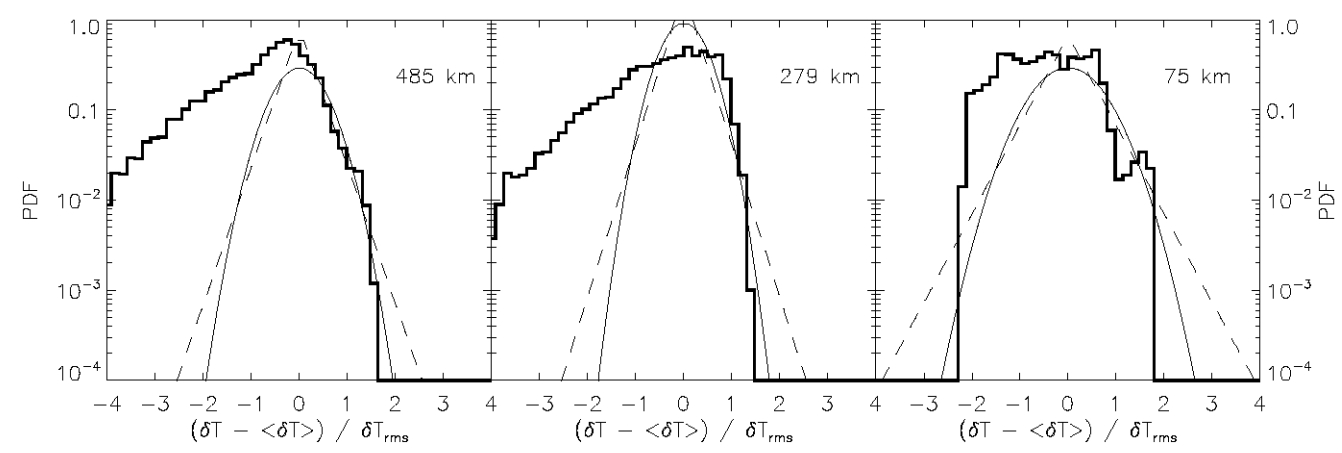
Kuhlen, Woosley,
and Glatzmaier
(in prep)

See also
Wunsch and
Woosley (2004)

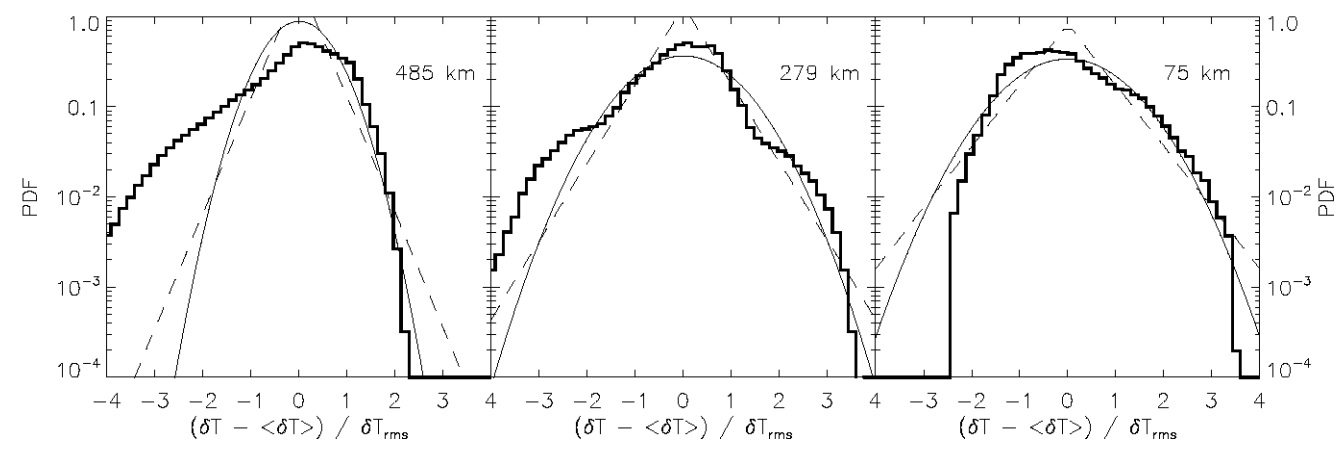
7 seconds of data



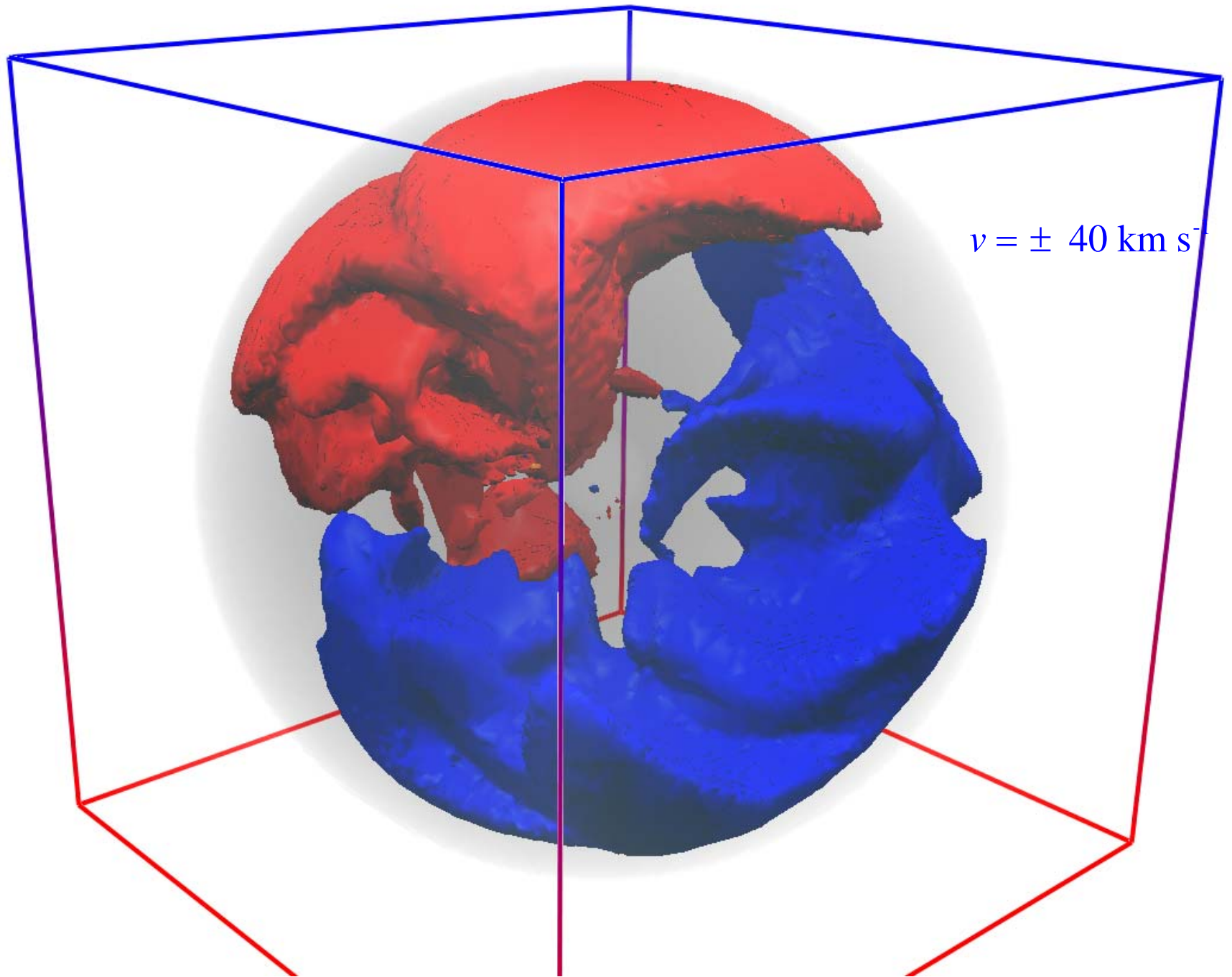
up



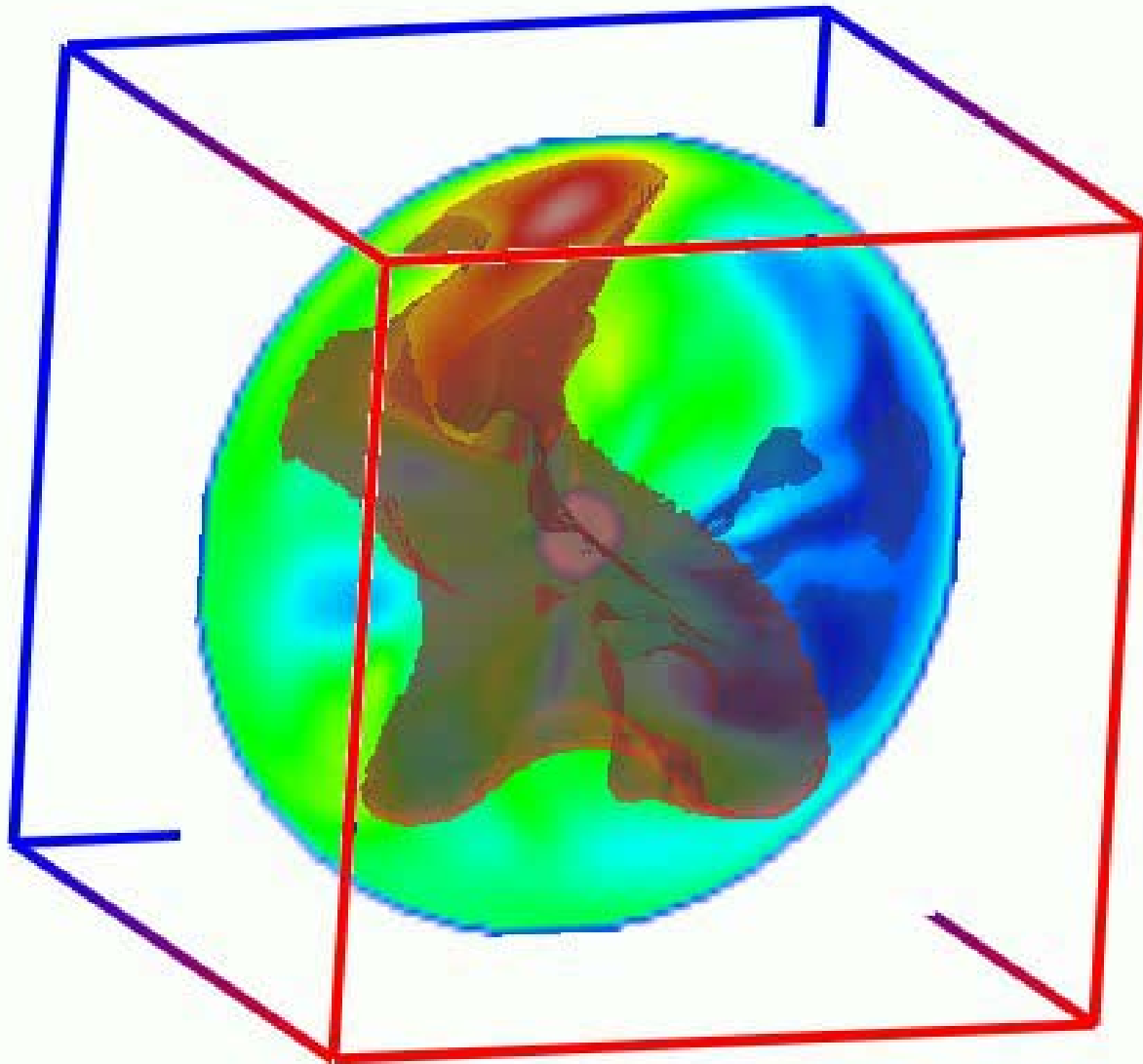
down



total



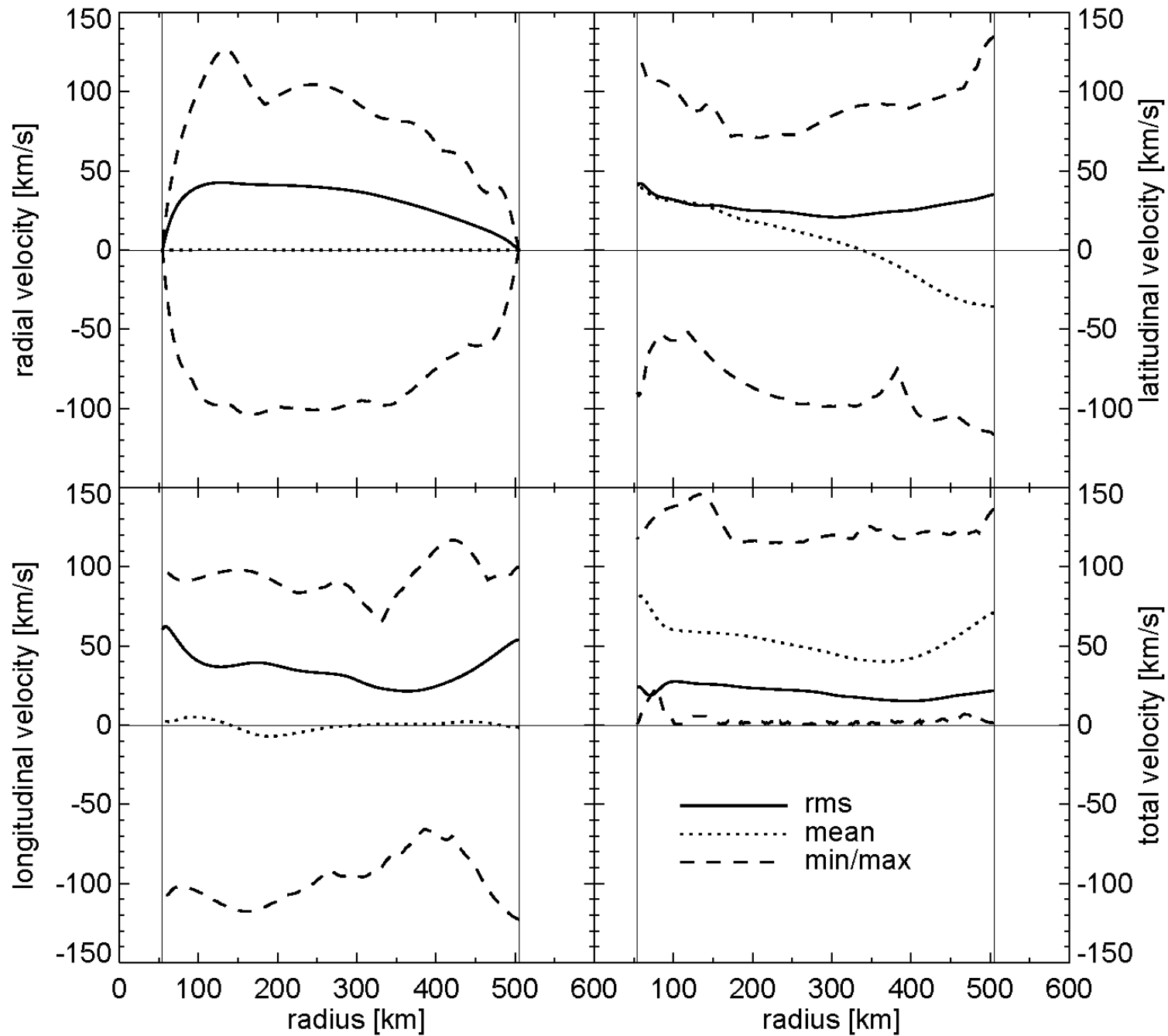
$n = 238$
42 orders in θ
38 orders in φ
70 s of star time



$$T_{9c} = 7.0$$

$$Ra \sim 10^7$$

Kuhlen, Woosley, and Glatzmaier (2005)

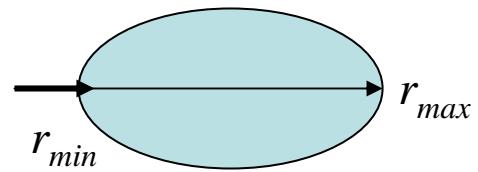


A possible implication is that the supernova ignites preferentially on one side at one or more points. But what is the spatial and temporal distribution of these points?

nb. they do not all ignite at once!

not to scale

r_{min} *determines if can ignite
on other side*



r_{max} *affects energetics*

r_{min} determines whether ignition propagates to other side

$$\frac{r_{crit}}{v_{eff}} = \sqrt{\frac{2 r_{crit}}{g_{eff} \alpha}} \approx \sqrt{\frac{1}{50 \alpha}} \Rightarrow r_{crit} \approx 20 - 40 \text{ km}$$

$$\alpha = 0.1 - 0.7 \quad v_{eff} = \text{Max}\{v_{cond}, v_{turb}\} \sim 100 \text{ km s}^{-1}$$

$$g_{eff} \approx 10^9 \left(\frac{r}{10^7 \text{ cm}} \right) = 100 r$$

Are all ignition points advected out of the core by the fluid flow or do some stay behind to seed burning on the other side?

Conclusions

(Kuhlen, Woosley, and Glatzmaier, 2003)

- *Ignition physics is central to understanding how SN Ia explode and is probably the cause of some unpredictable diversity in SN Ia properties.*
- Most of the white dwarf will have a turbulent kinetic energy of order 10^{14} erg g^{-1} *before* the explosion. This sets a lower bound on the flame propagation speed.
- Ignition probably occurs off-center and at multiple points and times, and it may also be grossly asymmetric.
- There may be ways out of this

Kraichnan (1962) regime at high Rayleigh number

Rotation

Surface detonation?

Flame Propagation

- The flame is born a deflagration at $\rho_c = 2.5 \times 10^9 \text{ gm cm}^{-3}$. Does a transition to detonation occur at $\rho \sim 10^7 \text{ gm cm}^{-3}$?

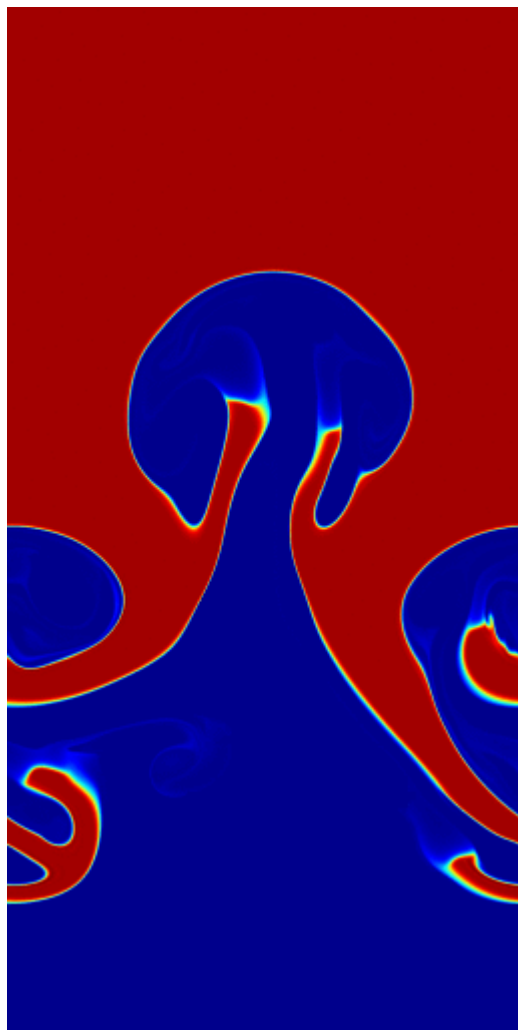
Probably not if the only physics included is the RT instability on the grid. It still might be possible for sufficiently energetic turbulence to provoke a transition on small scales. (Zingale et al. 2004, 2005)

Effects of off center ignition and break out still being explored (Plewa et al 2004)

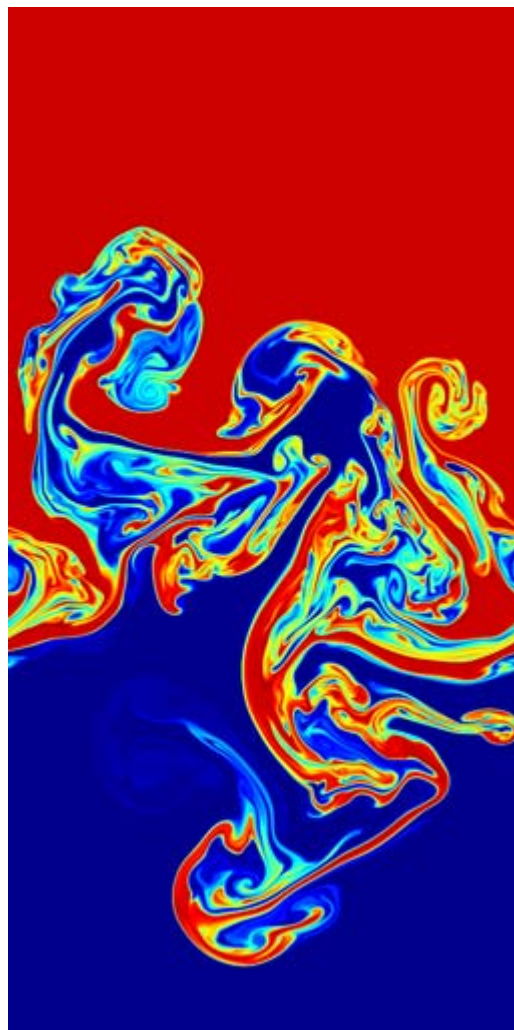
- How to correctly represent the effects of turbulence generated by the RT instability on large scales on the subgrid flame propagation?

A purely local RT model is inadequate. Must include turbulent cascade from above (Niemeyer, Hillebrandt et al).

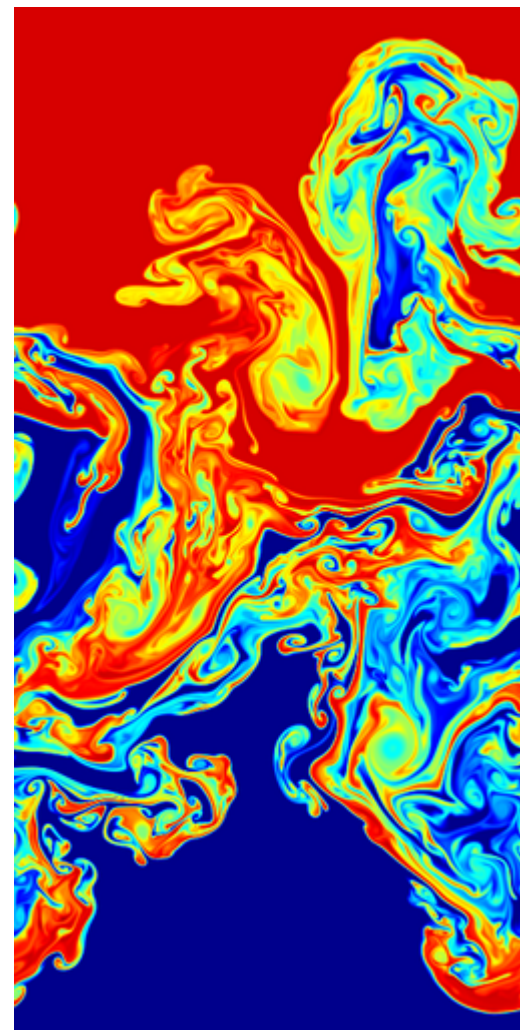
- Issues of resolution and “back propagation”.



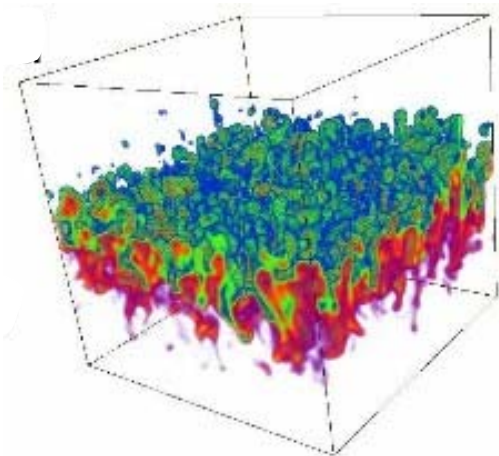
1.5×10^7



1.0×10^7

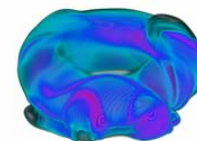
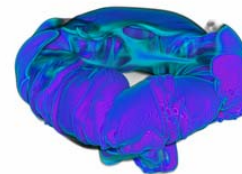
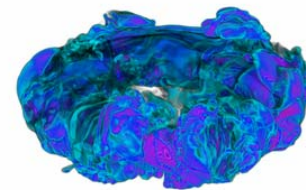


0.667×10^7

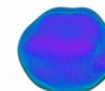
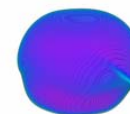
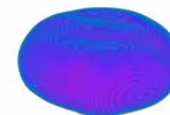


Calder et al. (2002)

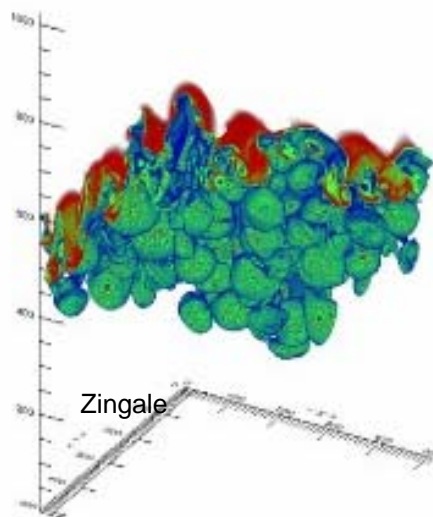
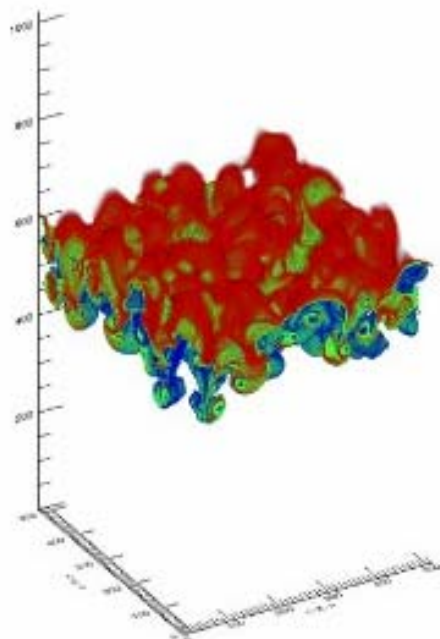
or



?



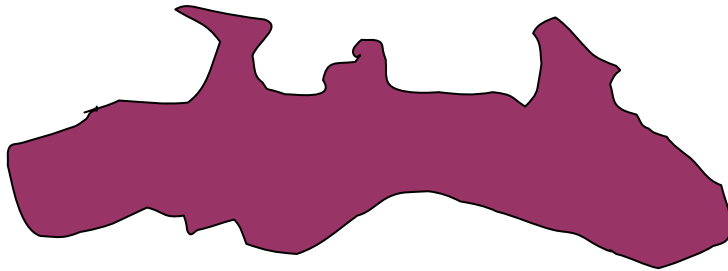
Zingale



Bubbles and planes


*How many bubbles
and how do they spread?*

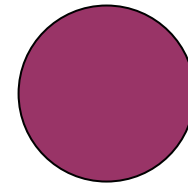
$$v \approx 0.1 g_{\text{eff}} t$$

Sharp-Wheeler

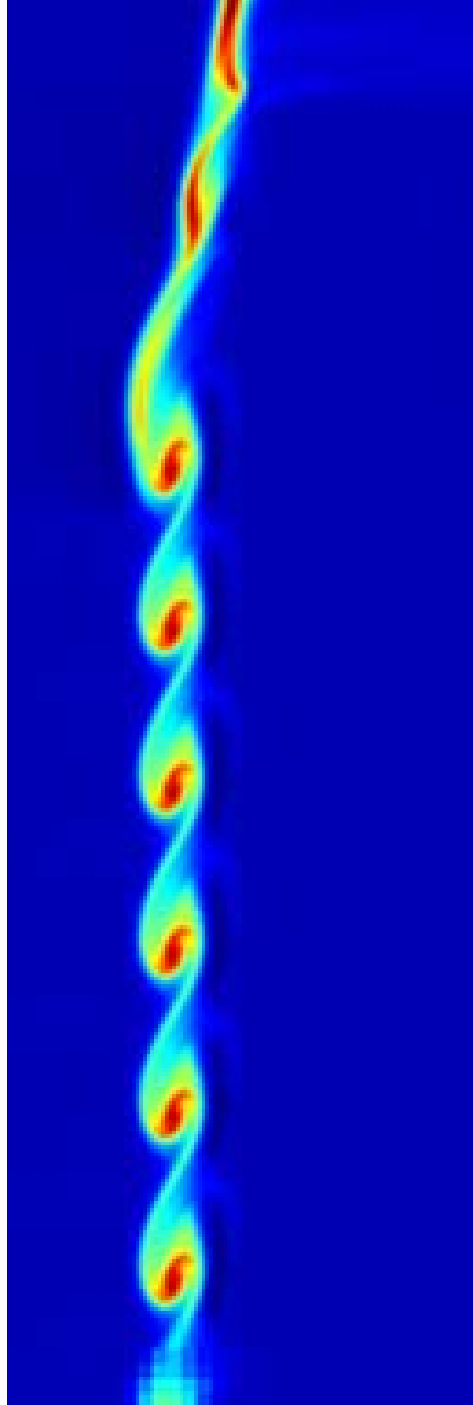
*This probably won't make it
to the surface*

$$v \approx 0.7 g_{\text{eff}} t$$




sphere

This probably will



Are lateral spreading and backwards propagation correctly included?

Zingale (2005)

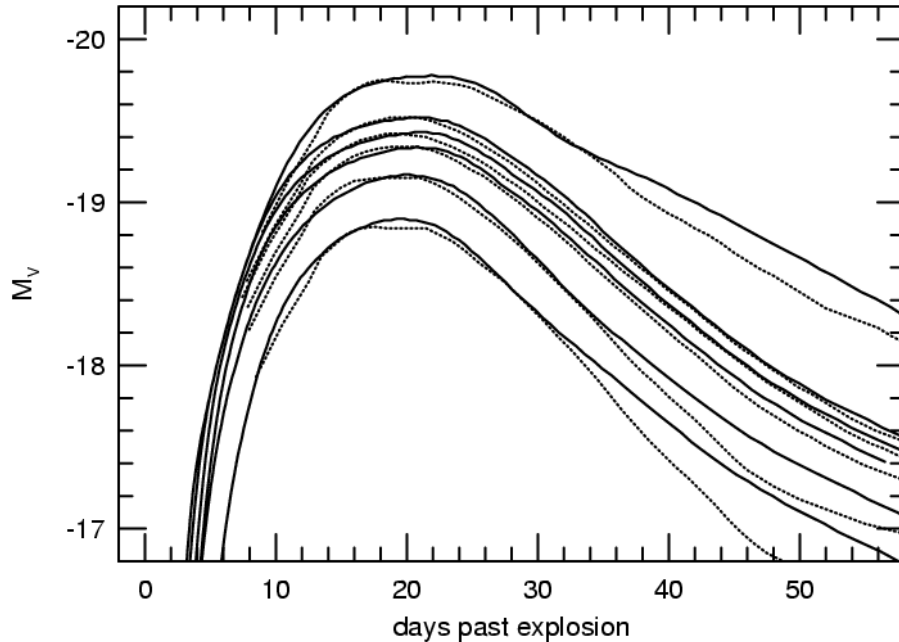
Shear velocity = 10 x laminar speed
small shear width

The Guinness Effect



*Big bubbles move up;
little bubbles move down.*

The Phillips Effect



Left – a single supernova model (energy, density structure, etc) in which only the mass of ^{56}Ni has been varied. Also shown are the standard template of light curves displaying the width-luminosity relation.

Pinto & Eastman, (2001), *New Astron*,

Light Curves

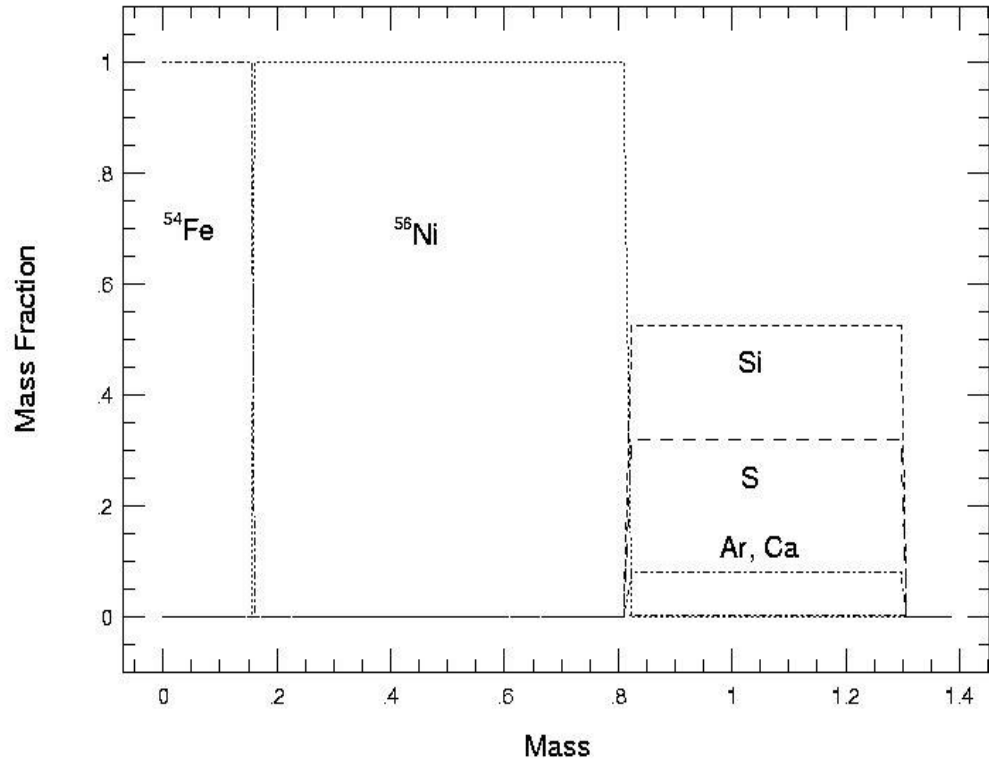
What matters?

- The mass of ^{56}Ni -- contributes explosion energy, radioactive energy, and opacity.
- The mass of ^{54}Fe , ^{58}Ni , and other stable members of the iron group -- contribute opacity and explosion energy, but no radioactive energy.
- The mass of SiSArCa -- contribute to the explosion energy, but not the opacity or radioactive energy.
- The explosion energy -- depends on the ignition density (hence accretion rate) and C/O ratio as well as all the above masses.
- **Mixing**

An idealized model

Assume a starting mass of 1.38 solar masses, a central density of $2 \times 10^9 \text{ g cm}^{-3}$ and a C/O ratio of 1::2

For a given starting density, the final composition (three variables, plus mixing) then defines the model.



The final velocity distribution is not very sensitive to how the energy is deposited (especially for the iron containing region).

