



... for a brighter future

Mass measurements: Experiment (1)

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of Energy

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Outline

- Definitions and scale
- Required accuracy
- Deflection type spectrometers
- Time-of-flight spectrometers
- Cooling of radioactive ions
- Ion traps spectrometer
- Schottky technique in storage rings
- Q-value measurements by reaction and decay
- Consistency check

Basic considerations

■ Atomic mass unit

- $u = m(^{12}\text{C}) / 12 = 931494.009 \text{ keV}/c^2$

■ Mass of the constituents

- $m_n = 939.565 \text{ MeV}/c^2 = 1.00866491574(56) u$
- $m_p = 938.272 \text{ MeV}/c^2 \Rightarrow m(^1\text{H}) = 1.00782503207(10) u$
- $m_e = 0.51100 \text{ MeV}/c^2$

■ Mass of a nucleus

- mass of constituents plus binding energy (usually negative ... not always)

$$B = \{m(A,Z) - Z (m_p + m_e) - N m_n \} c^2$$

- huge amount of stored energy
- binding energy is about $8 \text{ MeV}/u$, that is $8/938 \sim 0.7\%$ of the total rest mass energy. That is the fraction that can be released by nuclear reactions ... still enough to power the sun and other stars.

$$B(^{12}\text{C})/c^2 \sim 6 \times (1.0087 + 1.0078) - 12 \times 1 \sim 0.099 u \sim 0.8\% \text{ of } m(^{12}\text{C})$$

Binding energy and mass excess

- Binding energy is the energy that is released when a nucleus is assembled from neutrons and protons

$$m(Z, N) = Zm_p + Nm_n - Bc^2$$

- Once B is known, the mass of the nucleus is determined
- B is roughly $\sim A$

- Masses are usually tabulated as atomic masses

$$m = m_{\text{nuc}} + Z m_e - B_e/c^2$$

Nuclear Mass
 $\sim 1 \text{ GeV}/c^2$ per A

Electron Mass
 $511 \text{ keV}/c^2$

Electron Binding Energy
 13.6 eV (H)
to $116 \text{ keV (K-shell U) / Z}$

Most tables give atomic mass excess Δ in MeV: $\Delta(A, Z) = (M(A, Z) - Am_u)c^2$

(with $m_u = M(^{12}\text{C})/12 = 931.478 \text{ MeV}/c^2$ and for ^{12}C : $\Delta=0$)

The Q-value for $A+B \rightarrow C$ can then be expressed as: $Q = \Delta(A) + \Delta(B) - \Delta(C)$

Required accuracy

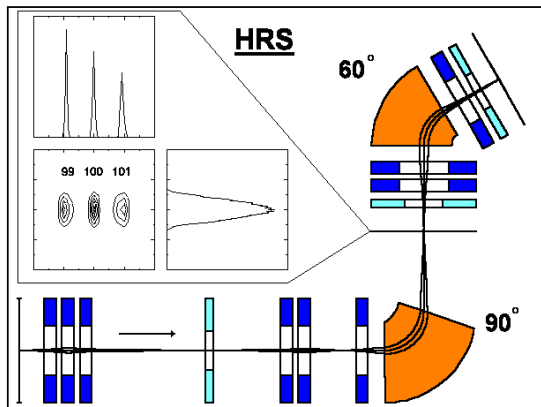
- Mass resolution and accuracy of the measurement determines the physics you are sensitive to ($A \sim 100$)

$\Delta m/m$	Mass accuracy	physics
$\sim 10^{-2}$	$\sim 1 \text{ GeV}/c^2$	number of nucleons
$\sim 10^{-3}$	$\sim 100 \text{ MeV}/c^2$	atom vs molecule
$\sim 10^{-5}$	$\sim 1 \text{ MeV}/c^2$	isobar
$\sim 10^{-6}$	$\sim 100 \text{ keV}/c^2$	nuclear mass calculations
$\sim 10^{-7}$	$\sim 10 \text{ keV}/c^2$	astrophysics, nuclear structure
$\sim 10^{-8}-10^{-9}$	$\sim 0.1-1 \text{ keV}/c^2$	superallowed decay, $\beta\beta$ -decay
$\sim 10^{-10}-10^{-11}$	$\sim 1-10 \text{ eV}/c^2$	electronic binding energy
$\sim 10^{-12}$	$\sim 0.1 \text{ eV}/c^2$	vibrational energy

- For nuclear physics and astrophysics, the requirement is typically 10^{-6} to 10^{-9} accuracy.

Tools of the trade

- Tools of various size, cost and accuracy ... no direct relationship between these quantities



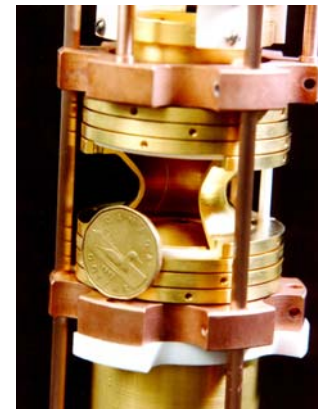
Deflection type separator



TOF spectrometer: SPEG



TOF or Schottky: ESR



Penning trap spectrometer

Accuracy is not the full story

- Specific applications might have other requirements besides accuracy
 - *mass models are not **that** accurate*
 - No mass model has predictive accuracy better than 300 keV/c² ... e.g. comparison to 310 masses measured at the FRS

$$\sigma_{\text{rms}}^2 = \frac{1}{N} \sum_{i=1}^N (m_i^{\text{exp}} - m_i^{\text{theory}})^2 \quad \longrightarrow$$

Mass model	σ_{rms} /keV
FRDM	372
FRLDM	696
Spanier-Johanson	1210
Myers-Swiatecki	395
Duflo-Zucker	668
HF+BCS	960
HFB	650

- to progress, models need anchor points very far from stability ... they need reach, i.e. sensitivity

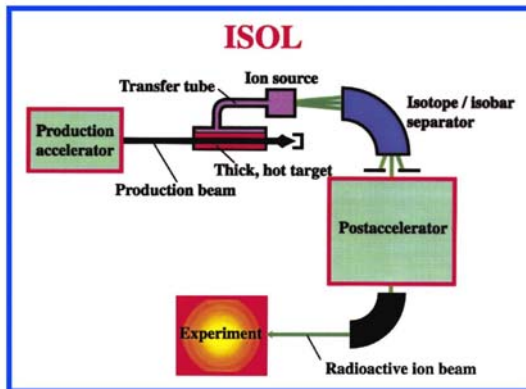
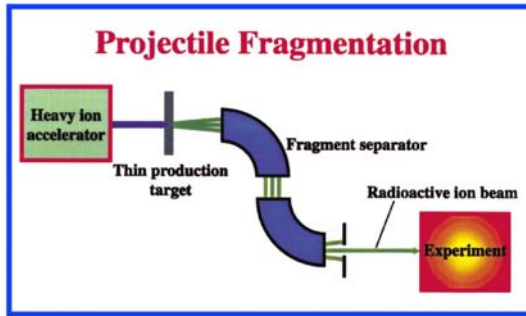
■ Specific nuclei versus representative cases

- in some cases, only that nuclei will do
 - *superallowed emitters, waiting point nuclei, ...*
- need measurement technique matched to the production of that specific nuclei

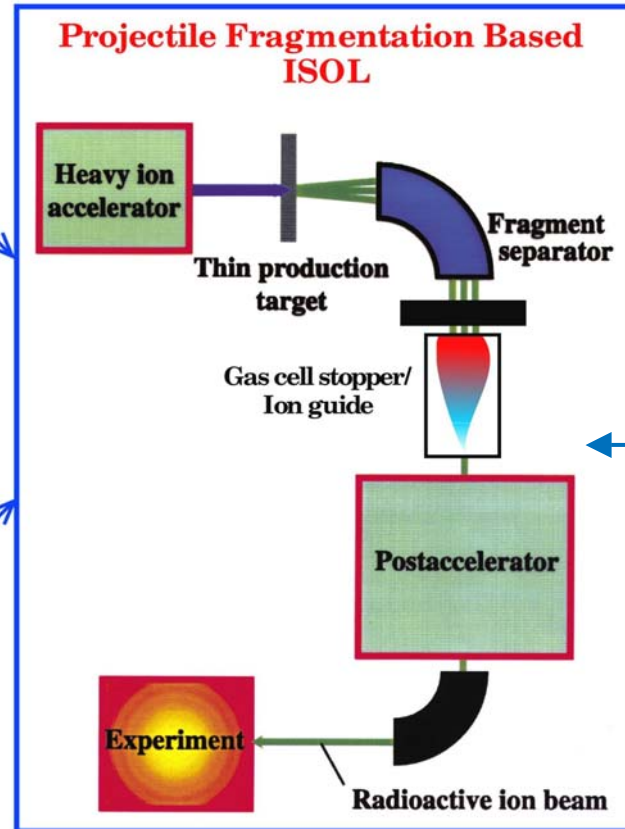
Production methods for beams of short-lived isotopes: beam properties determine the measurement techniques applicable

- Fast Extraction Times (\sim msec)
- Chemical independence
- Isobar separation

GSI,
RIKEN,
MSU,
GANIL



ISAC II,
REX-
ISOLDE,
HRIBF



In-flight
generated beam
stopped and
cooled to ISOL
beam energies
and properties

Fusion-
evaporation:
ANL, GSI

Fragmentation:
GSI, MSU,
RIKEN

Mass measurement approaches

■ Indirect

- Decay (2 or 3 body final state)



$$Q_b = m_A - m_B - m_b$$

- Reaction



$$Q = m_A + m_a - m_B - m_b$$

- Quantum mechanics

$$\nu_e \leftrightarrow \nu_u$$

$$K \leftrightarrow \bar{K}$$

■ Direct (less indirect)

- Deflection spectrometer
- Time-of-flight spectrometer
- Cyclotron frequency measurement

Method of choice depends on production method, yield, lifetime, and accuracy required.

Beginnings of nuclear mass spectrometry

- Pioneering work by J.J. Thomson around the early 1900s using a positive ray parabola apparatus (mass resolution of about 10!)
- Mass spectrometry field really started with A.J. Dempster (1918) and F.W. Ashton (1919)
 - Deflection type mass spectrometer

- Ion source at voltage V

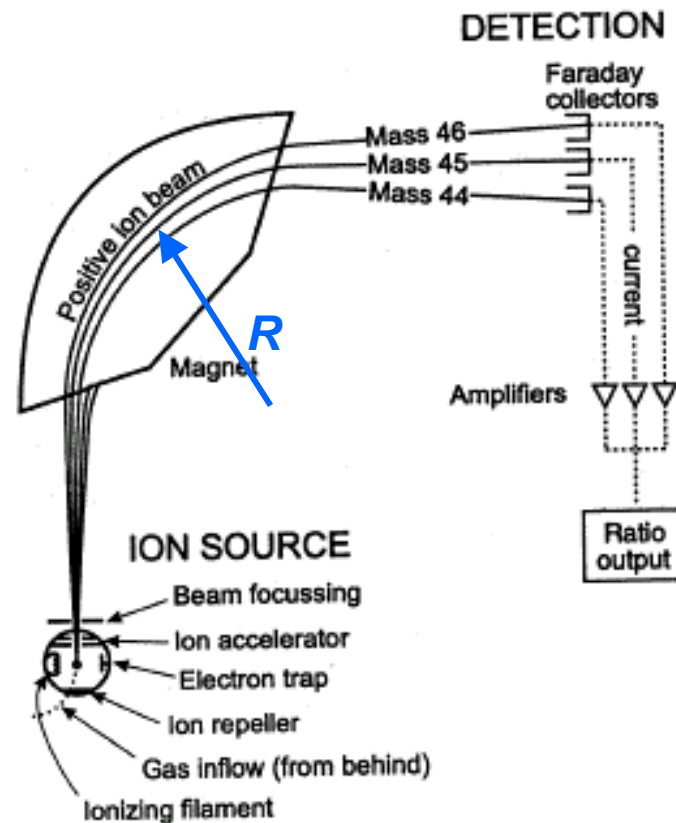
$$E = eV = mv^2/2$$

- Magnetic sector with field B

$$F_c = mv^2/R = q\vec{v} \times \vec{B} = qvB$$

$Brho \rightarrow$

$$BR = \frac{mv}{q} = \frac{p}{q} = \frac{\sqrt{2mE}}{q}$$



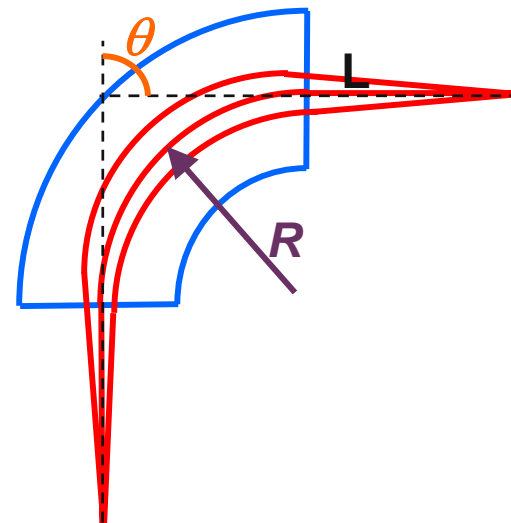
Deflection type spectrometer: dispersion

- Radius of curvature depends on p/q

$$R = \frac{mv}{qB} = \frac{p}{qB} = \frac{\sqrt{2mE}}{qB}$$

- different masses will have different R
- image is displaced laterally

$$d \sim L \delta\theta \sim K \delta R$$



- Dispersion in mass, momentum and energy

- from equation above:

$$\frac{\delta R}{R} = \frac{\delta p}{p} = \frac{\delta m}{2m} = \frac{\delta E}{2E}$$

mass dispersion = energy dispersion = $\frac{1}{2}$ momentum dispersion

- momentum dispersion typically in $\text{cm}/\%$
- cannot separate mass and energy dispersion

Deflection spectrometer: resolution and accuracy (1)

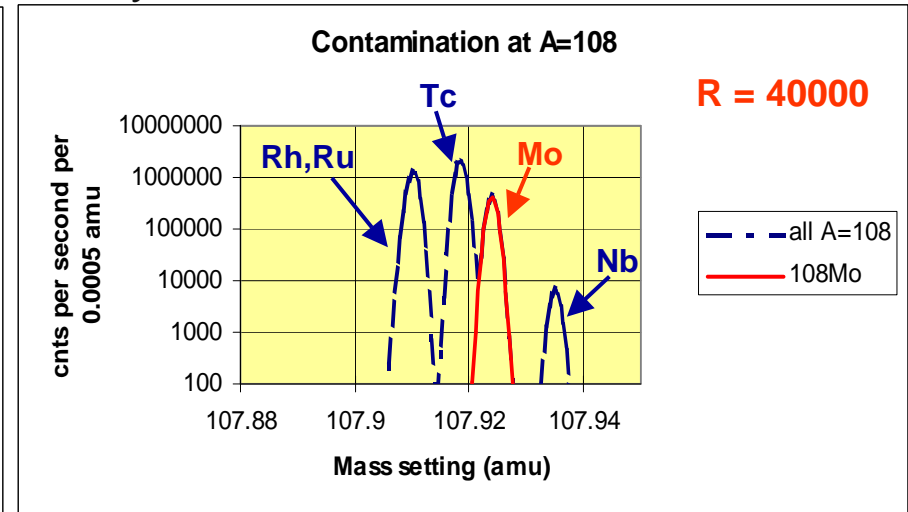
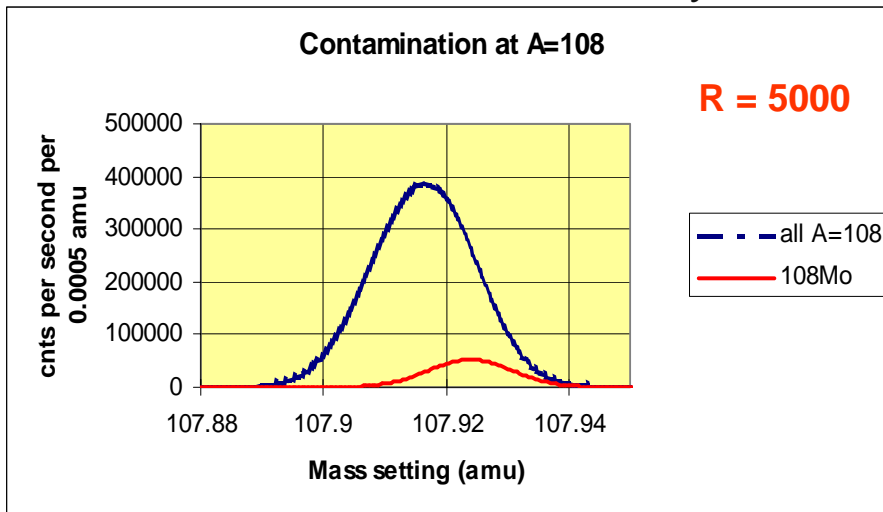
- Resolution is a measure of how well a spectrometer can separate different mass peaks:

$$R = \left(\frac{\text{peak width}}{\text{dispersion}} \right)^{-1} = \left(\frac{f(\varepsilon, \delta E, D)}{D} \right)^{-1} \quad \text{with:} \quad \begin{array}{l} \varepsilon = \text{emittance} \\ \delta E = \text{energy spread} \\ D = \text{dispersion} \end{array}$$

- *Magnetic field imperfections or optical aberrations can limit resolution*
- *resolution not only a function of the spectrometer*
 - *energy spread will limit resolution*
 - *better transverse beam emittance can improve resolution*

- Resolution provides selection

– Can't measure it if you can't identify it!



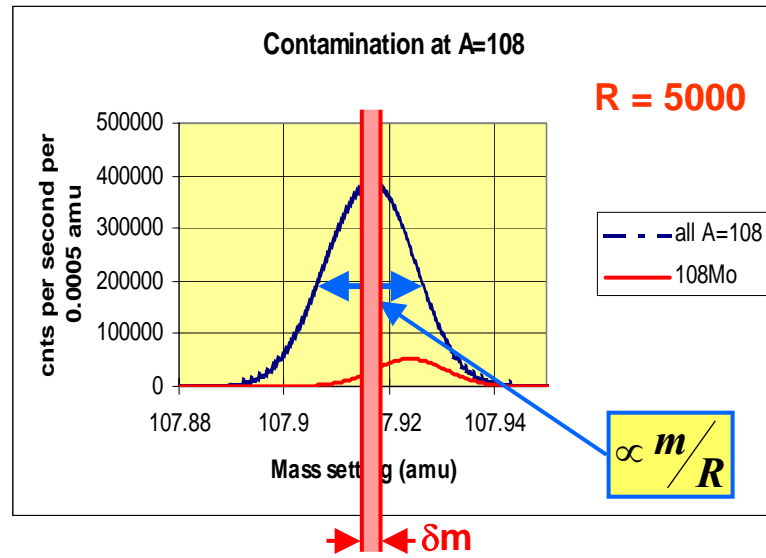
Deflection spectrometer: resolution and accuracy (2)

■ Precision ... and hopefully accuracy

- Precision: how well you can determine the centroid of the peak

$$\delta m \propto \frac{m}{R\sqrt{N}}$$

with:
 δm = mass uncertainty
 R = mass resolution
 N = counts in the peak

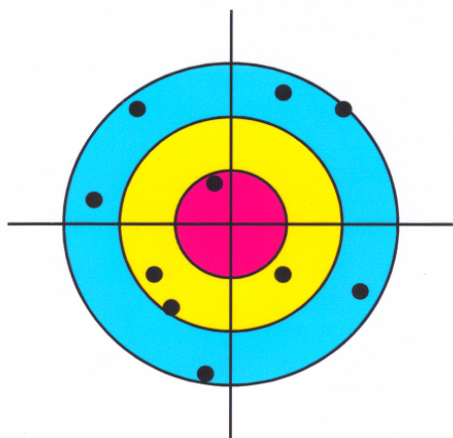


- Accuracy: how well you can relate that centroid to a mass value

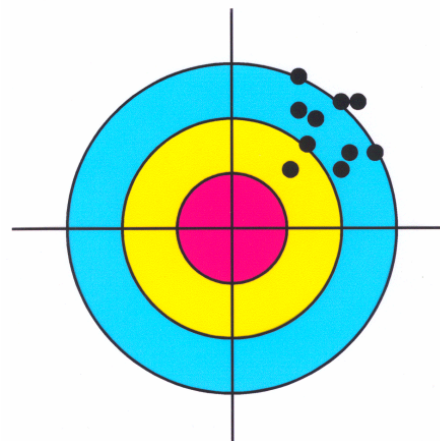
■ Systematic errors

- voltage and magnetic field calibration and stability
- plasma potential, anything that can affect the energy of the ions

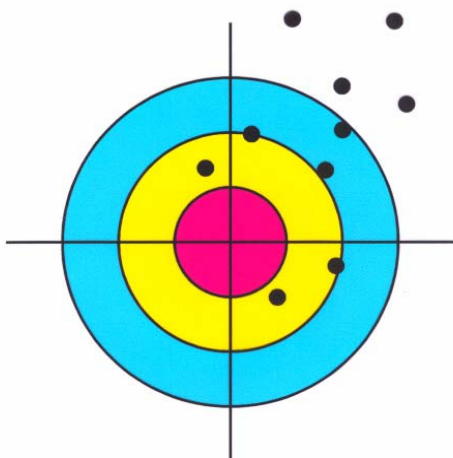
Difference between precision and accuracy



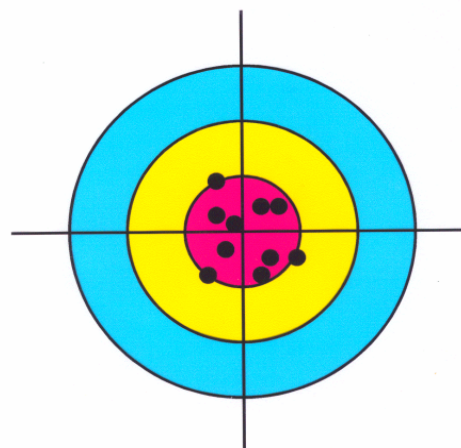
low precision, high accuracy



high precision, low accuracy



low precision, low accuracy



high precision, high accuracy

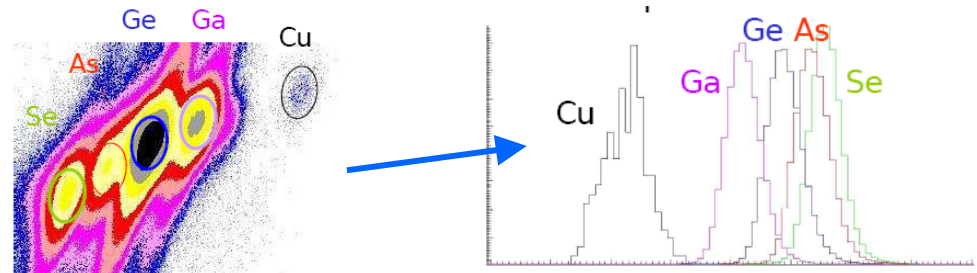
Deflection spectrometer: resolution and accuracy (3)

■ Practically achievable resolution

- Ashton (1918): flat field magnet → $R \sim 130$
- Chalk River (1980s): $n=1/2$ magnet → $R \sim 7000-20000$
- CARIBU (now): 2 flat field magnets → $R \sim 20000$
- limitations
 - *Field homogeneity*
 - *Field and voltage stability*
 - *Beam properties*

■ Achieved accuracy

- Chalk River → $\sim 10^{-6}$ accuracy on short-lived isotopes
 - *decay tagging to improve isobar identification*
- Oak Ridge → $\sim 10^{-5}$ accuracy on short-lived isotopes
 - *energy loss to identify isobars*



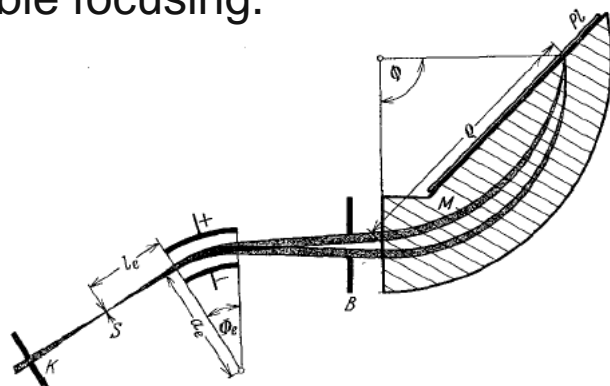
Double focusing spectrometer

- Main limitation of deflection type spectrometer is the intrinsic energy dispersion
- Electrostatic sectors have energy dispersion but no mass dispersion

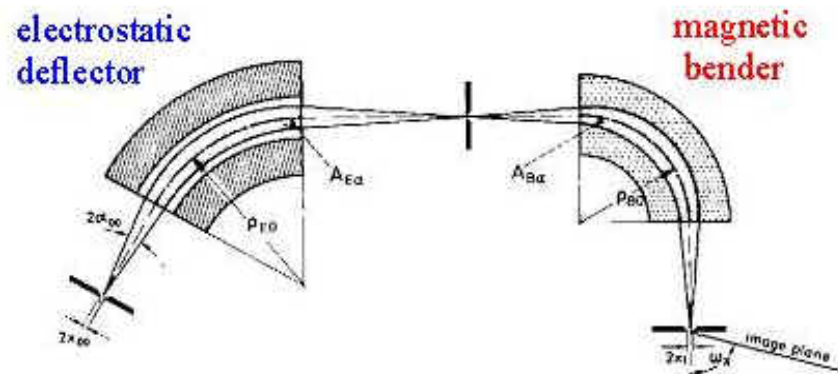
$$F_c = mv^2/R = qE \quad \rightarrow \quad dR/R = dE/E \quad \text{and no mass dispersion}$$

↑
electric field
↑
energy

- Adding an electrostatic sector of equal energy dispersion to a deflection type spectrometer can remove the energy dispersion and significantly enhance the resulting mass resolution. Spectrometer is then focusing in angles and energy ... double focusing.



Mattauch-Herzog spectrometer (1934)



Minnesota, Manitoba I and II (1970s - ...)

Double focusing spectrometer (2)

- Achieved resolution
 - $m/\Delta m \sim 50000$ to 500000 in about a dozen devices
- Precision/accuracy
 - high resolution but limited stability
 - magnetic field fluctuations
 - *temperature variations, electronic noise, ...*
 - *$\Delta B/B < 10^{-6}$ is hard when not closed loop superconducting*
 - voltage fluctuations, ...
 - Solve by fast peak matching and averaging
 - jump from one peak to the other at the rate faster than the fluctuations
 - Accuracy of $\sim 2-3 \times 10^{-9}$ with Argonne, Minnesota and Manitoba II spectrometers
- Still subject to systematic errors due to ion source effective potential

Time-of-flight mass spectrometer

- Basic TOF spectrometer (first proposed by Stephens in 1946)

- charged particle in an electric field E of length d gains energy V_0 and drift over distance L before reaching a detector

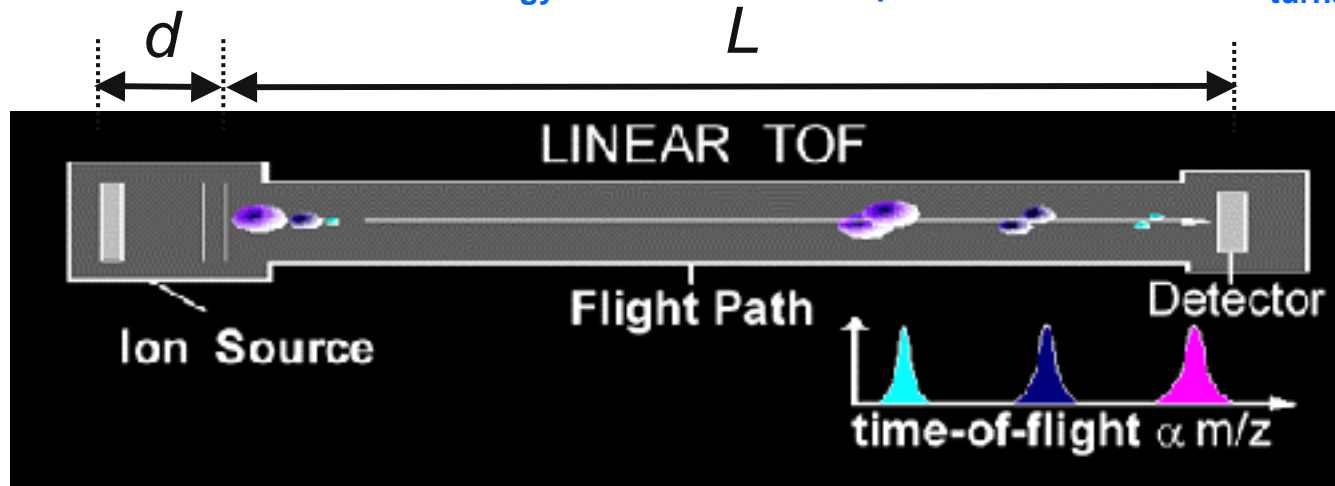
- For ions initially at rest we get:

$$t = t_s + t_D \quad ; \quad t = \left(\frac{2md}{eE} \right)^{\frac{1}{2}} + L \left(\frac{m}{2eV_0} \right)^{\frac{1}{2}} \quad \longrightarrow \quad \boxed{\frac{\Delta m}{m} = \frac{2\Delta t}{t}}$$

- If the ions starts with an initial energy U_0 at position s_0 :

$$t = t_s + t_D + t_0 \quad ; \quad t = \frac{(2m)^{\frac{1}{2}}}{eE} \left[(U_0 + eEs_0)^{\frac{1}{2}} + U_0^{\frac{1}{2}} \right] + \frac{(2m)^{\frac{1}{2}} D}{2(U_0 + eEs_0)^{\frac{1}{2}}} + t_0$$

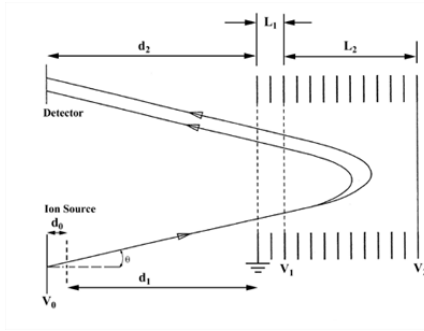
Initial energy
Initial position
turnaround time



Time-of-flight mass spectrometer

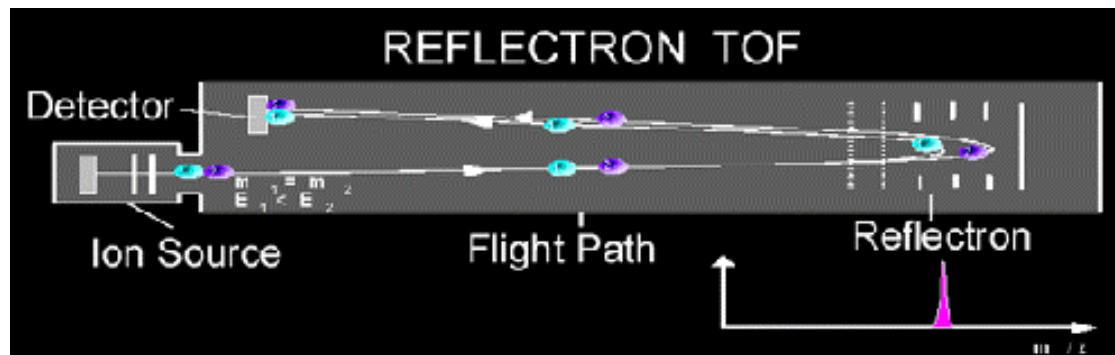
■ Reflectron TOF spectrometer

- correct for initial energy spread by having higher energy ions go through a longer path inside an electrostatic reflector

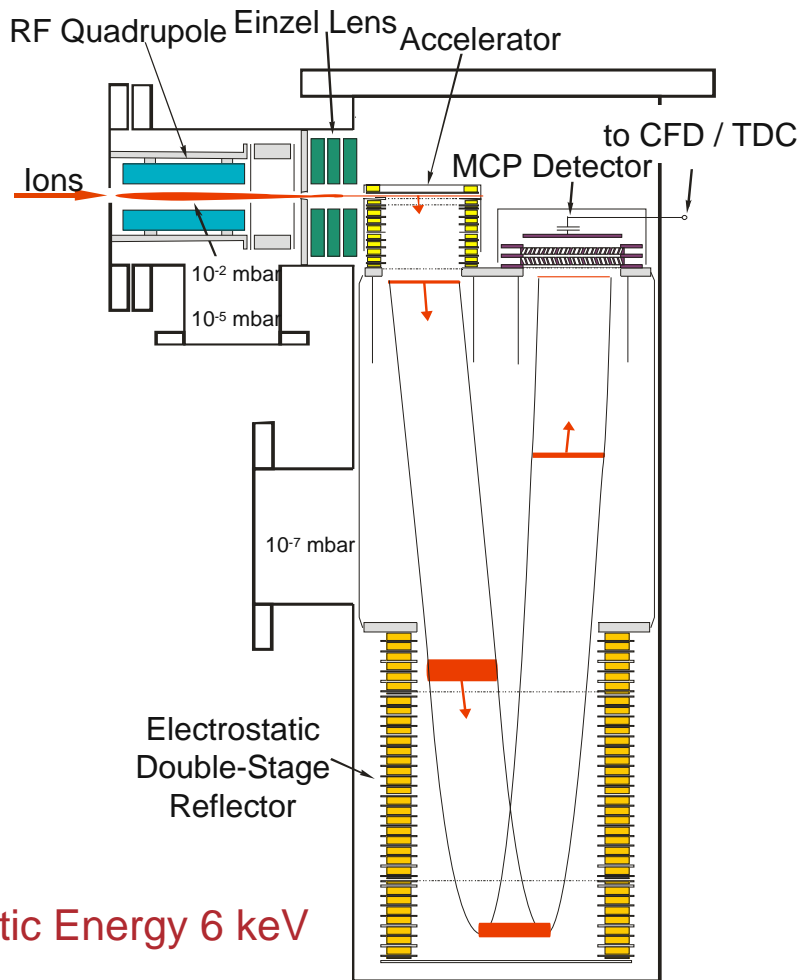


- still get a simple a simple mass-tof relationship after calibration, but with better resolution

$$m = q(at + b)^2$$



Ortho-TOF mass spectrometer



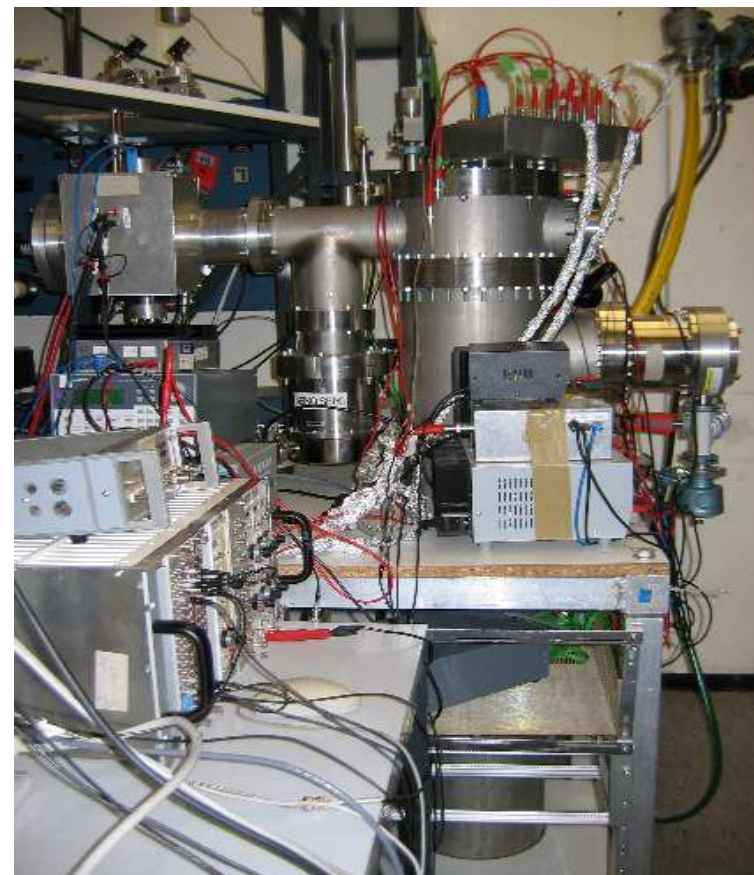
Kinetic Energy 6 keV

Mass Resolving Power: $10^4 \dots 2 \cdot 10^4$

Mass Measurement Accuracy: $1-3 \times 10^{-6}$

Overall Efficiency (Cooling, Bunching, Mass Analysis, Detection): 1-3 %

Mass Measurement Cycle Duration: < 1 ms



1.7 m

(W.R. Plaß)

Ortho-TOF spectrometer (2)

■ advantage

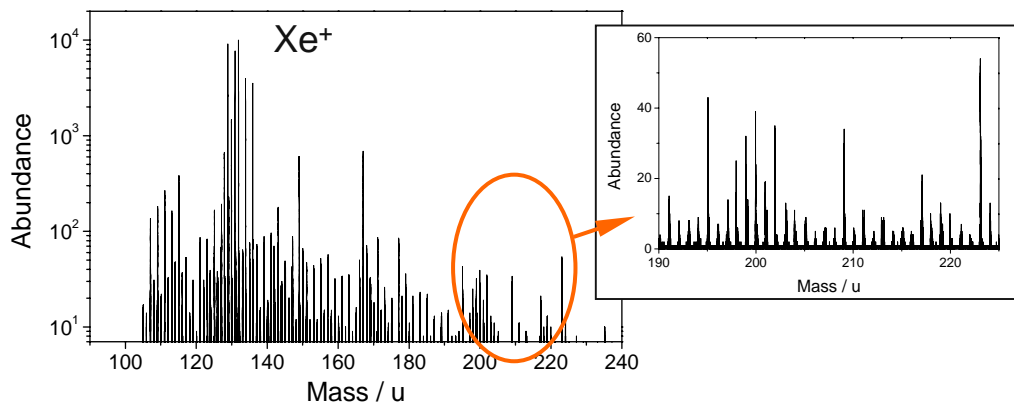
- full mass spectra can be observed in one shot
- fast
- no practical mass range limit

■ disadvantage

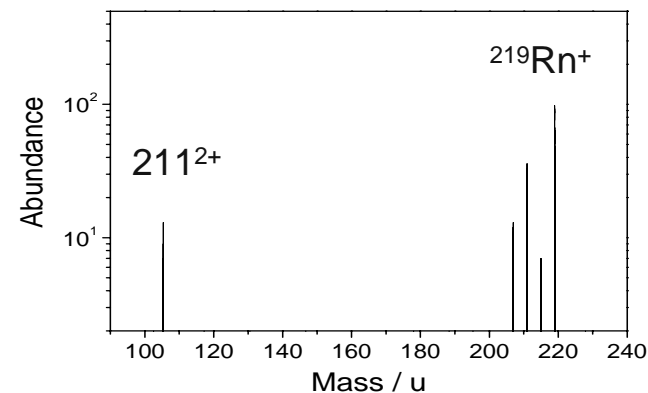
- requires a **start signal** → pulsed beam
- requires a good quality low energy beam

Diagnosis of gas catcher purity

No cold trap, no baking

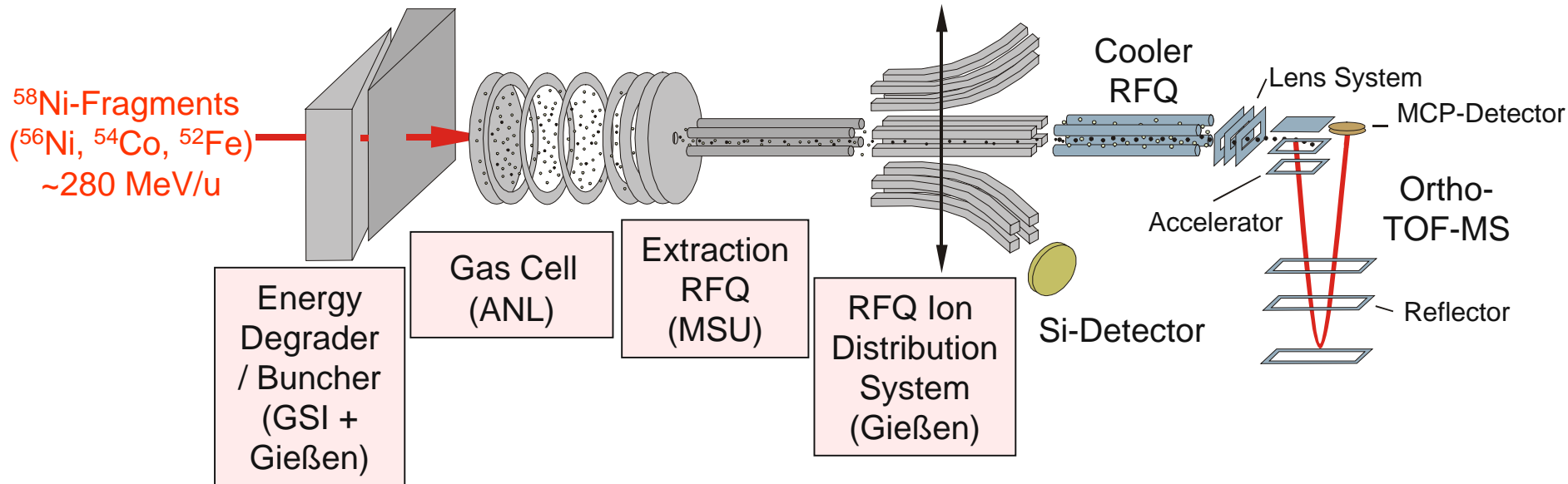


cold trap, after baking



Ortho-TOF spectrometer (3)

- Achieving the right beam properties to use such devices online can mean a significant investment in the front end at fast beam facilities



TOF spectrometer: SPEG at GANIL

- Use GANIL as a whole as a TOF spectrometer

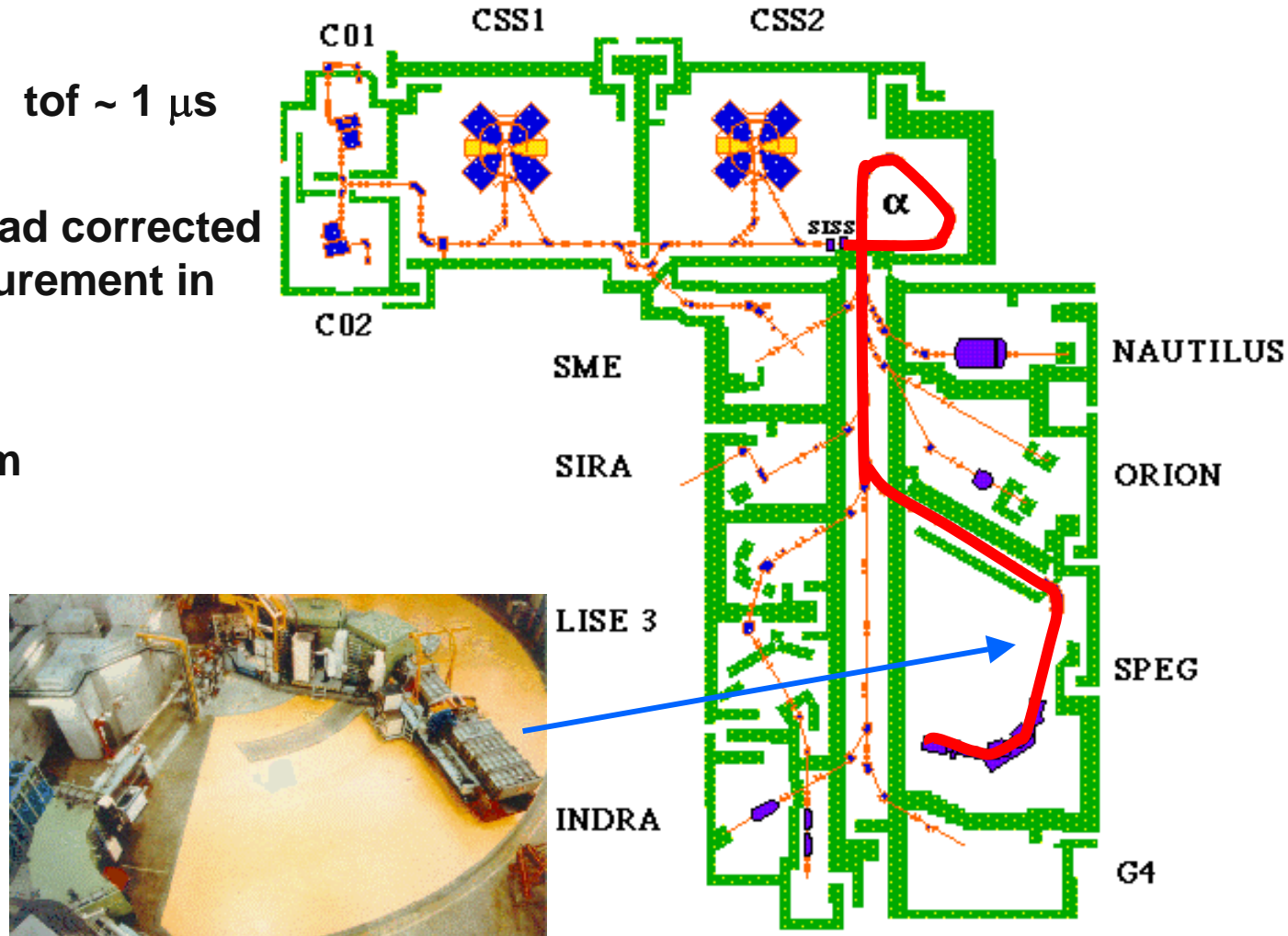
- long flight path

$L \sim 82 \text{ m} \rightarrow \text{tof} \sim 1 \mu\text{s}$

- momentum spread corrected by rigidity measurement in SPEG

- obtain mass from

$$B\rho = \gamma m_0 v / q$$



TOF spectrometer: SPEG at GANIL (2)

■ Advantage

- well matched to GANIL energies (~ 90 MeV/u)
- produce many species simultaneously
 - *calibration*
- isotope with very short lifetime can be measured
- extremely sensitive ... far reach

■ Disadvantage

- limited resolution
 - 200 ps / 1 μ s $\sim 2 \times 10^{-4}$
- limited accuracy
 - $\sim 10^{-5} - 10^{-6}$

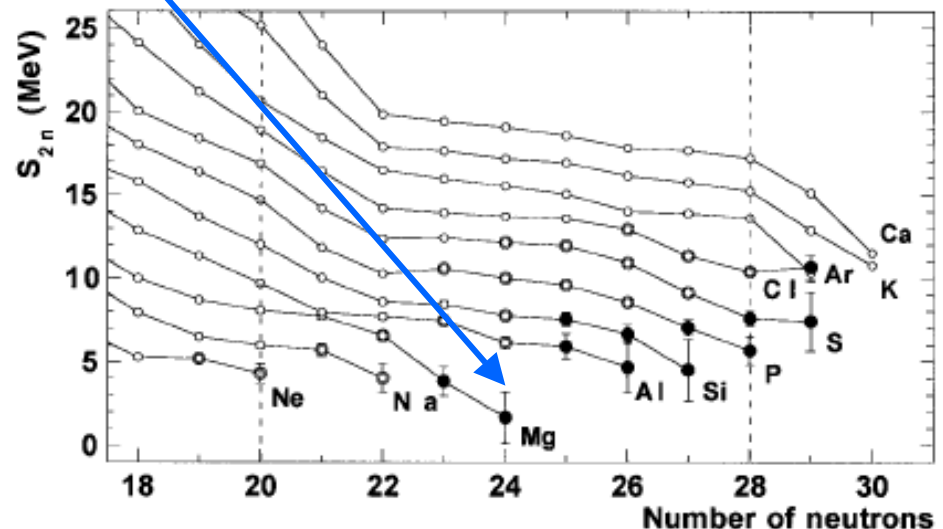
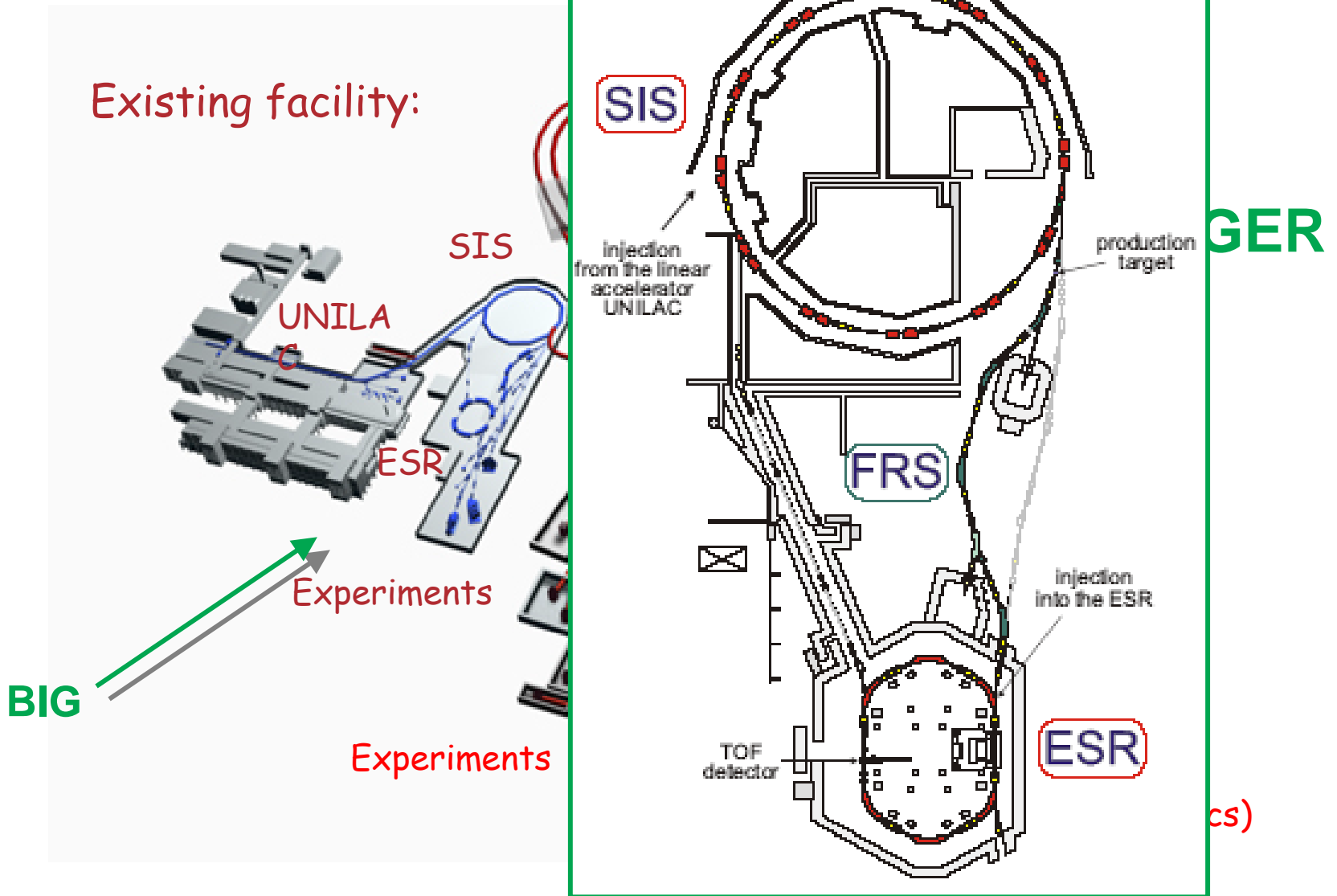


Figure 4. Experimental S_{2n} values in the region of the $N = 20$ and $N = 28$ shell closures. The circles correspond to values from [25], the bold circles to values for which the precision was improved and the full circles to masses measured for the first time.

TOF spectrometer: resolution limited by flight path



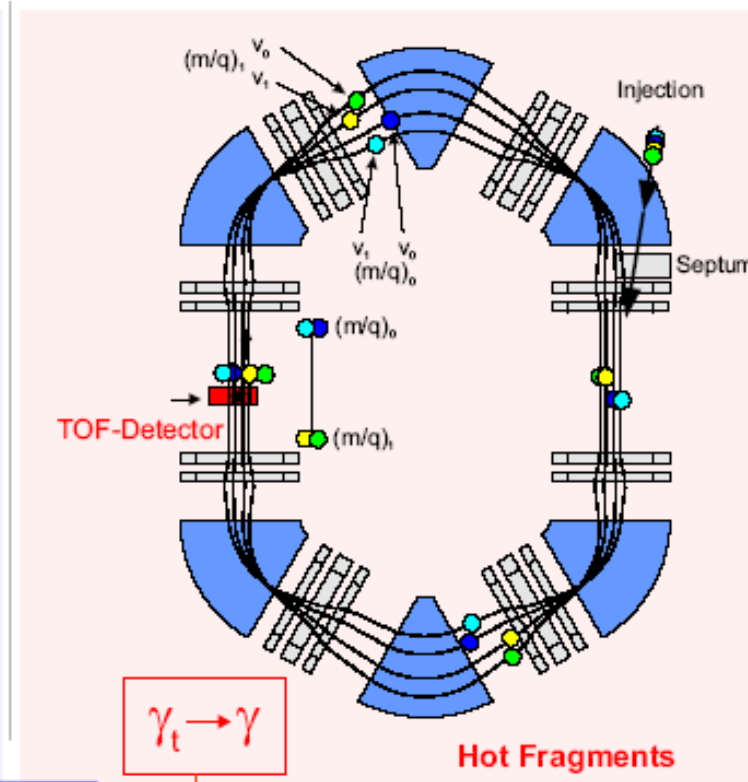
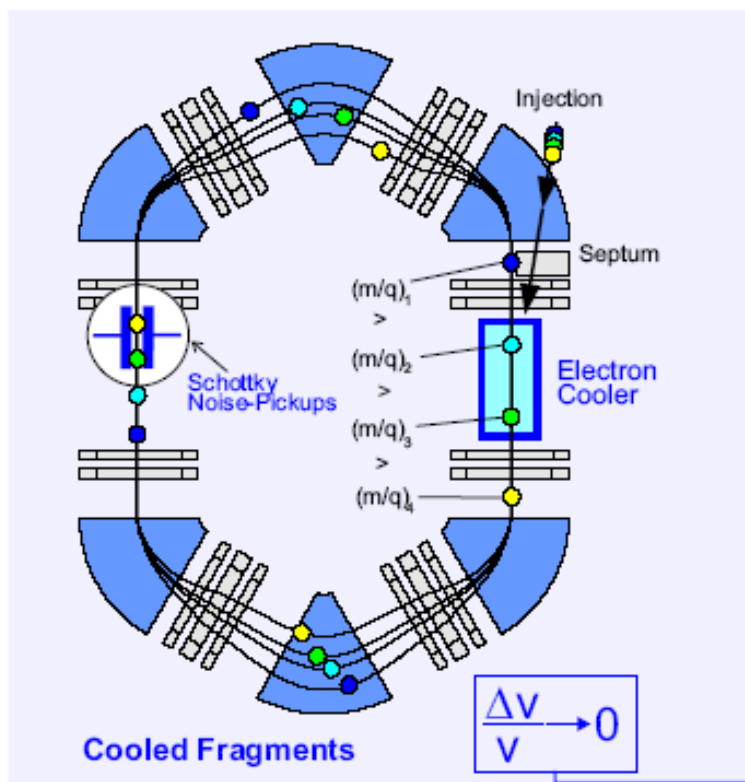
TOF mass measurements at the ESR

- To get resolution in a TOF system, you need distance

→ storage ring in isochronous mode ←

SCHOTTKY MASS SPECTROMETRY

ISOCHRONOUS MASS SPECTROMETRY



$$\frac{\Delta f}{f} = -\frac{1}{\gamma_t^2} \frac{\Delta(m/q)}{m/q} + \frac{\Delta v}{v} (1 - \frac{\gamma^2}{\gamma_t^2})$$

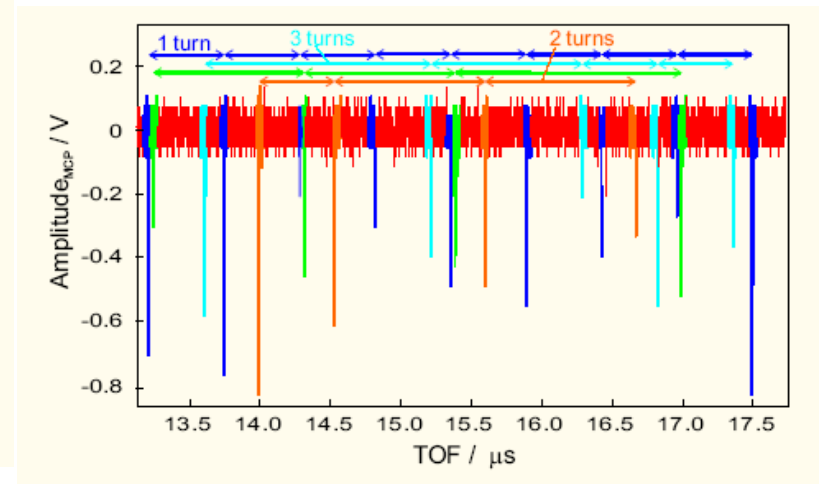
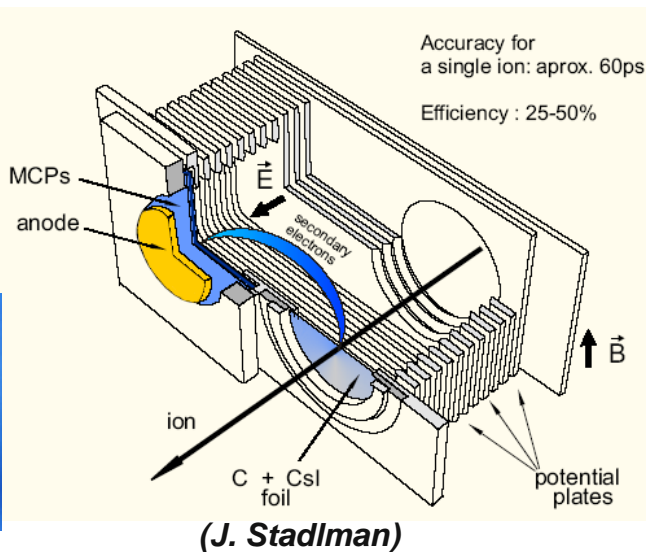
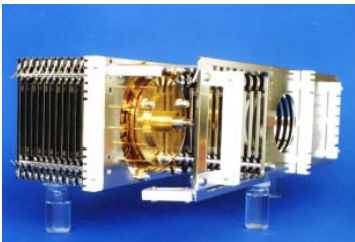
TOF mass measurements at the ESR (2)

- Last term in frequency equation below must be made small
 - Reduce energy spread by cooling → introduce long delay
 - Run ring in isochronous mode → no cooling required

$$\frac{\Delta f}{f} = -\frac{1}{\gamma_t^2} \frac{\Delta(m/q)}{m/q} + \frac{\Delta v}{v} \left(1 - \frac{\gamma^2}{\gamma_t^2}\right) \rightarrow 0$$

$\frac{\Delta v}{v} \rightarrow 0$ $\gamma_t \rightarrow \gamma$

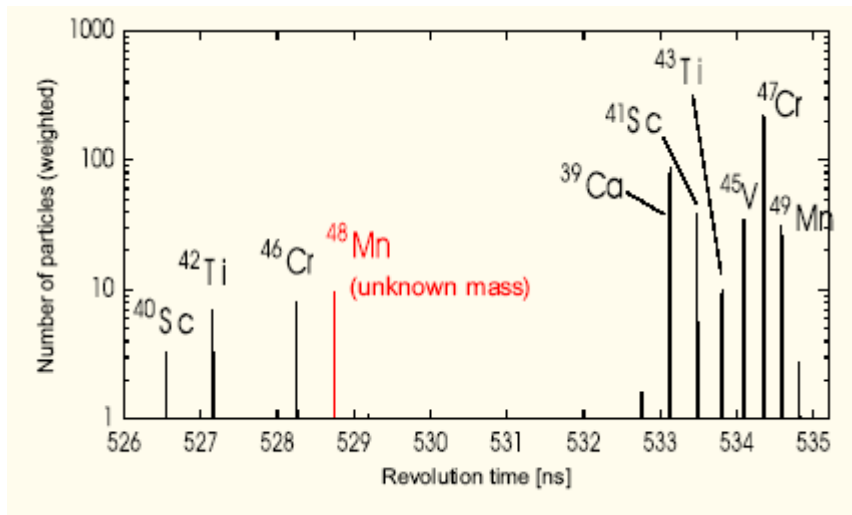
- Fast but need “transparent” detector (Schottky not applicable here)



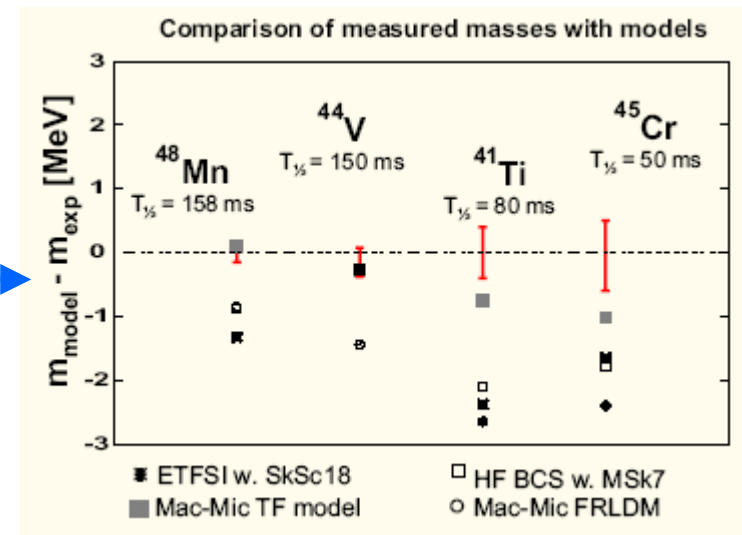
TOF mass measurements at the ESR (3)

■ Performance

- resolution ~ 100000
- essentially no lifetime limitation
- limited accuracy $\sim 10^{-6}$
- can access many masses simultaneously
- well matched to the GSI facility
- main limitation is acceptance into FRS



(J. Stadlman)



Mass measurements and radioactive beam properties

- Most of the mass measurement techniques we have seen so far have their resolution and ultimate accuracy affected by the beam properties
 - Resolution of deflection type spectrometer limited by energy spread and transverse emittance
 - Double focusing spectrometers affected by transverse emittance and variation of energy with species
 - Low energy TOF system affected by initial energy spread and requiring a pulsed beam structure
 - ESR TOF resolution and accuracy limited by the quality of the isochronicity of the ESR ring

To obtain the utmost accuracy, cooling is required.

- This not only improves the applications we have seen, it also opens the door to the highest accuracy ones:

[Ion traps and storage rings](#)

Cooling: Physical considerations

- Liouville's theorem (paraphrasing)

- phase-space density is conserved in a non-dissipative system

- i.e.:

angular spread X radial spread → constant

time spread X energy spread → constant

- Cooling or bunching (**reduction of transverse or longitudinal phase-space**) therefore requires a dissipative system with the following conditions

- “Cold” thermal bath (electrons, gas, laser beam, ...)

- Interaction of “ion beam” with the thermal bath

- Sufficient acceptance of the bath and interaction time with the bath

- Capability to extract from the bath without substantial reheating

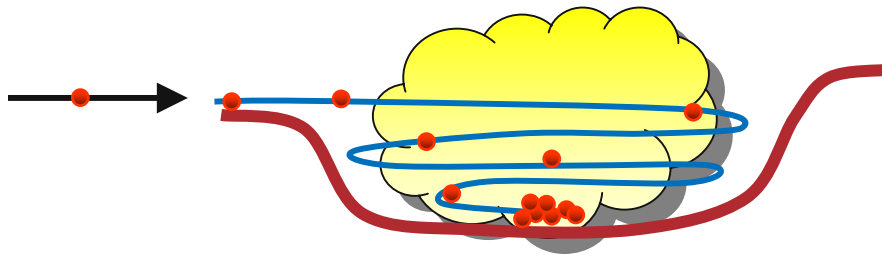
One road to fast and universal cooling/bunching

Collisions with a buffer gas in a guiding/trapping structure

- gas provides thermal bath
- guiding/trapping structure provides large interaction time and localization

Conditions to be met

- enough stopping/cooling power to capture in longitudinal potential after one “interaction length”
- guiding/trapping potential/volume large enough to accept initial transverse emittance and energy spread after one “interaction length”



Acceptance/stopping requirements for different radioactive ion sources

- Radioactive ion source

1) poor quality ISOL beam

Beam ~ 30 - 60 keV ; $\Delta E \sim 1 - 100$ eV ; emittance ~ up to 100π mm mrad

approach: electrostatic deceleration to 100 eV, absorb remaining energy in gas ... transverse guiding potential about 10-20 eV

2) fusion-evaporation reaction

Recoils energy ~ 0.2 - 5 MeV/u ; $\Delta p/p \sim 1 - 15\%$

typical: **Sn @ 3MeV/u** Range ~ 4.6 mg/cm² straggling ~ 0.2 mg/cm²

approach: remove most energy in solids, absorb final range straggling in gas... recoil spectrometer sets transverse size

3) fragmentation or in-flight fission reaction

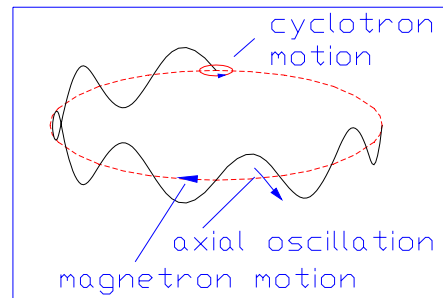
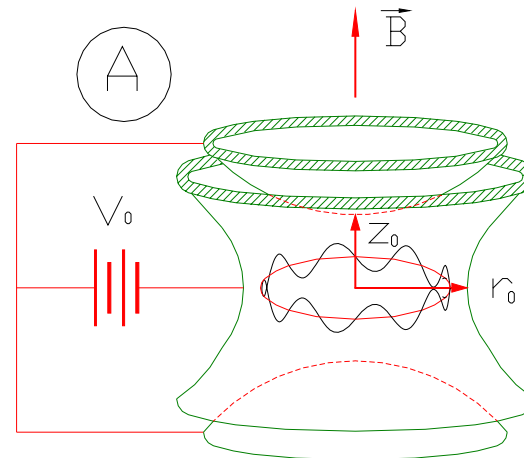
Recoils energy ~ 100 - 1000 MeV/u ; $\Delta p/p \sim 1-20\%$

typical: **Sn @ 250 MeV/u** Range ~ 2.2 g/cm² straggling ~ 3 mg/cm²

approach: minimize energy spread, remove most energy in solids, absorb final range straggling in gas... fragment separator sets transverse size

Guiding/trapping structure(s)

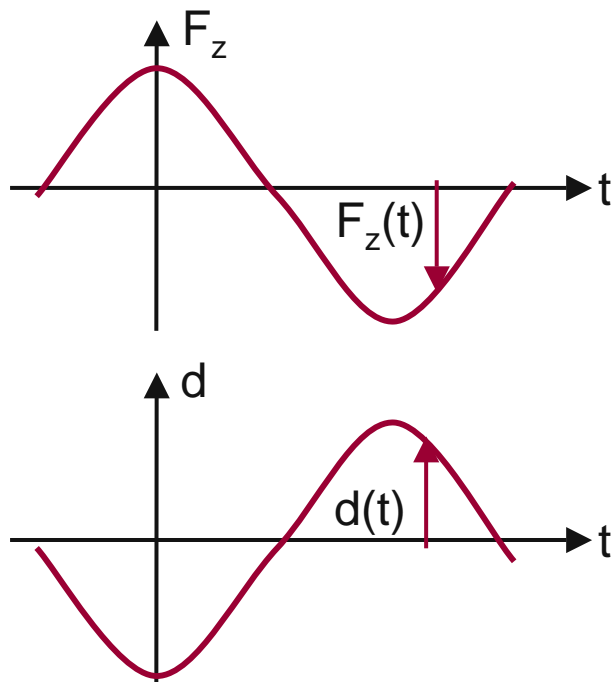
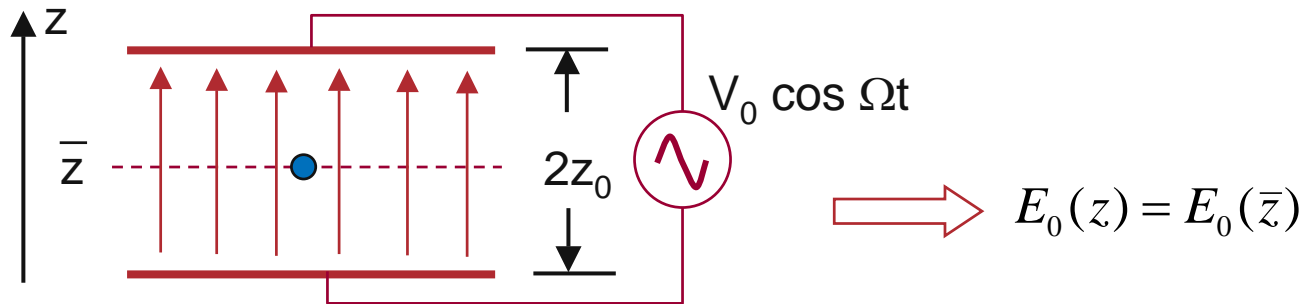
Penning
Trap



*More of a
measurement device
... we will come back
to it later*

RF focusing(1)

Uniform
RF field



Basic harmonic motion

$$m\ddot{z} = F_z(t) = eE_0(z) \cos \Omega t$$

$$z(t) = \bar{z} + d(t)$$

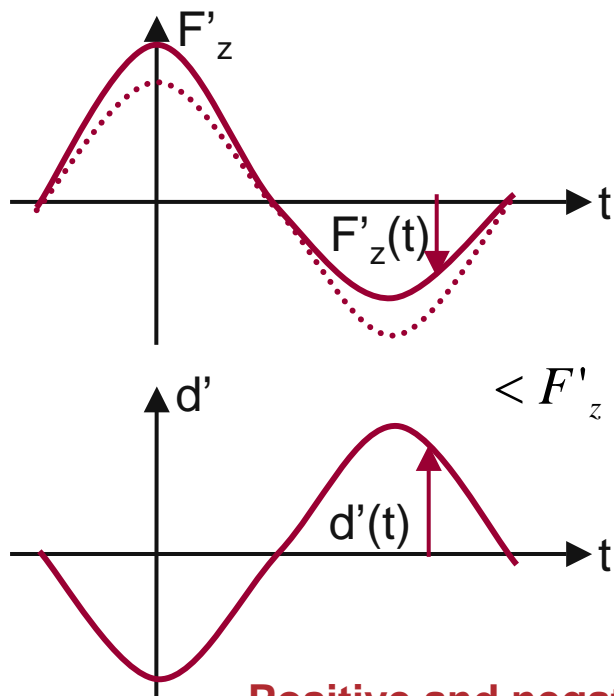
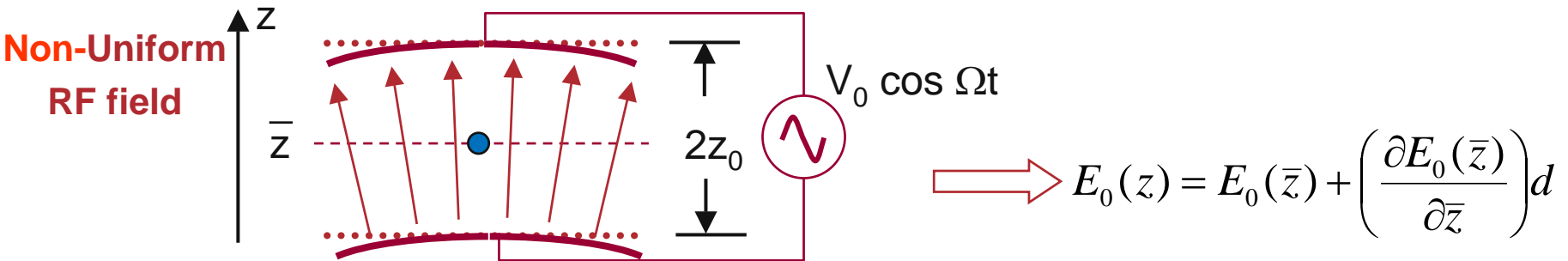
$$d(t) = -d_0 \cos \Omega t$$

$$d_0 = \frac{eE_0(\bar{z})}{m\Omega^2}$$

$$\langle F_z(t) \rangle_{av} = eE_0(\bar{z}) \langle \cos \Omega t \rangle = 0$$

No net force when averaged over full RF cycle!

RF focusing(2)



$$m\ddot{z} = F'_z(t) = eE_0(z) \cos \Omega t$$

$$z(t) = \bar{z} + d'(t)$$

$$d'(t) \cong d(t) = -d_0 \cos \Omega t$$

$$d_0 = \frac{eE_0(\bar{z})}{m\Omega^2}$$

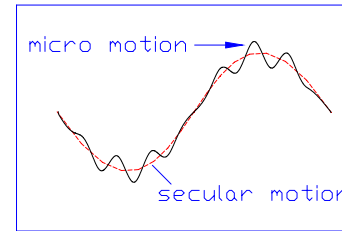
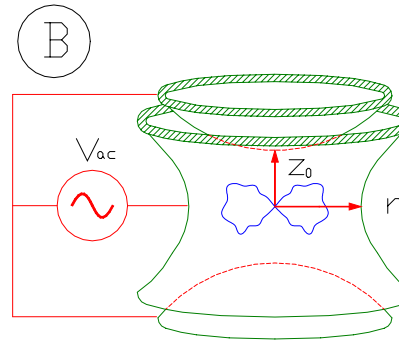
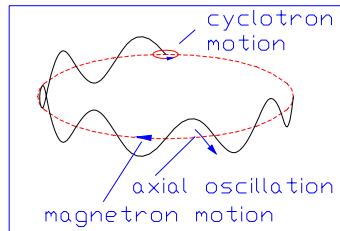
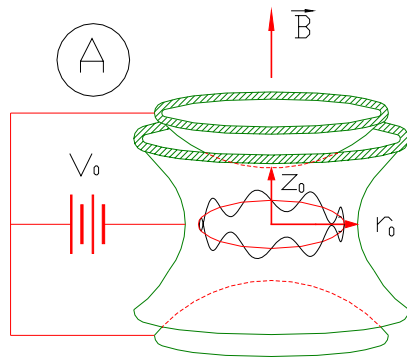
$$\langle F'_z(t) \rangle_{av} = e \left(\frac{\partial E_0(\bar{z})}{\partial \bar{z}} \right) \langle d' \cos \Omega t \rangle = \frac{-e^2 E_0(\bar{z})}{2m\Omega^2} \left(\frac{\partial E_0(\bar{z})}{\partial \bar{z}} \right)$$

$$F' = -e \frac{\partial V_{ps}}{\partial z} \Rightarrow V_{ps} = \frac{eE_0^2(z)}{4m\Omega^2}$$

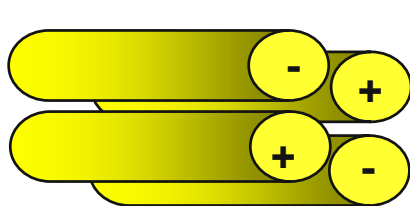
Positive and negative charges attracted to regions of lower RF amplitude!

Guiding/trapping structures

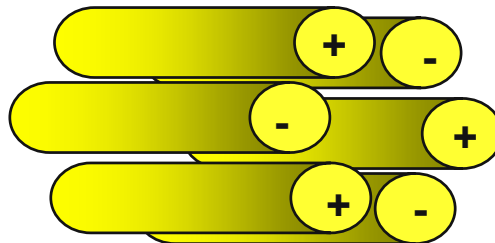
Penning Trap



RFQ Trap

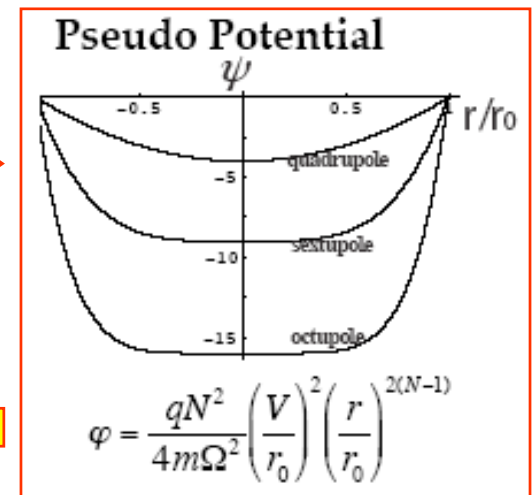
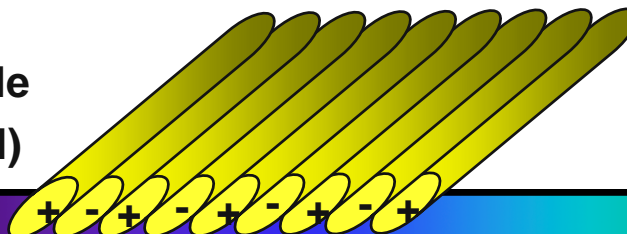


RF quadrupole



RF hexapole

Centipole (RF wall)



Low energy beam coolers

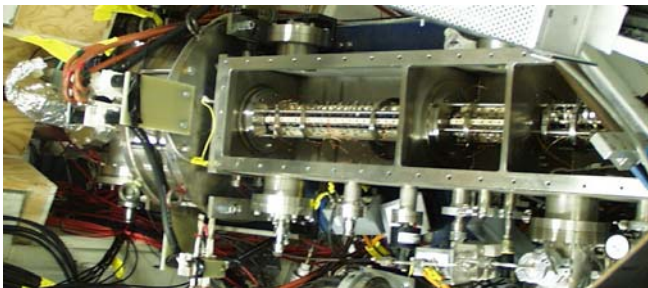
RF structures provide enough radial confinement and stopping length

First on-line attempt → Paul trap to bunch ISOLDE beam (R.B. Moore et al)

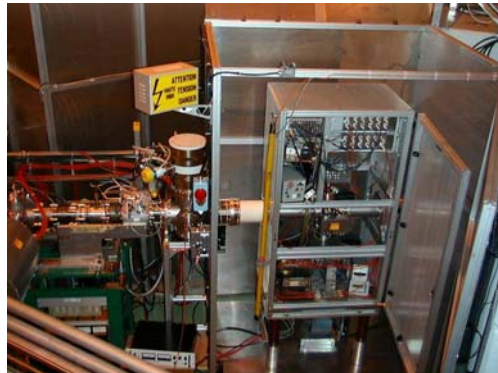
Linear RF structure provide more stopping length so higher efficiency

- efficiency ~ 30-70% with beam deceleration
> 90% from a low energy beam
- energy spread < 1eV
- Transverse emittance ~ 3π mm mrad

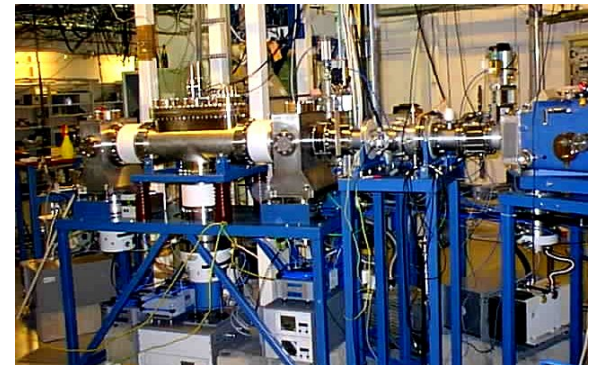
More than a dozen RFQ coolers in operation/construction in nuclear physics labs!



3 RFQ sections to extract from high gas flow region



Bunch low energy beam to match to experiment

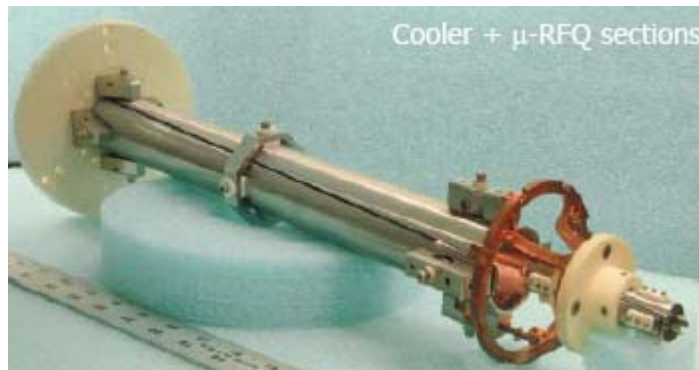


Reduce energy spread in DC mode

Further developments of low energy coolers

- Decoupling of DC and RF drives → Wada et al for a while now but becoming more widespread

- Cooling of RF structure to liquid nitrogen temperature (MSU)



- Square wave RF drive (ISAC)

- Cooling for lighter species (CAEN) → Helium cooled

Cooling/bunching of fusion-evaporation residues

Transverse emittance too high for any realistic small trapping device to handle (MV potential required)

Need a different approach

- **remove much of the energy before entering the device**
- **use gas to handle energy spread and range straggling**
- **once thermalized, use the fact that residues are ionized to guide them out selectively from stopping volume**

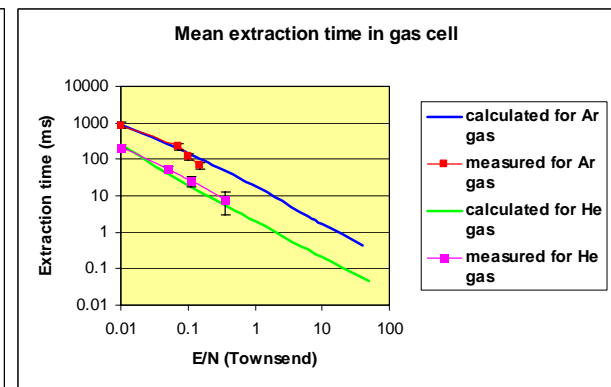
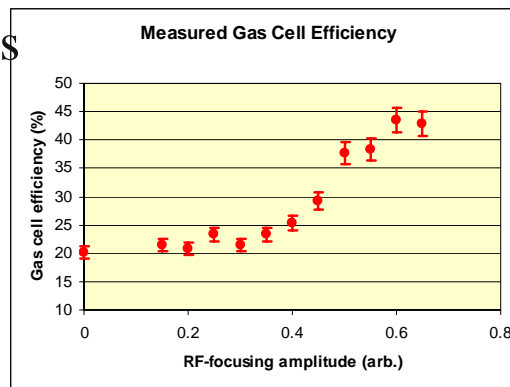
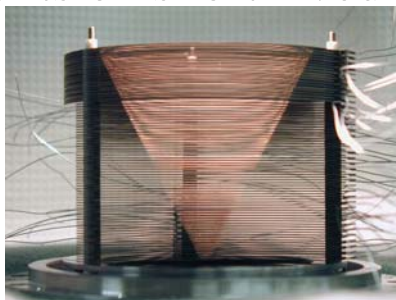
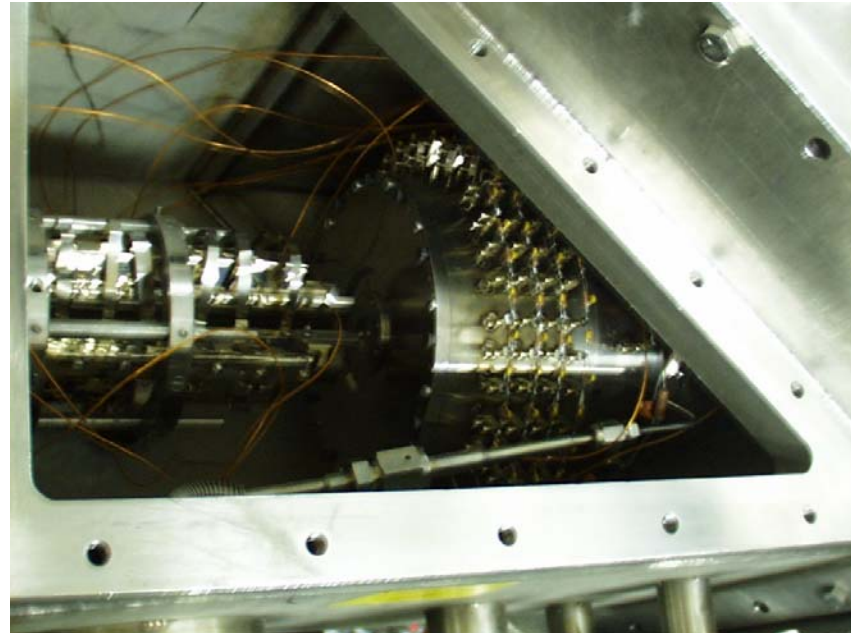
Gas volume requirement

- **longitudinally roughly 0.1 – 1 mg/cm² He**
- **laterally depends on ion optics but typically 5 – 10 cm diameter**

Too large a gas volume for a standard confining ion guide/trap!

Gas catcher developed at the Canadian Penning Trap (CPT) at ATLAS

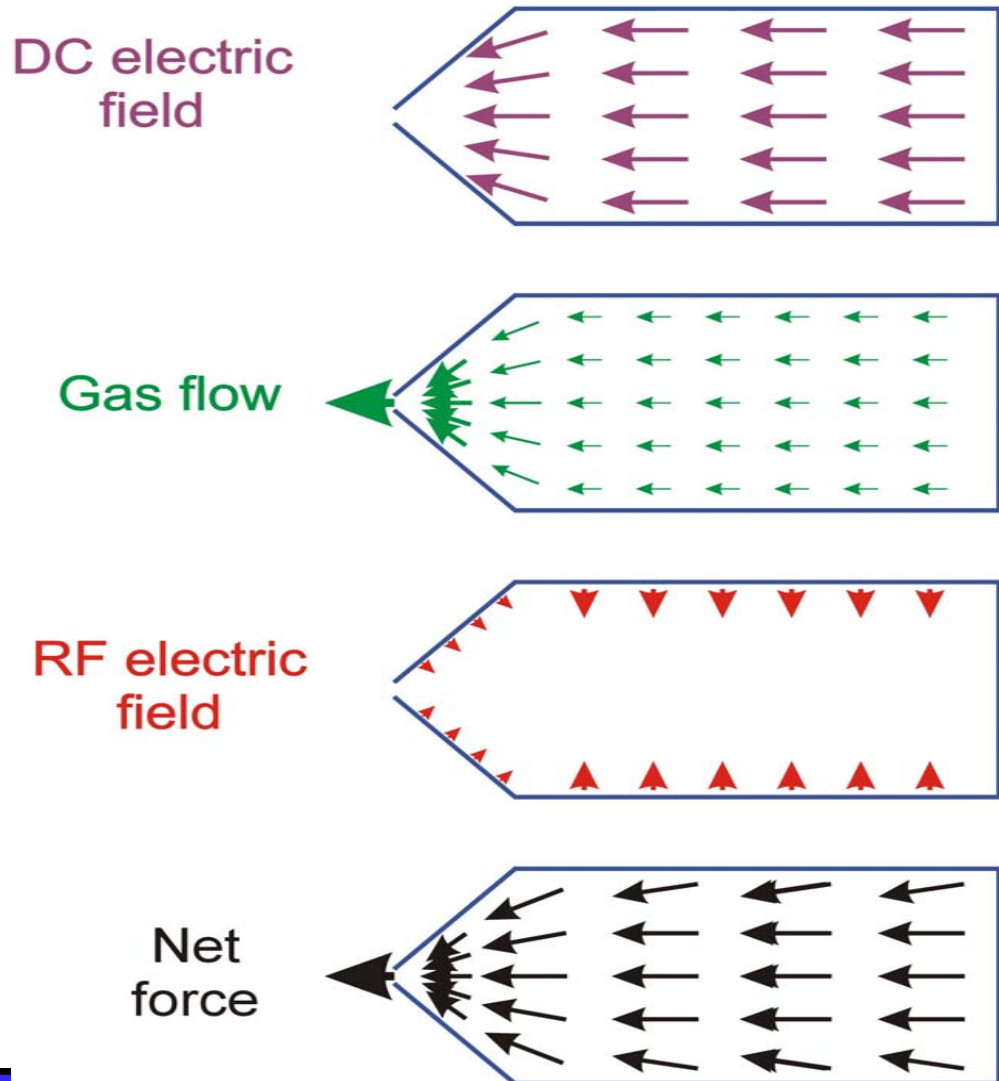
- 20 cm long gas cell with first generation RF cone
- $\varepsilon \sim 45\%$
- mean delay time below 10 ms
- tested off-line with fission products and on-line with fusion–evaporation reactions
- routinely used for physics with CPT at Argonne for mass measurements on short-lived isotopes



Forces in gas catcher system

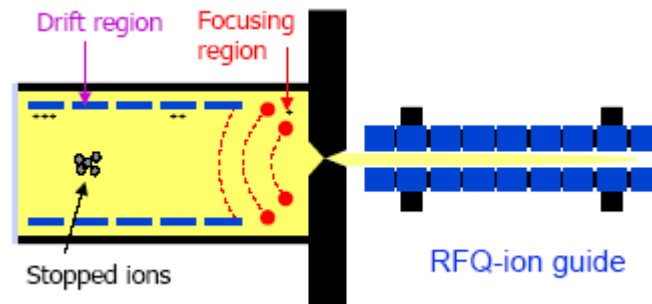
A combination of forces working together is required to obtain

- Fast extraction times over the full volume
- High efficiency over the full volume
- Tolerance to high intensity

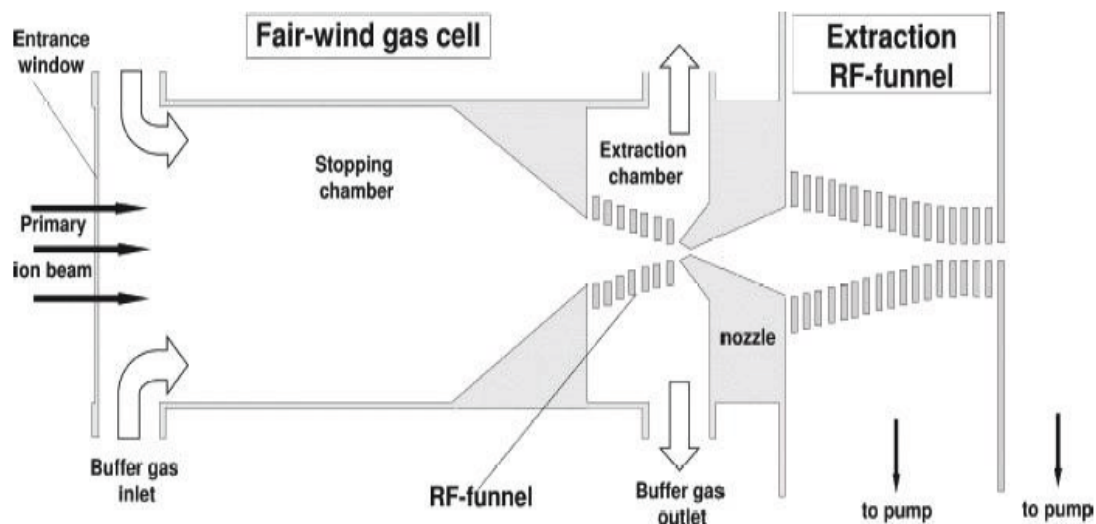


Other approaches being pursued

- No RF focusing, plain DC and gas flow

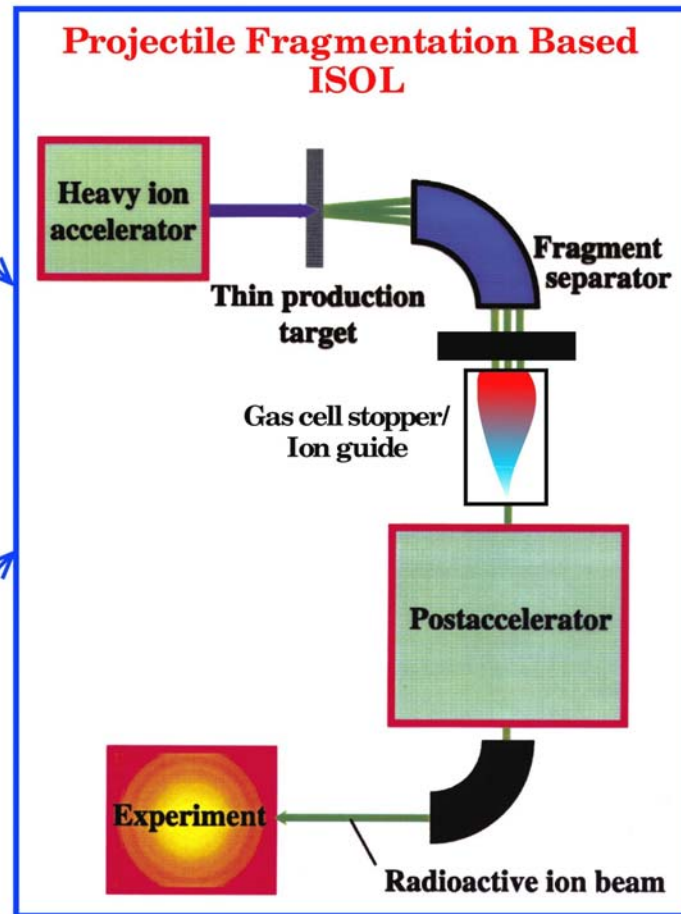
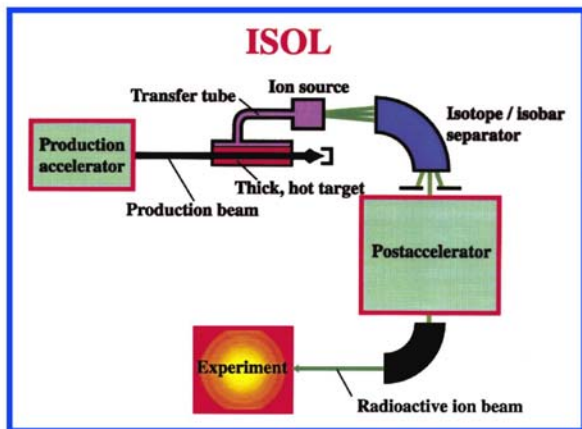
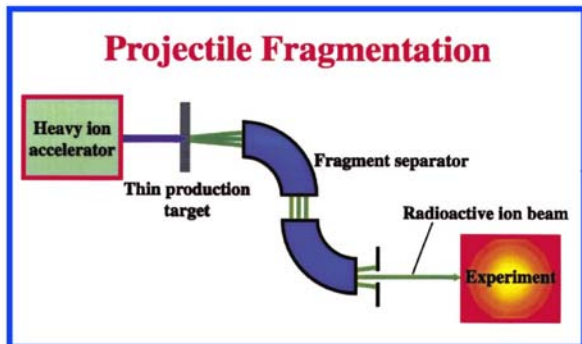


- Forced gas flow transport throughout catcher



Rare Isotope Production Schemes

- Fast Extraction Times (\sim msec)
- Chemical independence
- Isobar separation

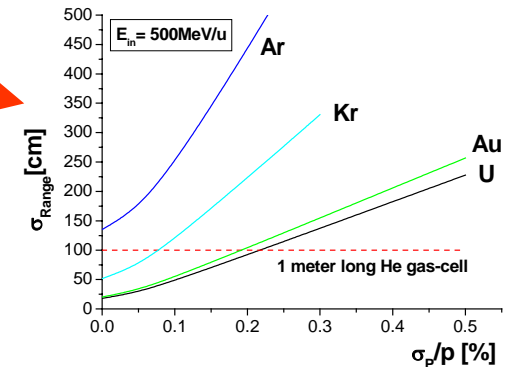


Cooling/bunching of fragmentation/in-flight fission residues

Transverse emittance too high for any realistic **small** trapping device to handle (multi MV potential required), range straggling too large also

Sn @ 250 MeV/u – 24 cm in 0.5 atm He

Same with $\Delta p = 0.1\%$ --- 70 cm



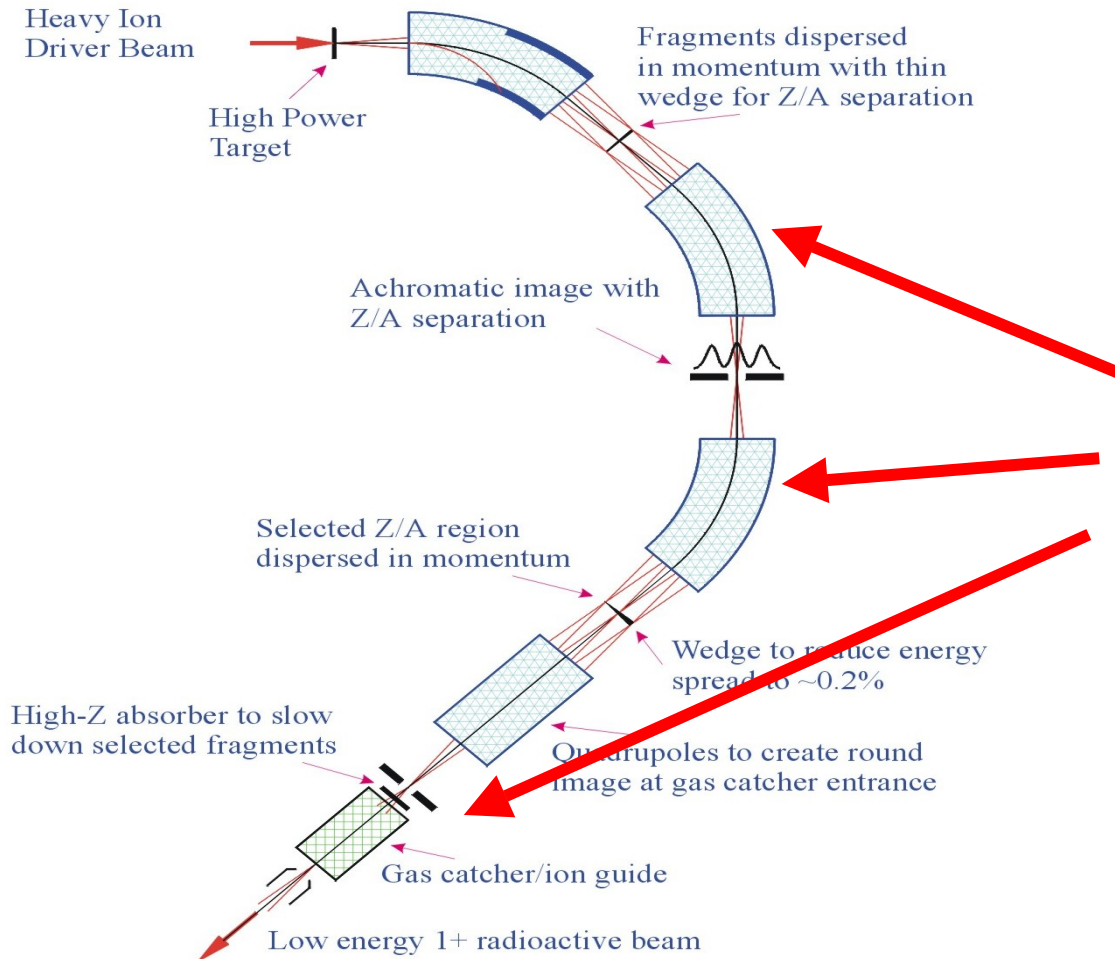
Need a more complex approach

- must first reduce energy spread
- remove much of the remaining energy before entering the device
- use gas to handle residual range straggling
- once thermalized, use the fact that residues are ionized to guide them out selectively from stopping volume

Gas volume requirement

- longitudinally roughly 2 – 20 mg/cm² He
- laterally depends on ion optics and achromatization

Schematic layout for gas catcher and fragment separator

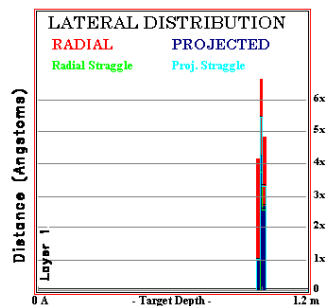
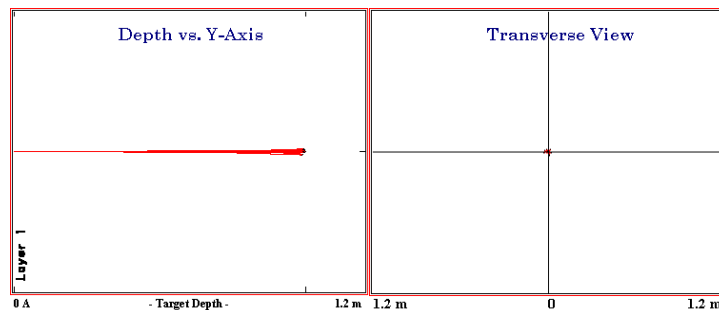
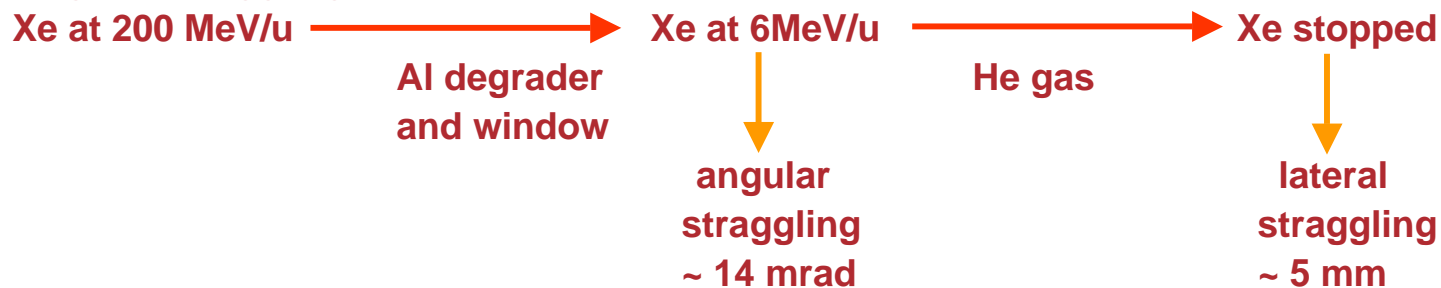


Schematic layout of fragment separator, achromatization stage and gas catcher system

Lateral dimension of large gas catcher

Lateral dimension of FRS gas catcher is determined by:

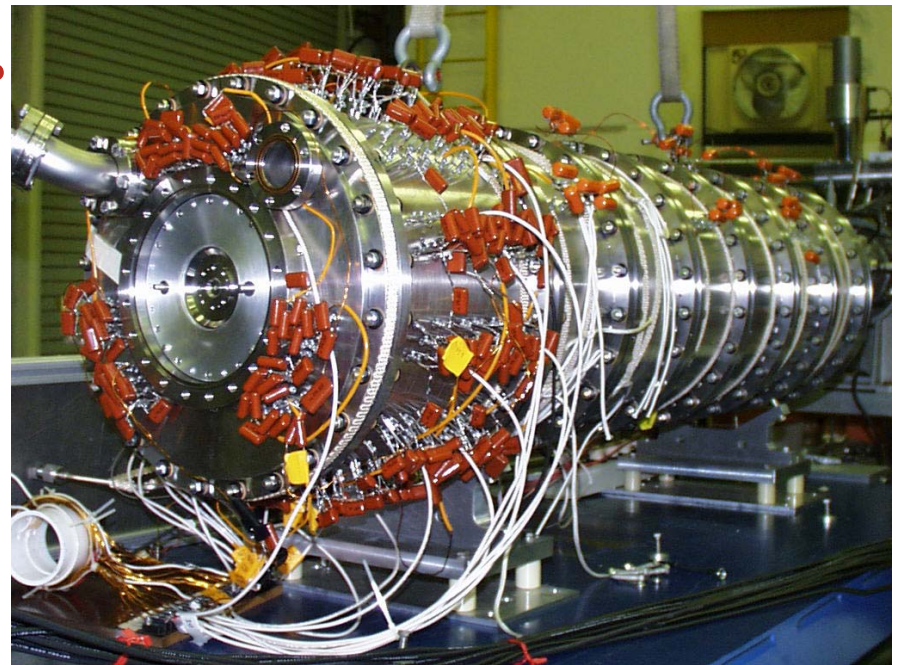
- Dispersion at wedge degrader
- Angular acceptance and magnification
- Angular straggling in deceleration
 - FRS acceptance : $\pm 1\%$ dp/p
 - Dispersion required for achromatization: 7cm / %
 - Angular acceptance : ± 10 mrad
 - Magnification : $\sim 1.0 - 1.2$
 - Angular straggling:



$\phi_{\text{gas catcher}} \sim 20-25 \text{ cm}$

Full scale RIA gas cell prototype

- 1.25 meter long(1.4 for GSI test), 0.25 meter inner diameter gas cell with same features as $\frac{1}{4}$ scale prototype
- over 7400 components, with more than 4000 prepared to UHV standards
- **Assembly completed FY02 DOE/NP Performance Target.**
- **Characterization at low energy at ATLAS**
- **International collaboration testing full scale prototype at RIA energy at the fragment separator at GSI**



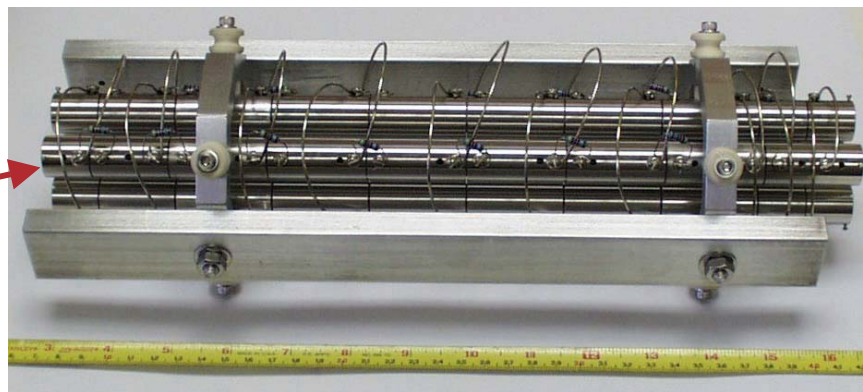
Completed large extraction RF cone



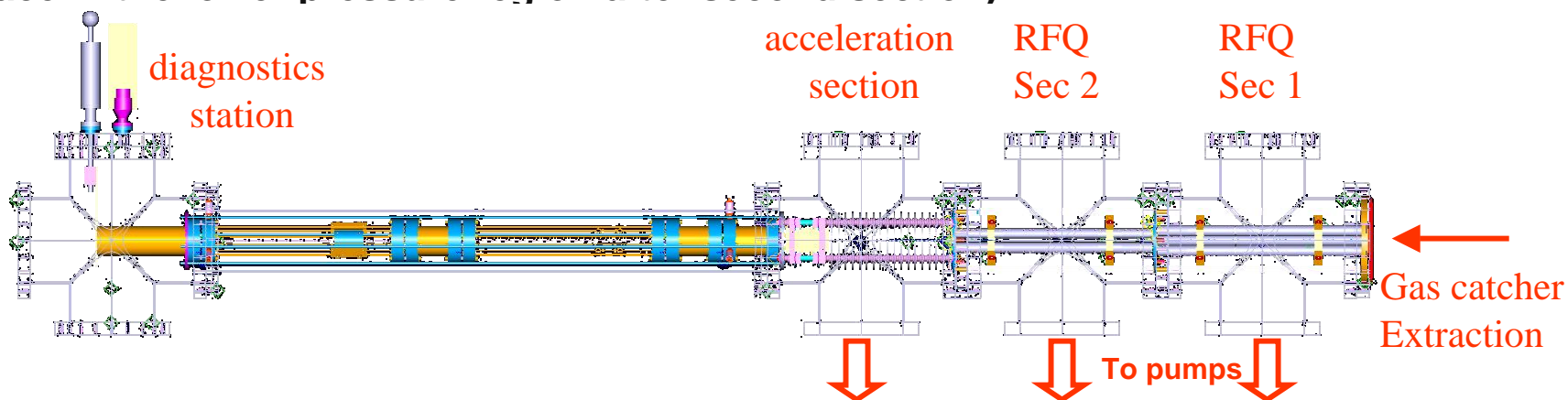
Extraction in the presence of large gas flow

Transport ions to lower pressure region via RF structures that guide ions while letting the gas escape and be pumped away.

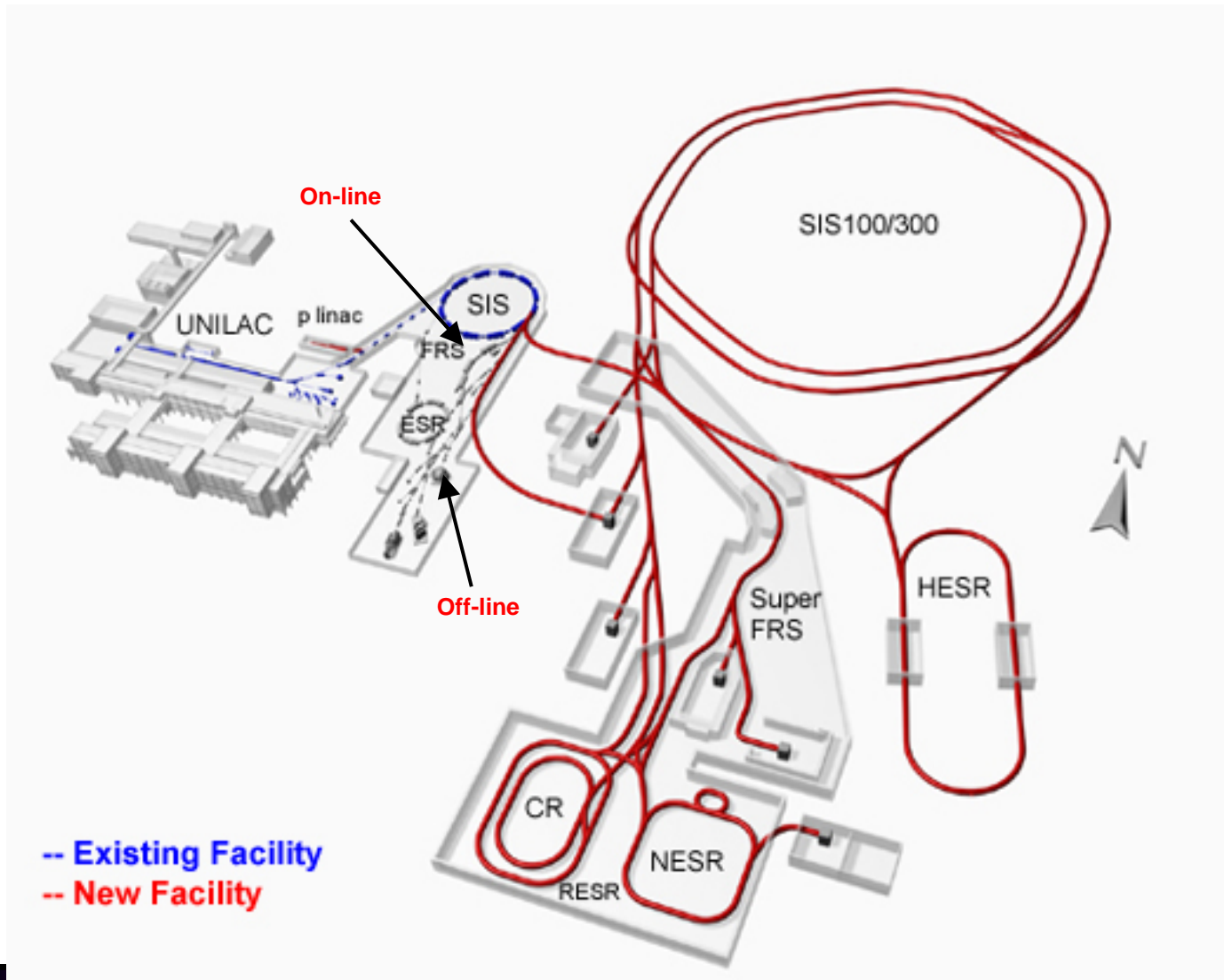
Section of segmented RFQ for ion transport and differential pumping



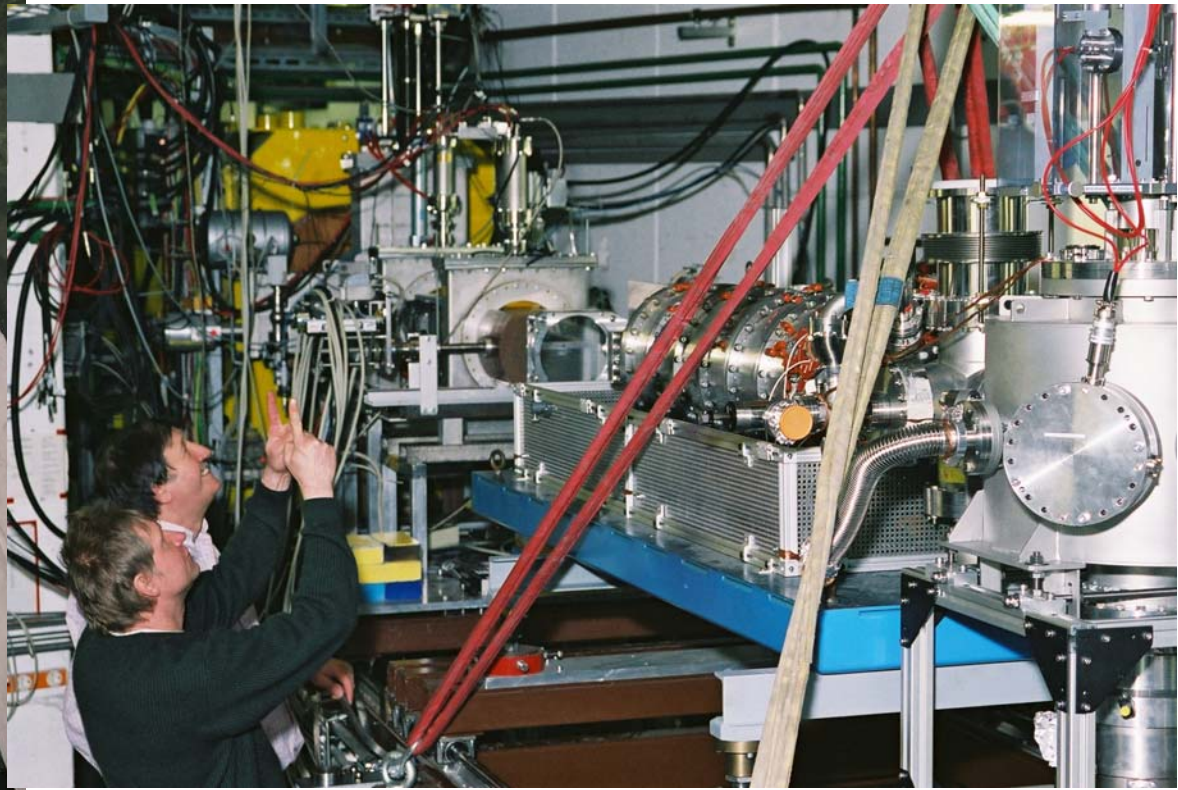
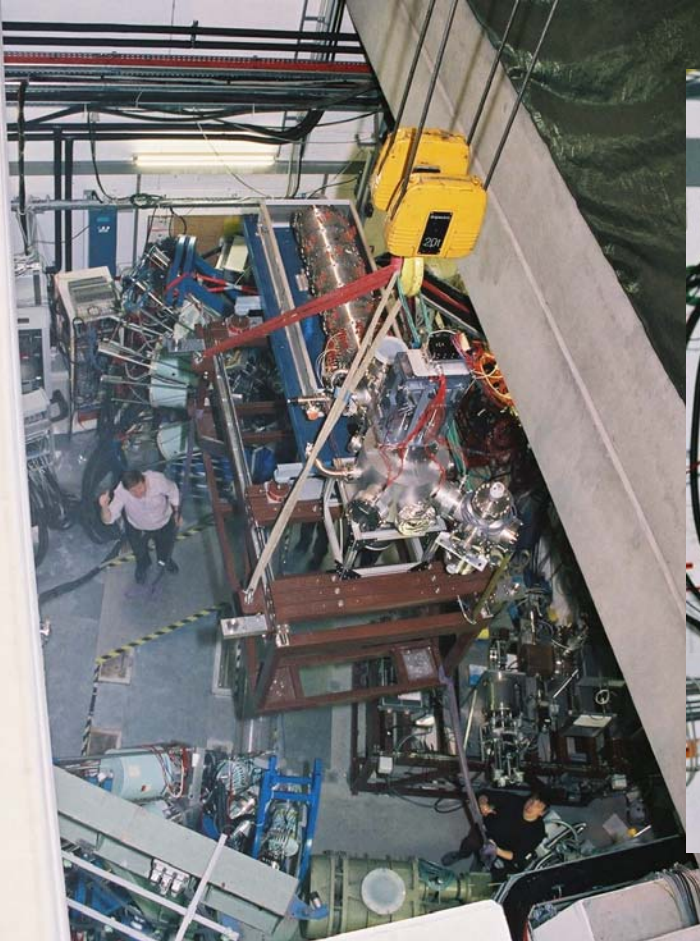
In DC mode, a limiting emittance (corresponding to roughly the gas temperature) is obtained after two such sections separated by small apertures (acceleration takes place in the lower pressure region after second section).



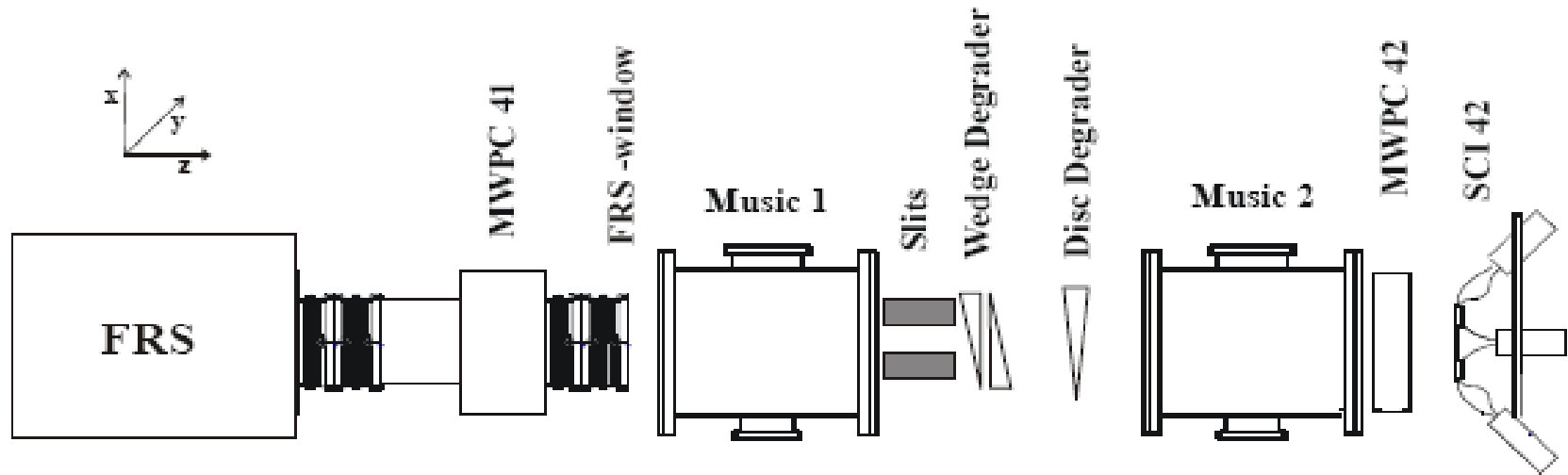
GSI Floor Plan



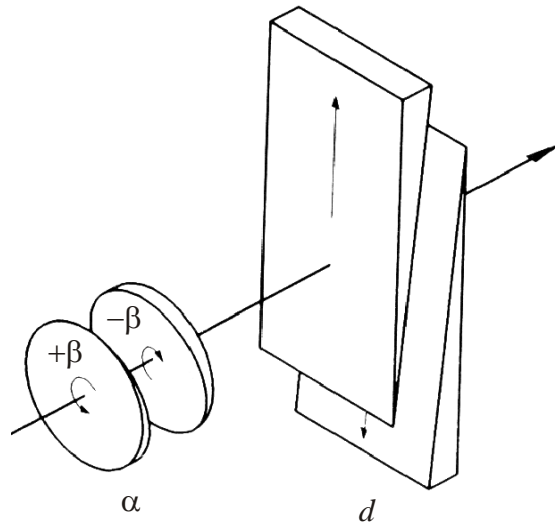
Installation of the RIA prototype gas catcher at the focal plane of the FRS



Detector system at F4 for particle identification



Precision Degradation System



Velocity distribution of the beam limited by

- * ion-optical resolution of the buncher
- * energy-loss straggling in degrader

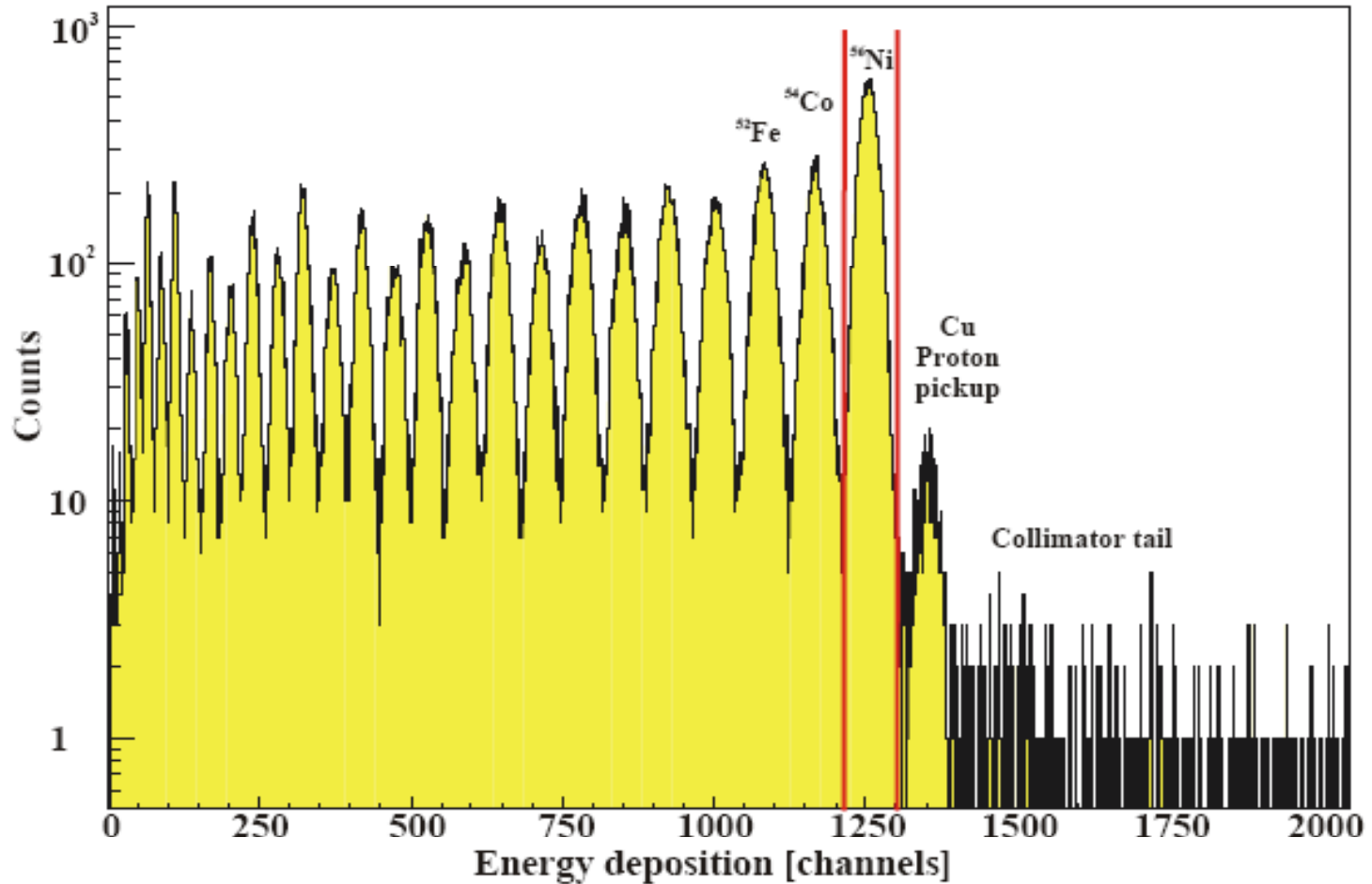
Practical limitation: inhomogeneities

Precision degrader system

Material:	Suprasil 2 (SiO ₂)
Surface roughness:	less than 10 nm
Maximum shape deviation:	less than 1 μm
Material homogeneity:	better than 10 ⁻⁴
Areal weight homogeneity:	better than 0.2 mg/cm ²
Minimum thickness steps:	180 μg/cm ²



MUSIC Chamber Spectrum



MUSIC chambers Identify each individual ions

Radioactive ions extracted from the RIA prototype gas catcher at GSI (S258 experiment)

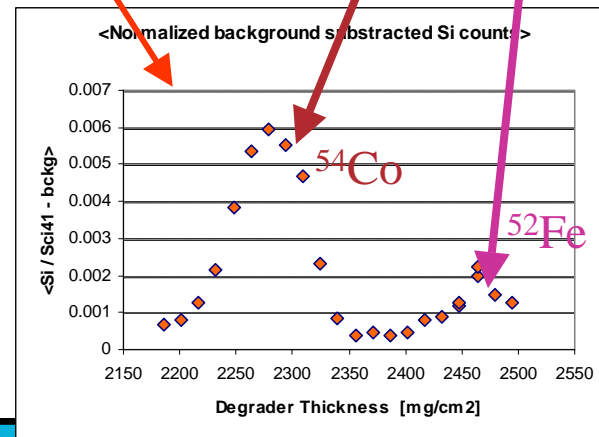
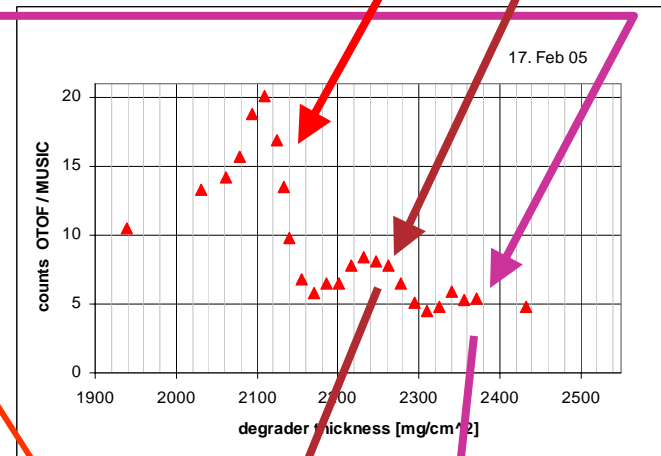
Energy loss in gas catcher by radioactive beam from FRS

- Bragg peak from ^{56}Ni beam
- Bragg peak from ^{54}Co beam
- Bragg peak from ^{52}Fe beam

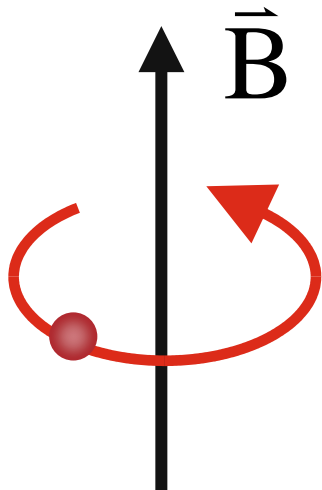
~ 50 % of radioactive ions stopped in the gas catcher were extracted as a radioactive ion beam!

No saturation up to the maximum radioactive beam intensity (~ 10^6 ions per spill) that the FRS could deliver!

By tuning the degrader thickness, one can scan over the Bragg peak in the gas catcher, at the end of which the radioactive ions are stopped in the gas and extracted as a cooled low-energy radioactive ion beam



2d-confinement: Charged particle in a magnetic field

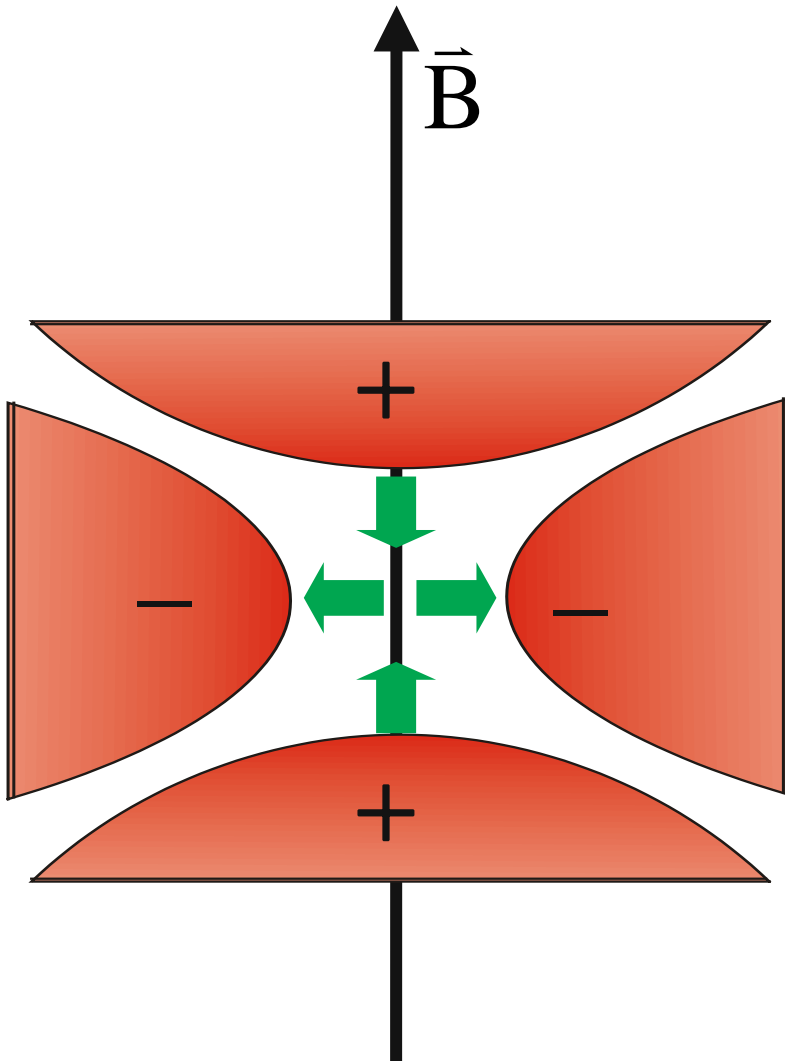


- **Constant axial magnetic field**
- **particle orbits in horizontal plane**

$$\omega_c = \frac{qB}{m}$$

- **free to escape axially**

3d-confinement: The Penning trap



- Add an axial harmonic electric field to confine particles

$$\varphi(\rho, z) = \frac{V}{4d^2} (2z^2 - \rho^2)$$

confining in z

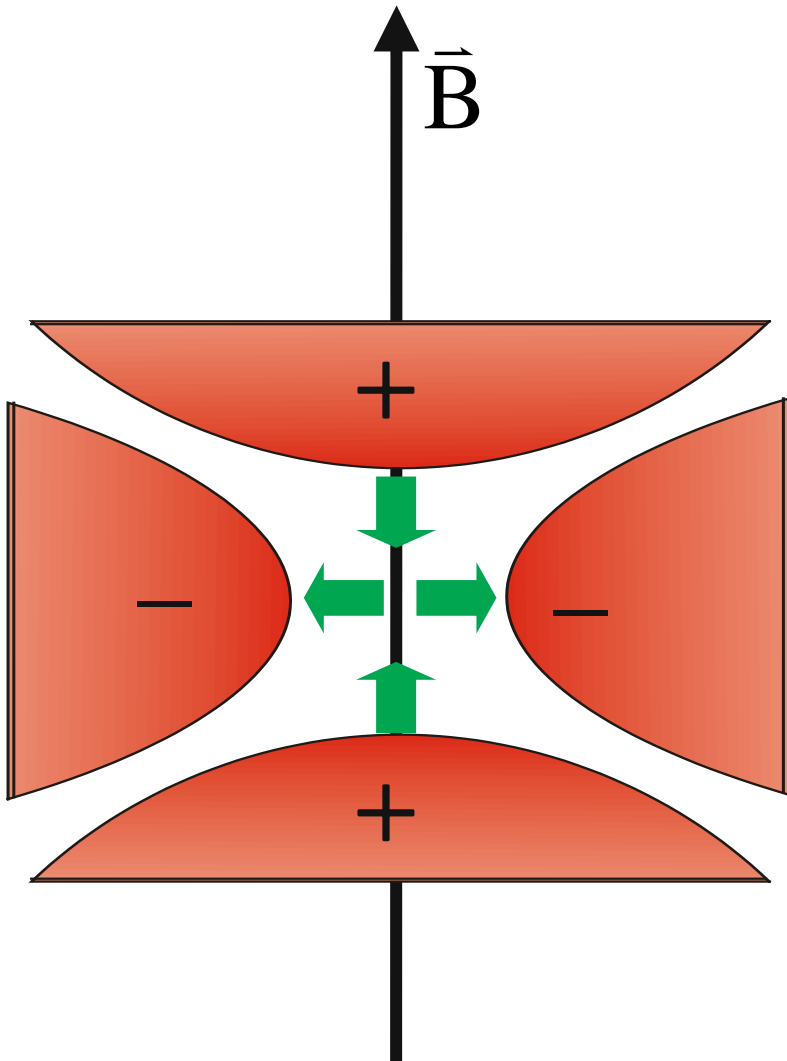
obeys Laplace $\nabla^2\varphi = 0$

- axial oscillations:

$$\omega_z = \sqrt{\frac{eV}{md^2}}$$

- axially confining potential comes with radially repulsive one

3d-confinement: The Penning trap



•radial motion now split into two eigenmodes

$$\frac{mv^2}{R} = qvB - qE_\rho = qvB - \frac{2VRq}{4d^2}$$

$$\omega^2 = \omega_c \omega - \frac{\omega_z^2}{2}$$

$$\omega_{\pm} = \frac{\omega_c}{2} \pm \sqrt{\frac{\omega_c^2}{4} - \frac{\omega_z^2}{2}}$$

confinement limit

•Radial motion split into two components by electric field:

→ ω_+ : reduced cyclotron frequency

→ ω_- : magnetron frequency

Precision measurements in a Penning trap

However:

$$\omega_c = \omega_+ + \omega_-$$
$$\omega_c^2 = \omega_+^2 + \omega_-^2 + \omega_z^2$$

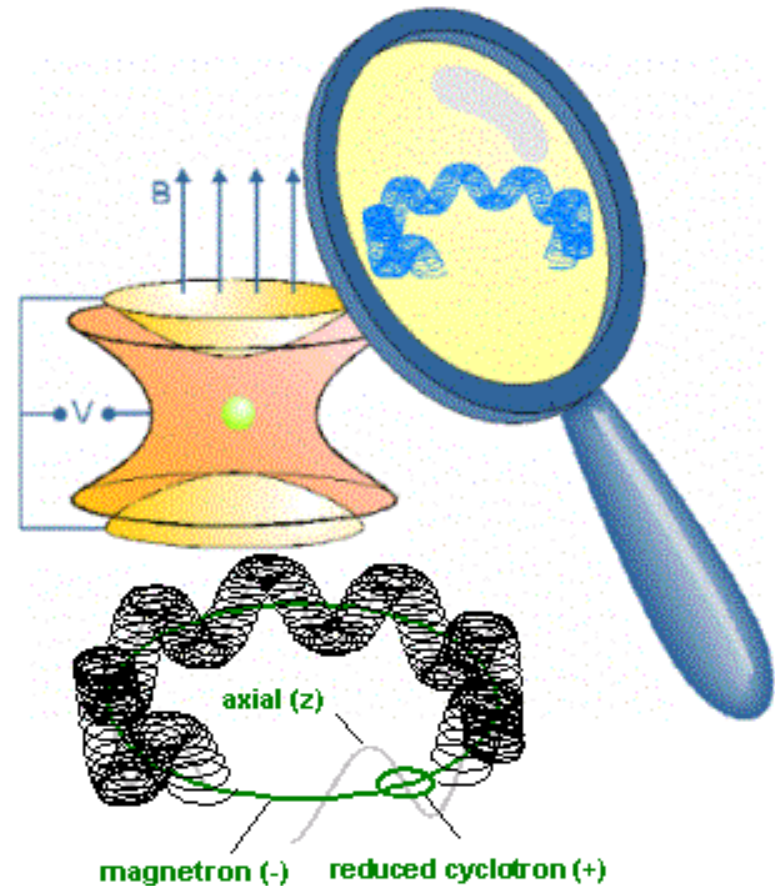
Recall:

$$\omega_c = \frac{qB}{\gamma m}$$

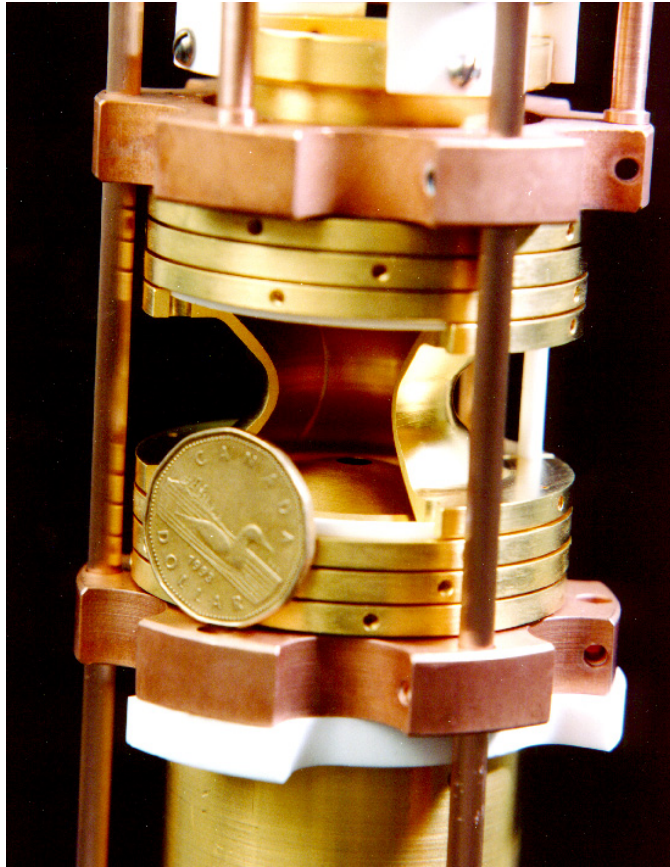
ω_c depends only on:

- the mass
- the magnetic field
- not on the electric fields or the energy as long as γ is small

Can use ω_c to make accurate and precise mass measurements



CPT mass spectrometer



**Ion trap system located
on-line at the
ATLAS superconducting linac**

**High-accuracy mass measurements on
short-lived isotopes via:**

$$\omega_c = qB/m$$

Concentrate presently along N=Z line

- Electroweak Interaction**
- Nuclear Astrophysics**

Accuracy : 10^{-6} - 10^{-9}

Half-life limit : ~ 50 ms

Resolution (Fourier limited) : $\sim 10^{-6}$

Superallowed Beta Decay

- *Precision tests of CVC*
- *Determination of weak vector coupling constant*
- *Unitary tests of the CKM matrix*

- For superallowed transitions between $0^+ T=1$ states

$$ft = ft (1 + \delta_R) (1 - \delta_C) = \frac{K}{2 G_V^2 (1 + \Delta_R)}$$

from experiment; from calculations of radiative and charge-dependent effects

- Test need for physics beyond the standard model

G_V together with G_μ yield the V_{ud} quark mixing element of the CKM matrix

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

weak eigenstates
rotation matrix
mass eigenstates

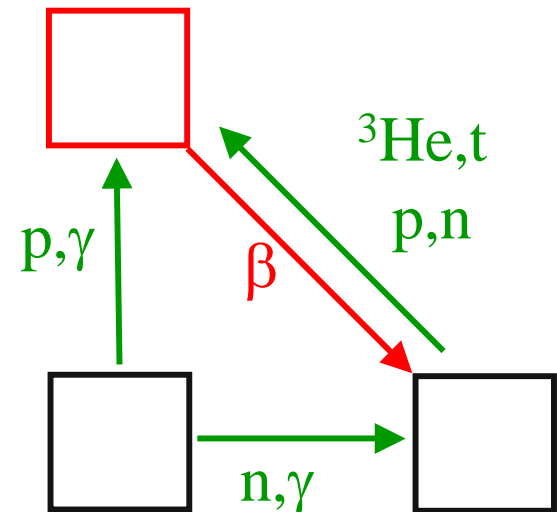
- If matrix is not unitary then we need new physics
Additional Z bosons, Right-handed currents, SUSY...

Big effect if R-parity violating ... can be more than 0.0020

At loop level if R-parity conserving ~ 0.0007

Precision frontier --- superallowed Q-value measurements

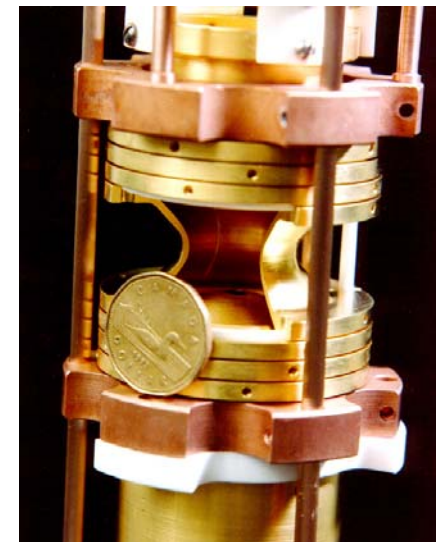
- required precision (0.1 – 1 keV) cannot be reached by β endpoint measurement
- Standard approach: reaction threshold (neutron yield vs energy for p,n reaction) or gamma-ray energy ... **not applicable to new cases**
- new approach required



- Penning trap mass measurements on short-lived isotopes

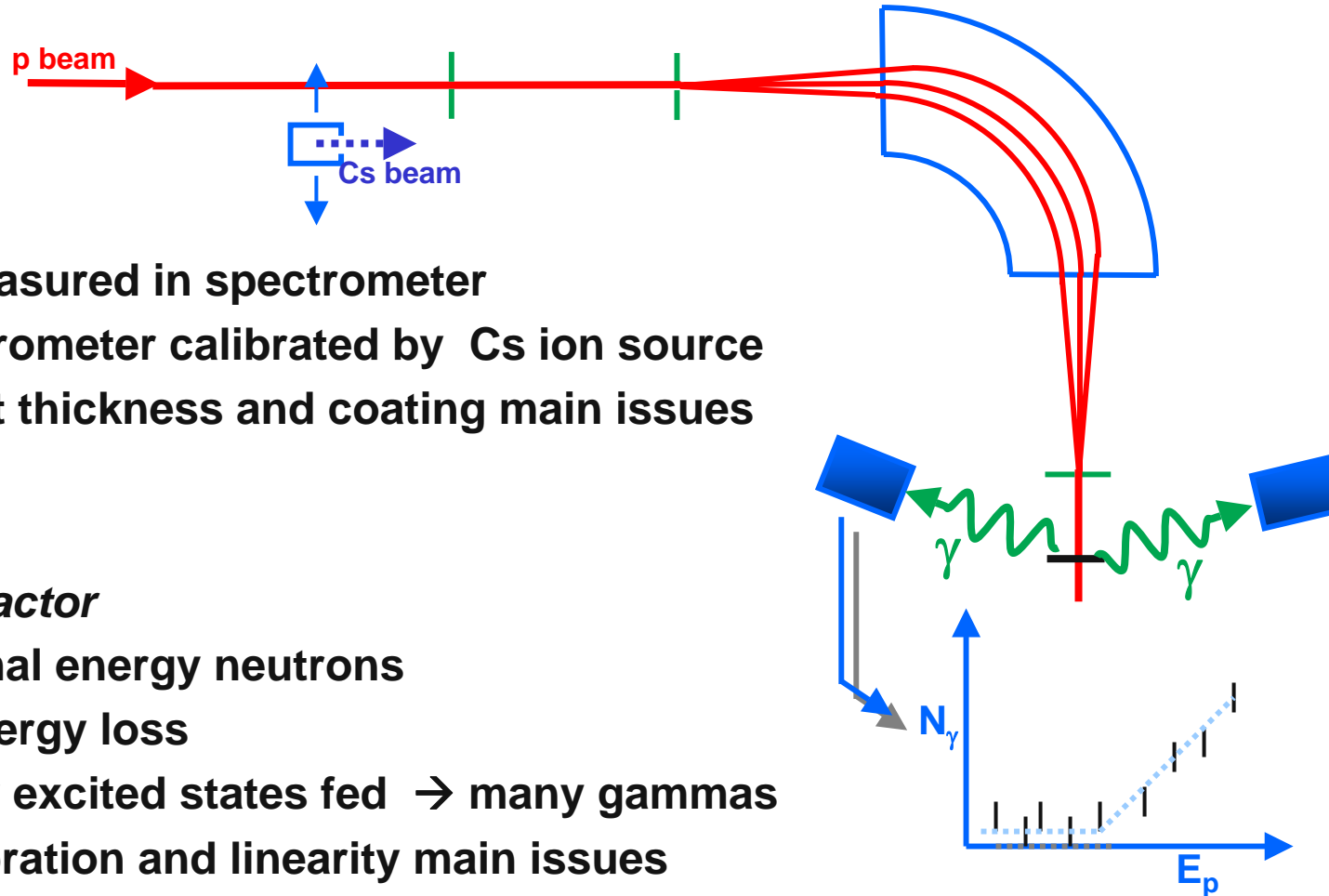
- Accuracy 10^{-7} - 10^{-9}
- Lifetime limit ~ 50 ms
- Resolution 10^6

$$\omega_c = qB/m$$



Reaction threshold measurement

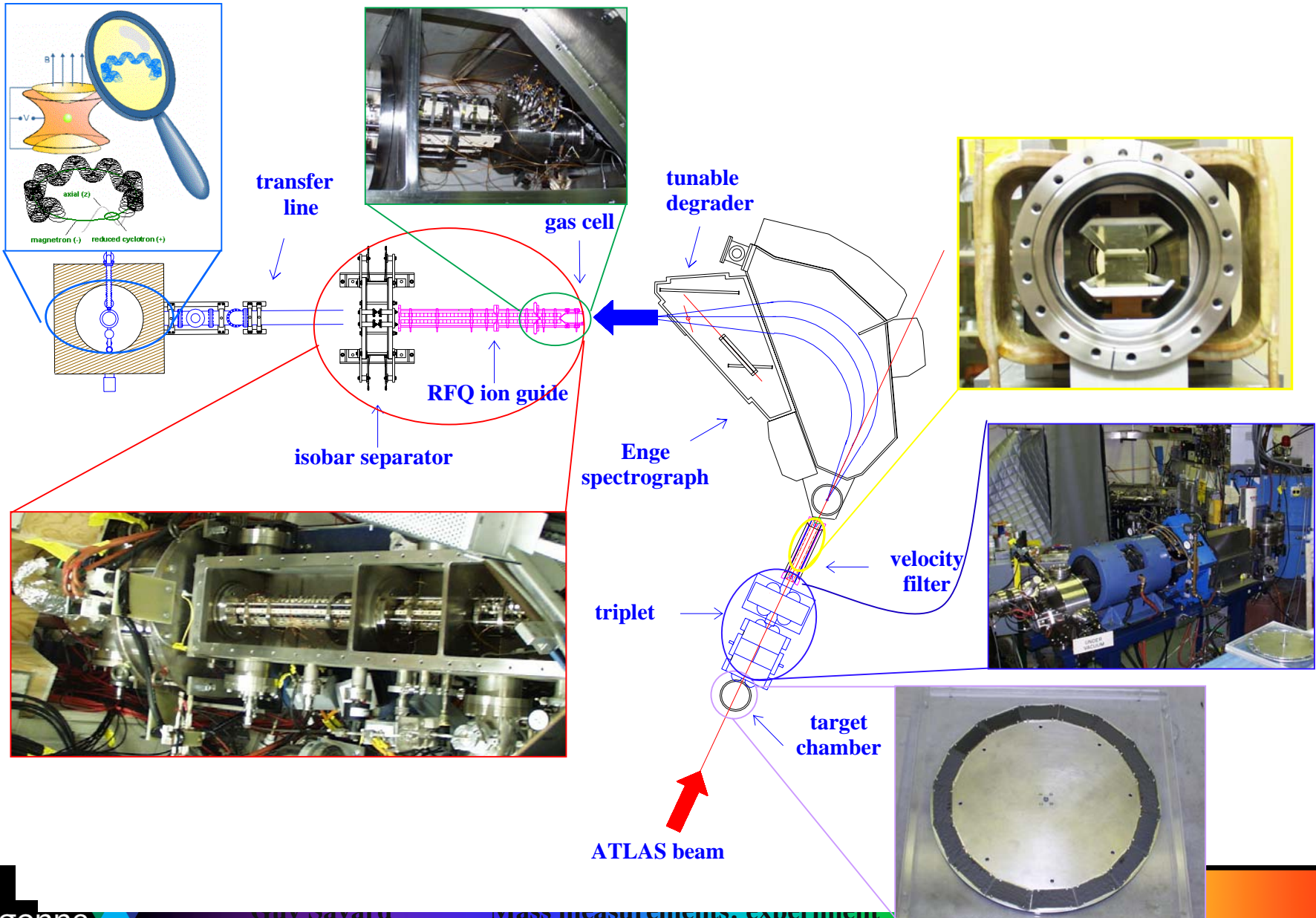
- Simple reaction to remove uncertainty from beam excitation
 - (p,n) or (p,γ) with *independently calibrated beam energy*



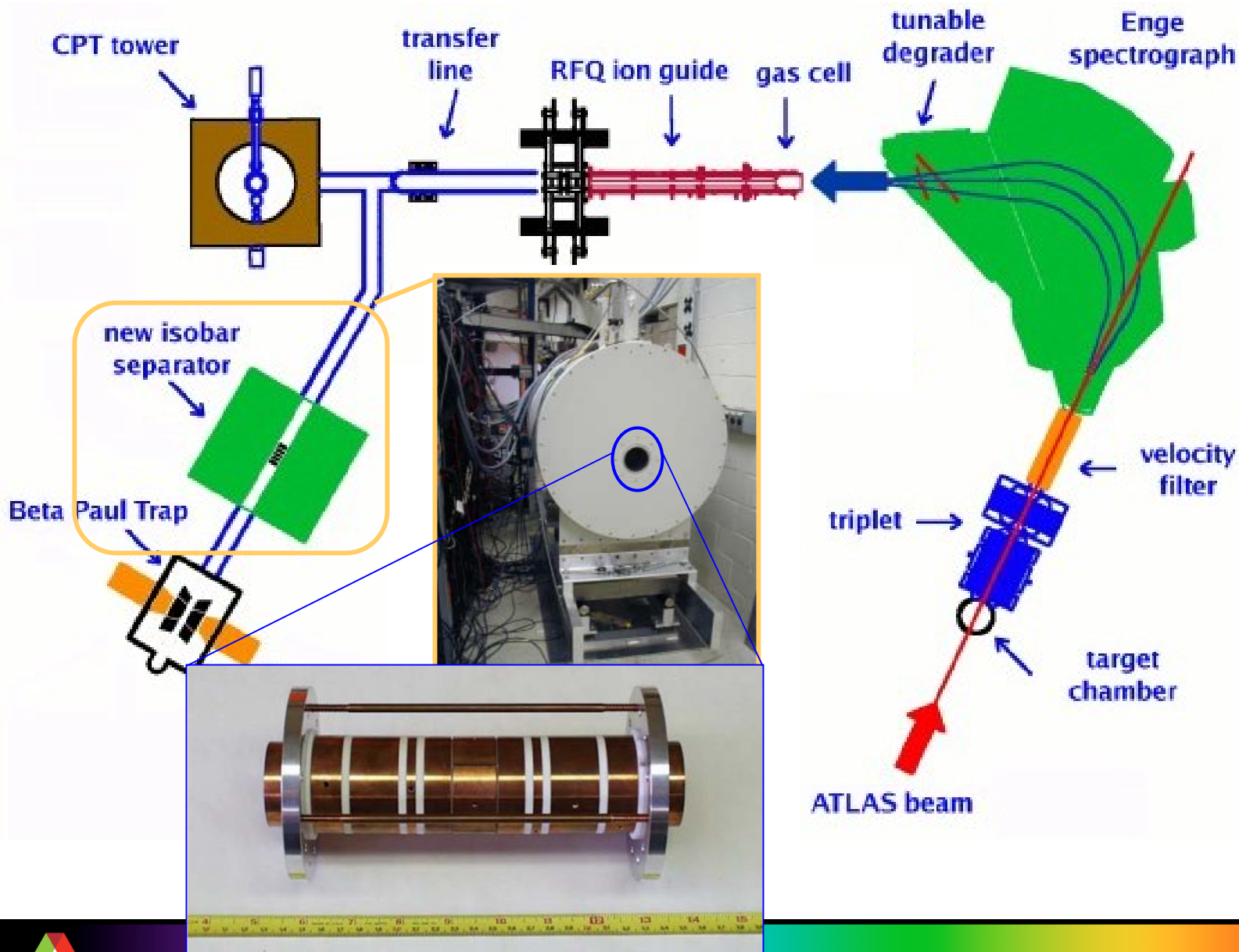
- E_p measured in spectrometer
- Spectrometer calibrated by Cs ion source
- Target thickness and coating main issues

- (n,γ) at reactor
 - Thermal energy neutrons
 - No energy loss
 - highly excited states fed \rightarrow many gammas
 - γ calibration and linearity main issues

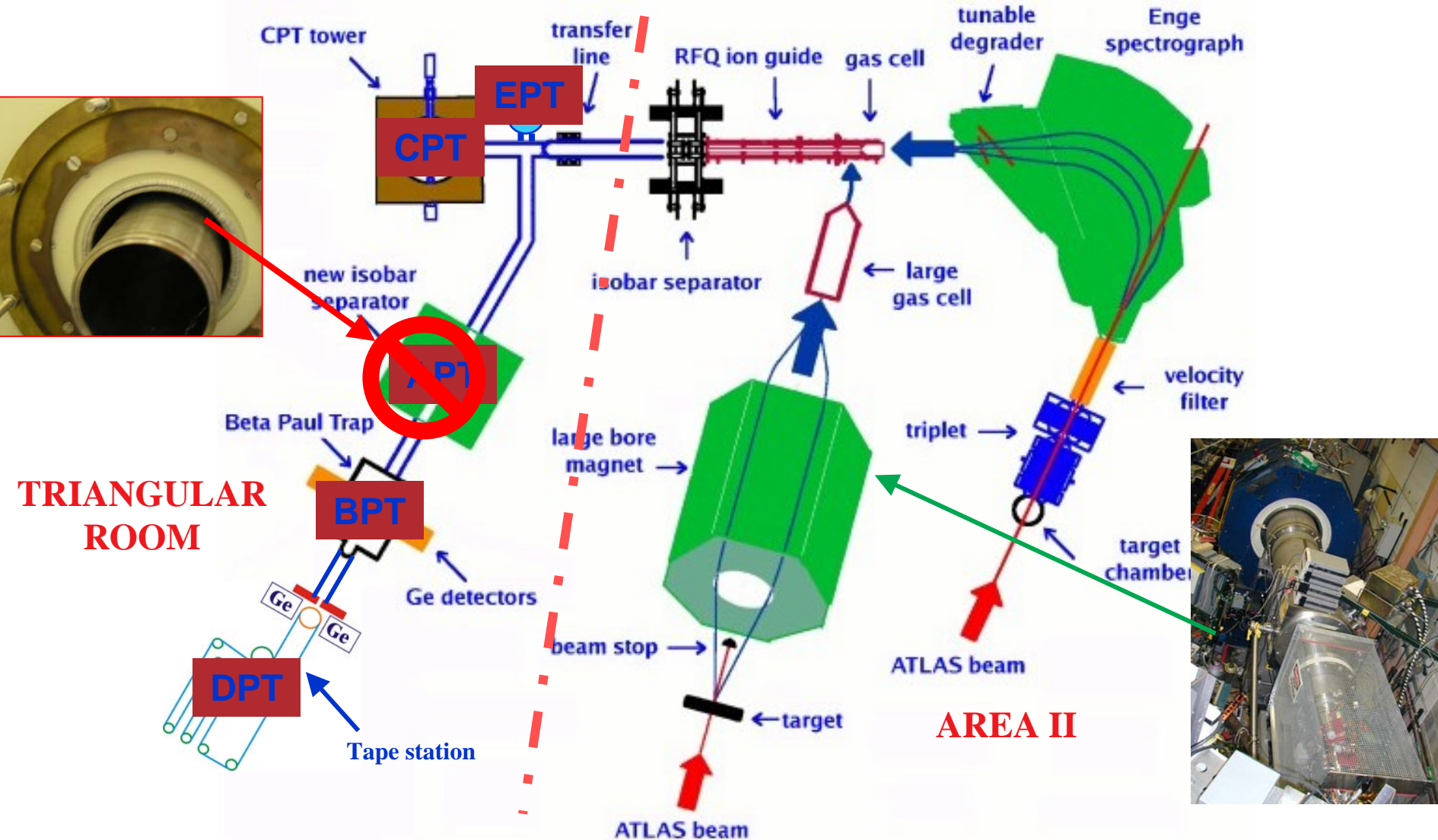
Overview of the CPT on-line mass spectrometer



Isobar separator for beam purification

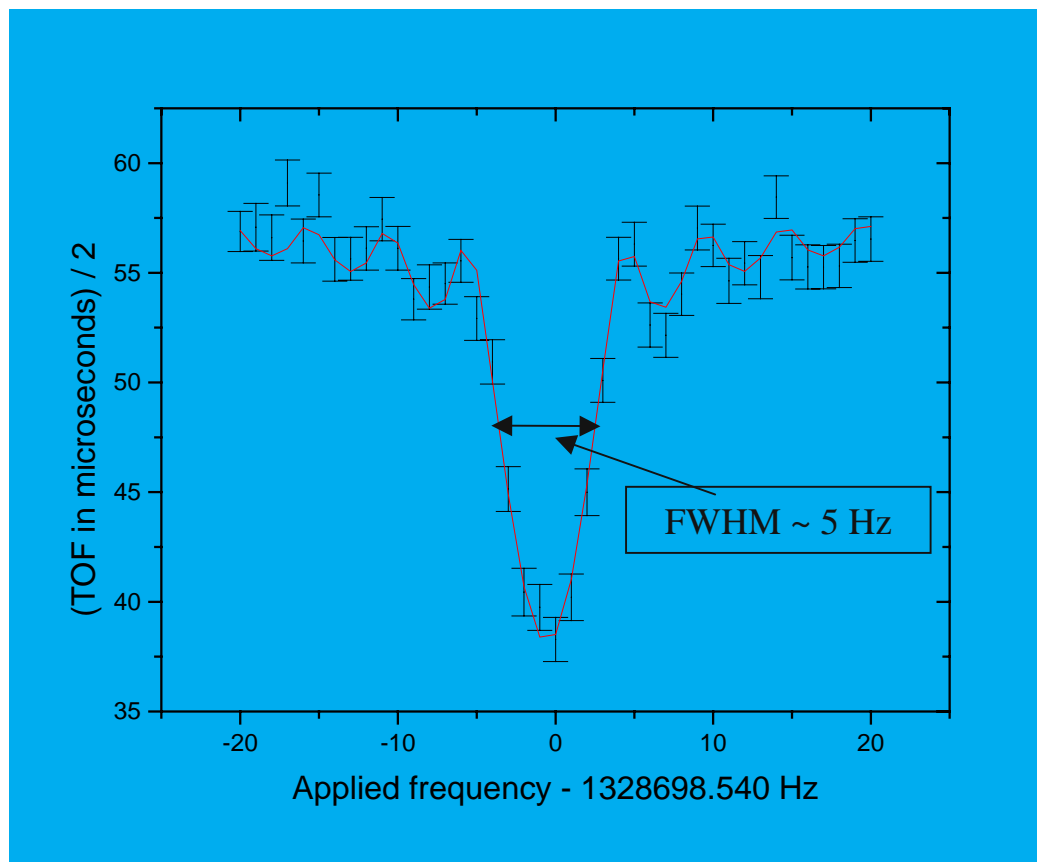


Fully evolved system giving access to all isotopes available at ATLAS ... end of 2006



Sample TOF spectra

Calibration: C_5H_8



$$\omega_c = \frac{qB_c}{m_c}$$

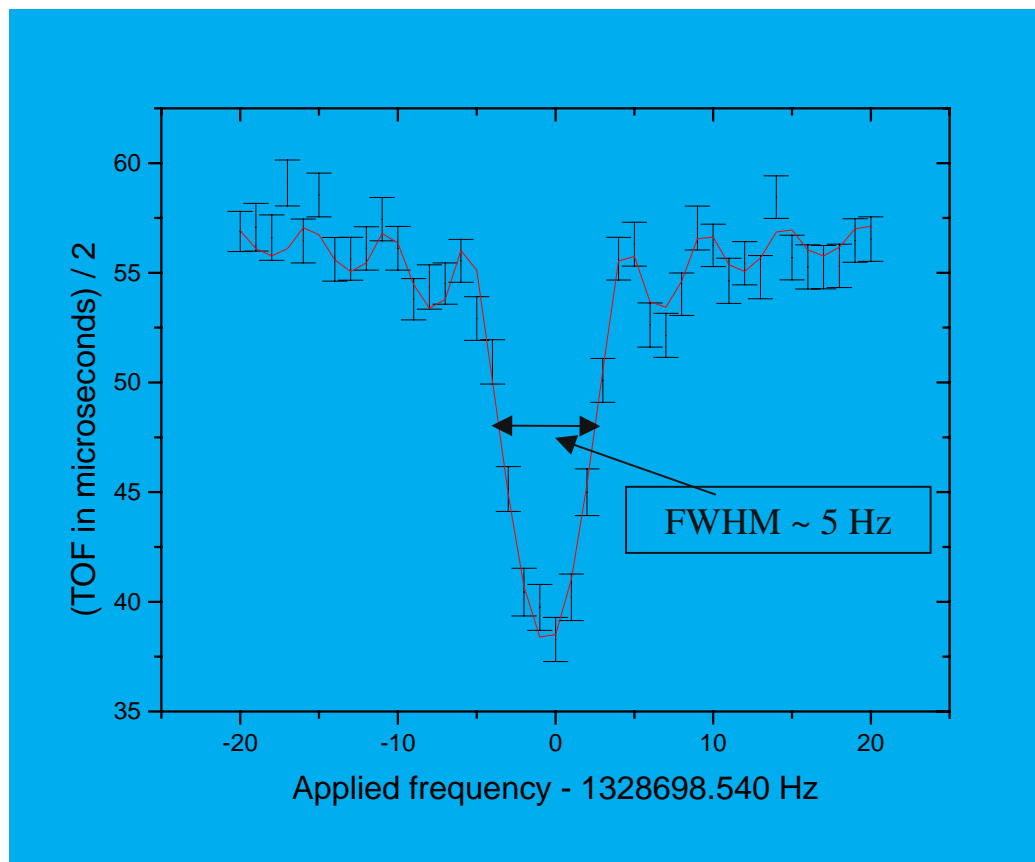
Unknown:

$$\omega_\gamma = \frac{qB_c}{m_\gamma}$$

$$\frac{\text{Unknown}}{\text{Calibration}} \Rightarrow m_\gamma = \frac{m_c \omega_c}{\omega_\gamma}$$

Sample TOF spectra

Calibration: C_5H_8



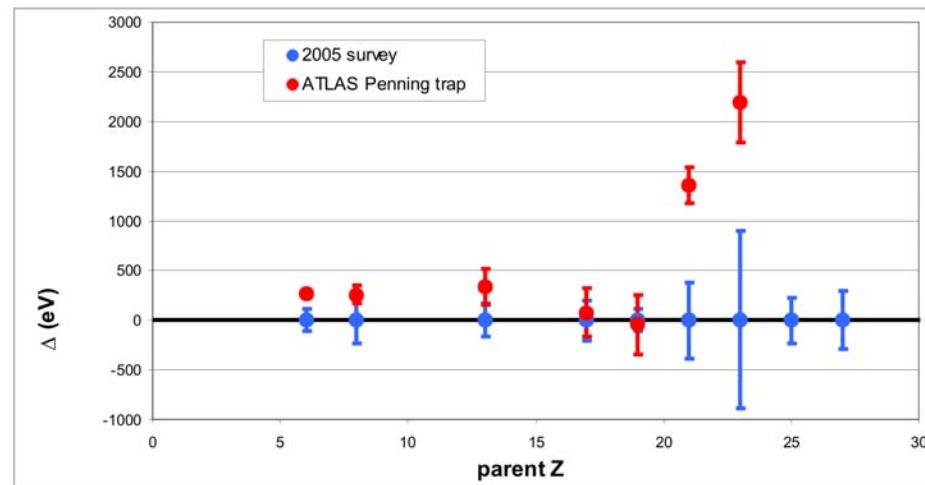
$$\text{Resolution} = \frac{\Delta\omega_{FWHM}}{\omega}$$

$$\Delta\omega_{FWHM} \sim \frac{0.9}{T_{RF}}$$

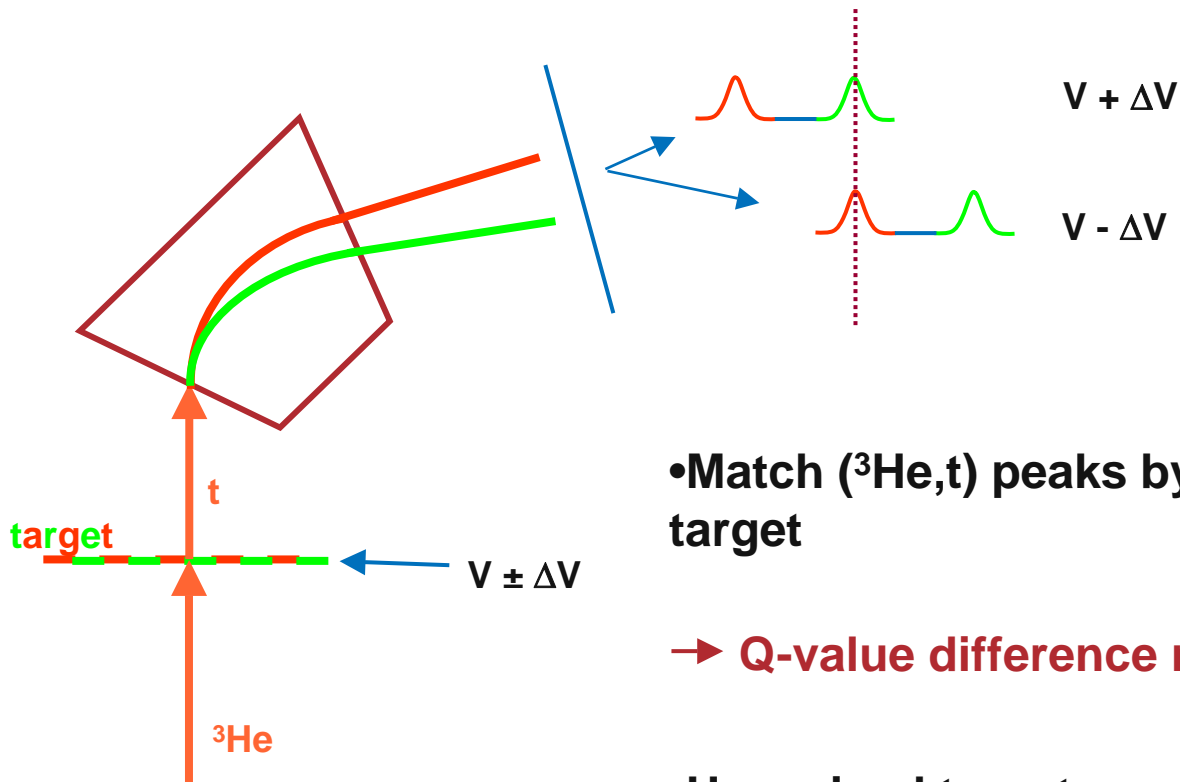
$$\text{Precision, } \frac{m}{\Delta m} \propto \frac{T_{RF} q B \sqrt{N}}{m}$$

Completing the Penning trap measurements of the nine highest precision superallowed emitters

- 7 of the 9 cases have now been measured at the CPT
 - ^{42}Sc was found, like ^{46}V , to be significantly higher than expected
 - Other cases are generally higher than last compilation but by smaller amounts
- Work at the accuracy frontier
 - extensive systematics check
 - absolute calibration during the experiment
 - highest accuracy ever achieved for online trap measurements
 - $\Delta Q(^{14}\text{O}) \sim 90 \text{ eV}$
 - $\Delta Q(^{10}\text{C}) \sim 40 \text{ eV}$
 - can now test atomic effects



Chalk River Q-value difference measurements



- Match ($^3\text{He}, t$) peaks by changing voltage on target

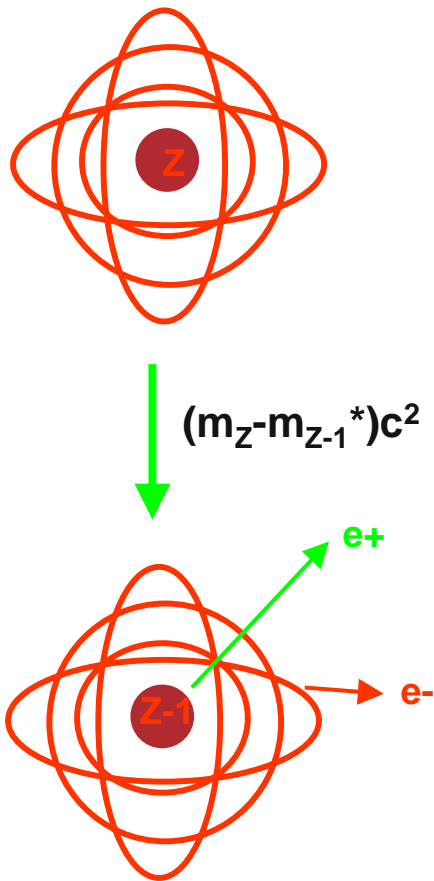
→ Q-value difference measured with a voltmeter ←

- Use mixed targets ... essentially all sources of systematics drop out

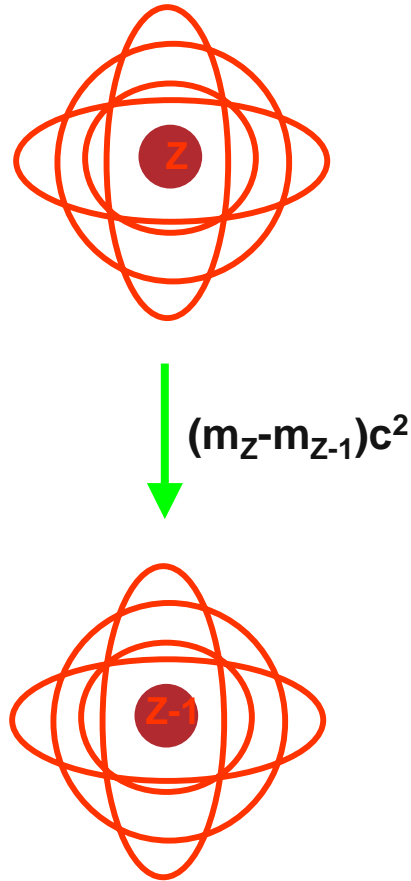
- Most robust of the previously existing data

Atomic structure effects ... are we measuring the same quantity?

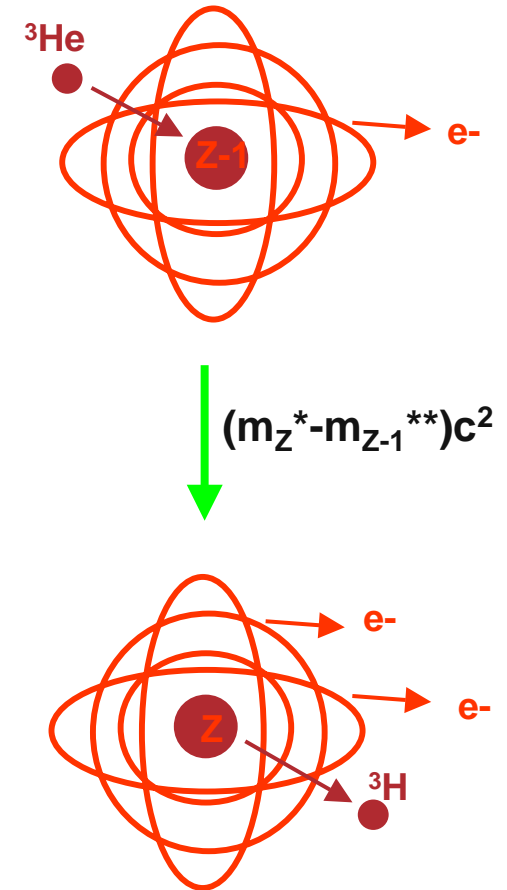
Beta decay



Mass measurements



reaction Q value



Are we consistent with any of the reaction results?

- Our new results disagree with previous reaction values by 1σ for ^{14}O , about 7σ for ^{42}Sc ... and about 4σ for our very recent $^{26\text{m}}\text{Al}$ result

- From the Chalk River Q value differences

$$Q(^{14}\text{O}) - Q(^{26\text{m}}\text{Al}) = 1401.68(13) \text{ keV}$$

$$Q(^{26\text{m}}\text{Al}) - Q(^{42}\text{Sc}) = 2193.5(2) \text{ keV}$$

- Our new value for ^{42}Sc shifts the Q value up by about 7 sigma, ^{14}O is only shifted slightly up. But the differences agrees with the difference measurements

- Chalk River Q value difference $\rightarrow Q(^{42}\text{Sc}) - Q(^{14}\text{O}) = 3595.18(24) \text{ keV}$

- CPT results (preliminary) $\rightarrow Q(^{42}\text{Sc}) - Q(^{14}\text{O}) = 3595.52(23) \text{ keV}$

- Can also predict the Q value of $^{26\text{m}}\text{Al}$ from the Q value differences and the CPT Q values for ^{14}O and ^{42}Sc ... again we find excellent agreement with the CPT preliminary value for $Q(^{26\text{m}}\text{Al})$.

It does not appear that the reaction approach is flawed ... when done in the best conditions it agrees with the trap measurements.

Status - Outlook

- **Enormous evolution in mass measurements techniques and hardware since the inception of the field roughly 100 years ago.**
- **Tools to make precision mass measurements to the accuracy required for astrophysics, nuclear structure and fundamental interaction studies have been developed and are operational.**
- **Main limitation at this point is access to the most exotic nuclei, but there is hope on the horizon with new large scale RIB facilities in preparation.**