



Mass measurements for nuclear astrophysics

Lecture 1: introductory physics and methods

David Lunney

*Centre de Spectrométrie Nucléaire et de Spectrométrie de Masse
(CSNSM – IN2P3 / CNRS) Université de Paris Sud, Orsay*



**Joint Institute for Nuclear Astrophysics
Special School on Nuclear Mass Models
Argonne National Laboratory - May 8-16, 2007**

I. General concepts – binding energy; the mass unit; resolution; precision; accuracy

II. Physics motivation

- a nuclear structure – shells, deformation, pairing, halos (the mass scale)
- b weak interaction – superallowed beta decay and the CKM matrix
- c astrophysics – stellar nucleosynthesis

III. Production of radionuclides – methods of FIFS (fragmentation) et ISOL;
(ion manipulation using traps and gas cells)

IV. Mass measurement techniques

- i. indirect methods – reactions et decays
- ii. direct methods – time of flight (SPEG et CSS2 au GANIL;
ESR isochronous mode at GSI); revolution (cyclotron) frequency
(ESR Schottky mode; ISOLTRAP and MISTRAL at ISOLDE)

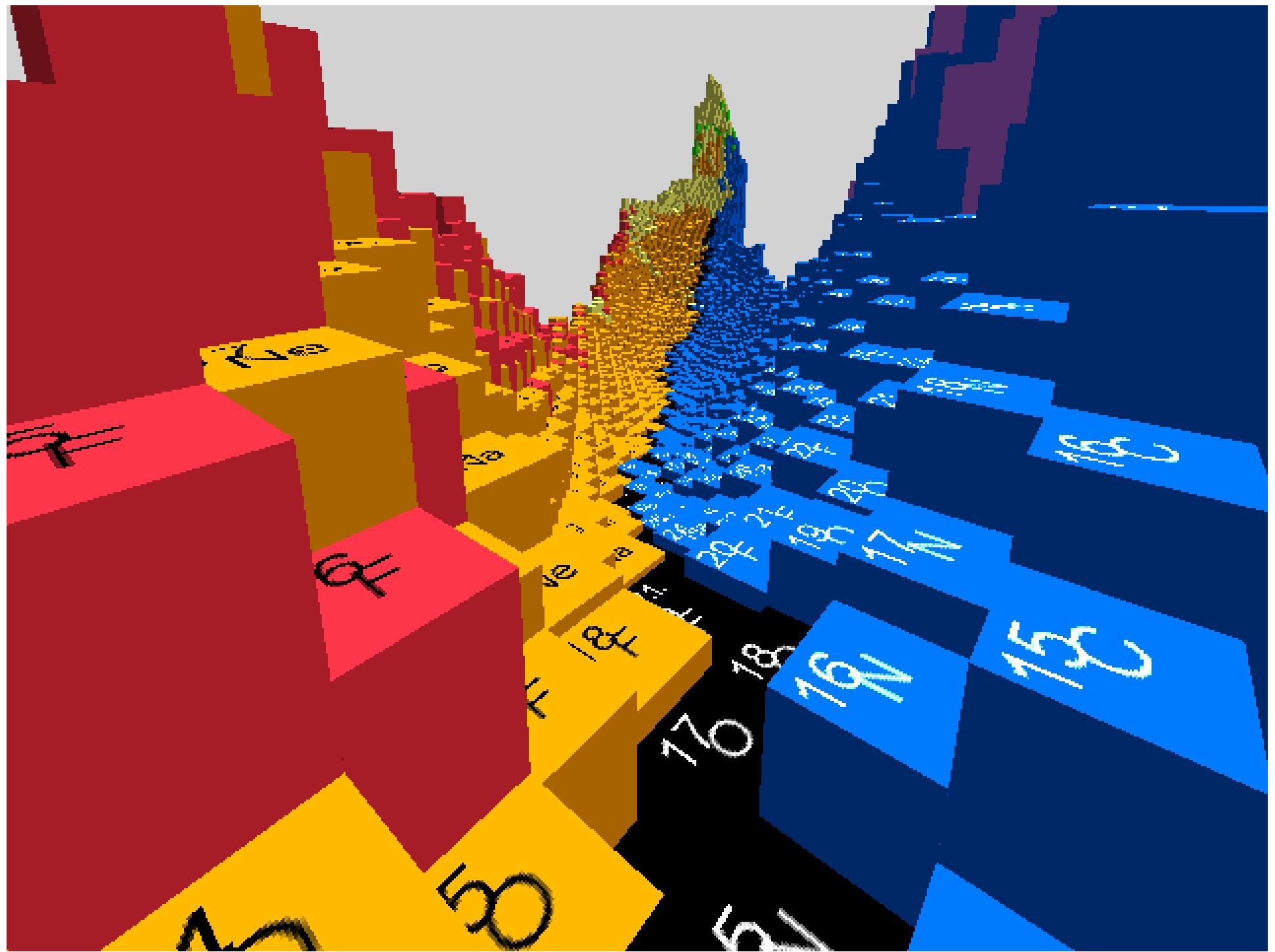
V. Comparisons of the different methods

VI. The atomic mass evaluation (demonstration of the program *NUCLEUS*)

VII. Mass models and comparisons; chaos on the mass surface?

VIII. A look into the future

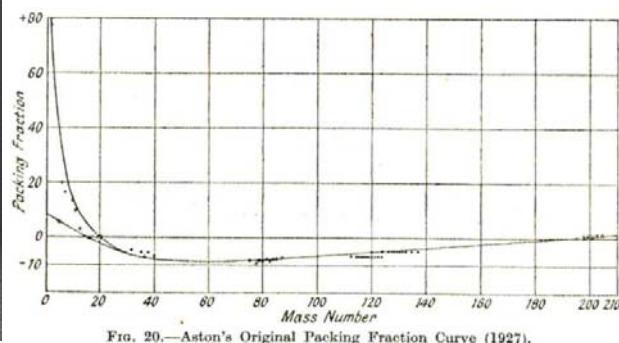
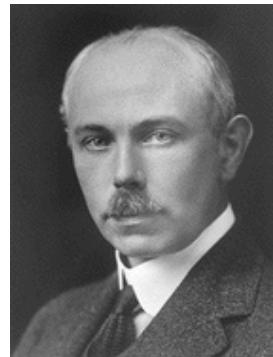
IX. Conclusions



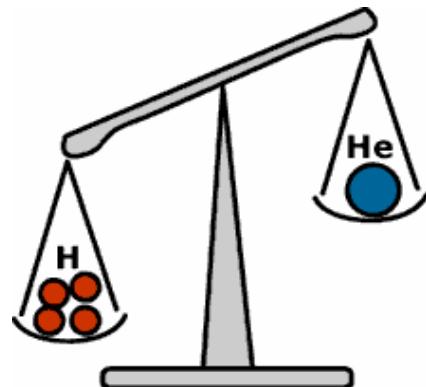
Some introductory remarks on history

High resolution mass spectrographs

F.W.Aston (~1920's): 212 isotopes discovered
Packing fraction



A. Eddington (~1920)
Stellar combustion

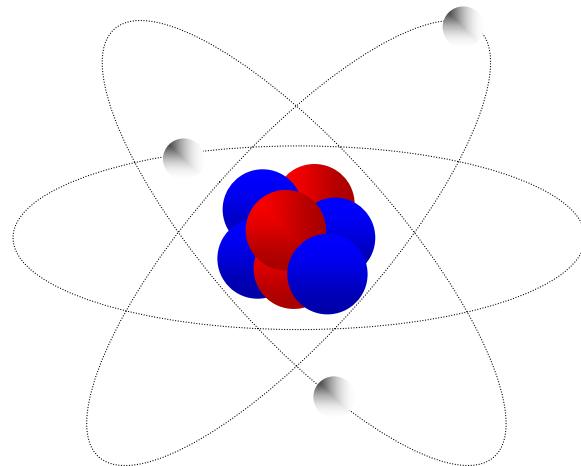


$$E = mc^2$$

How the sun shines,"
J. Bahcall
<http://nobelprize.org/physics/>



the atomic mass



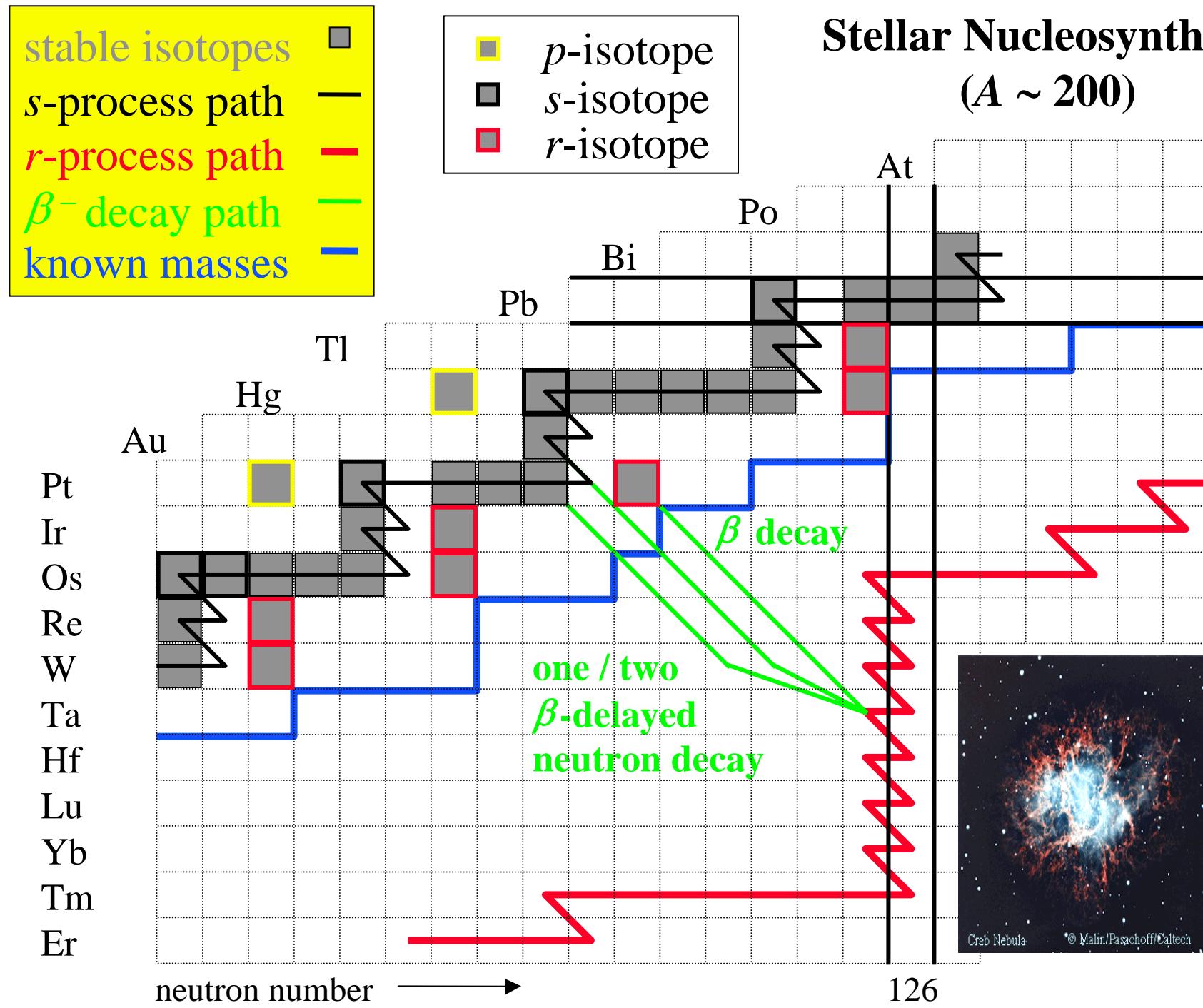
$$\begin{aligned} & Z \cdot m_p + N \cdot m_n \\ & (+ Z \cdot m_e) \\ & - \text{BINDING} \\ & \text{ENERGY} \end{aligned}$$

nuclear structure
(shells, shapes, halos)

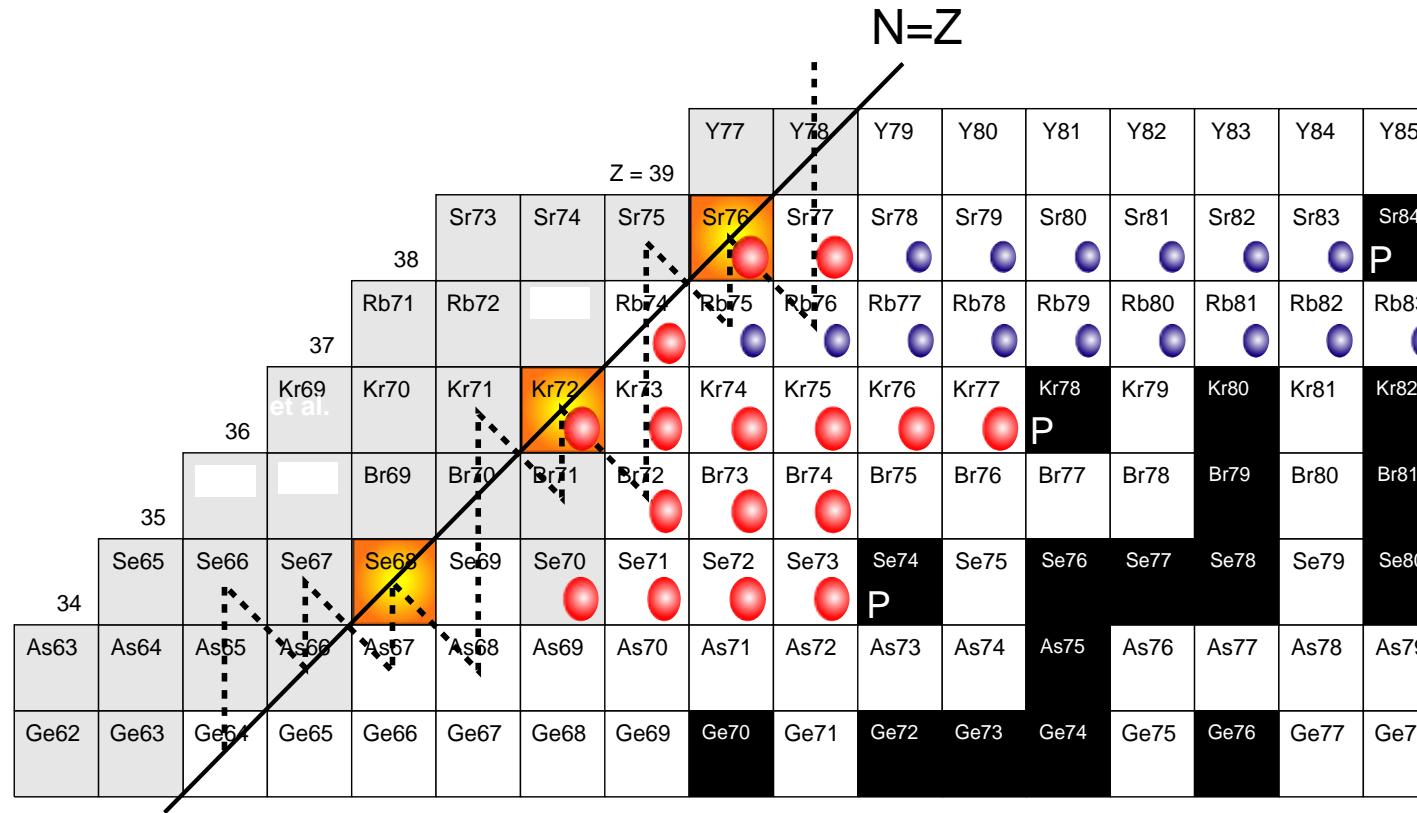
nuclear astrophysics
(decay mode, reaction)

Stellar Nucleosynthesis

($A \sim 200$)



rapid proton-capture (rp) process



----- possible rp - process main path

(H. Schatz *et al.* Phys. Rep. 294 (1998) 167)



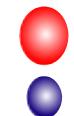
possible waiting points



mass excess not yet measured

(AME95)

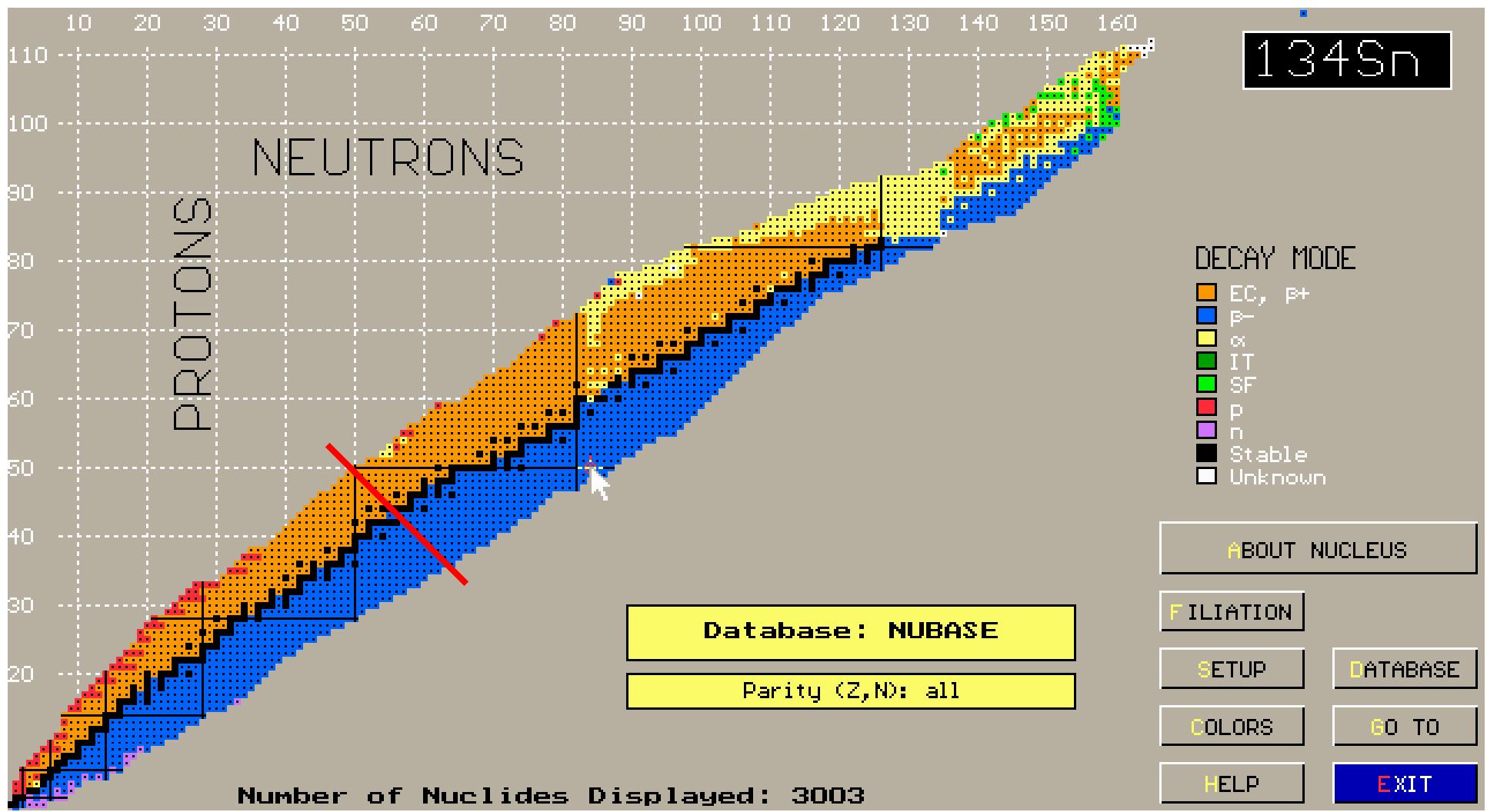
ISOLTRAP measurements

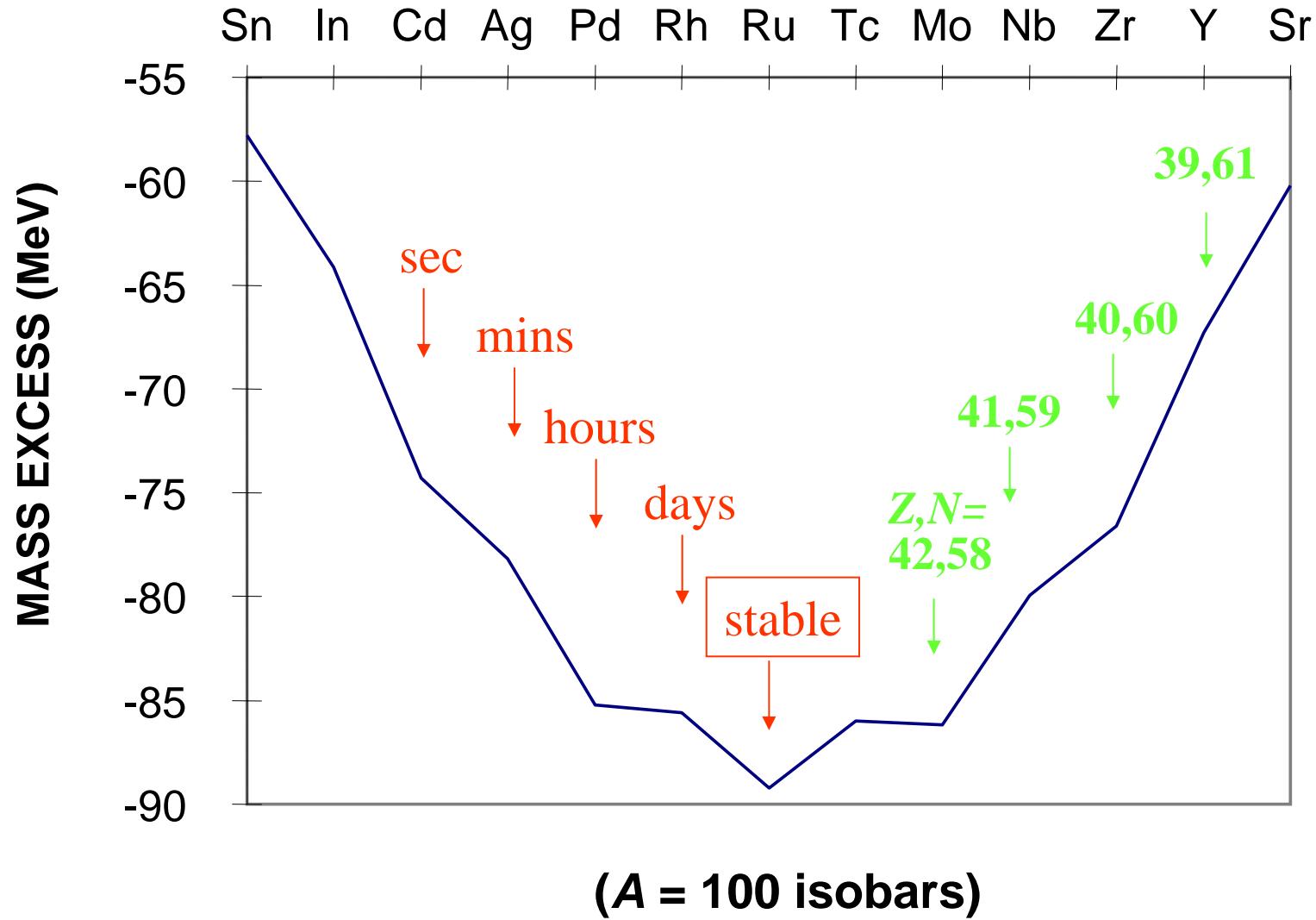


2000 - 2002

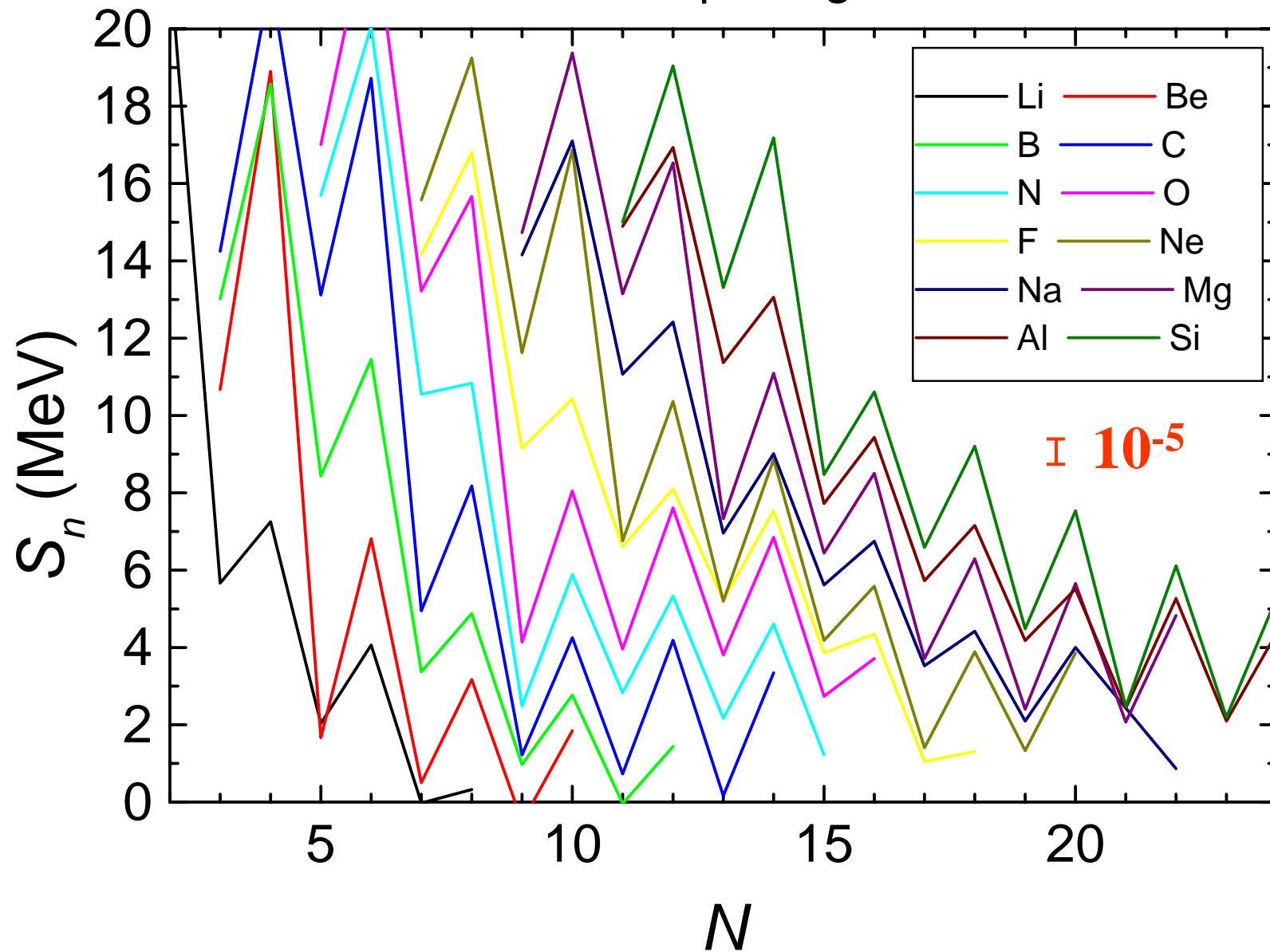


before 2000

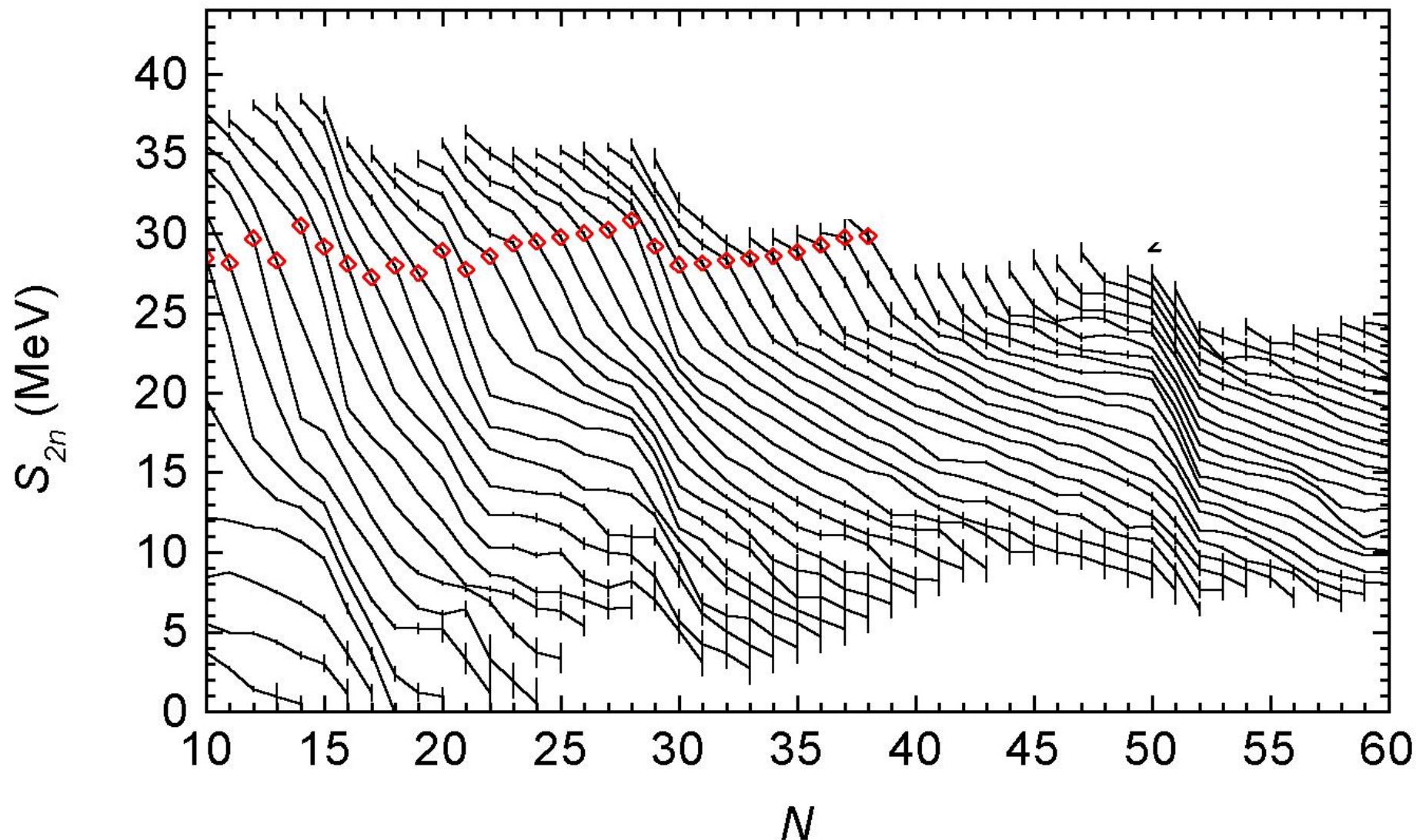




Nucleon pairing

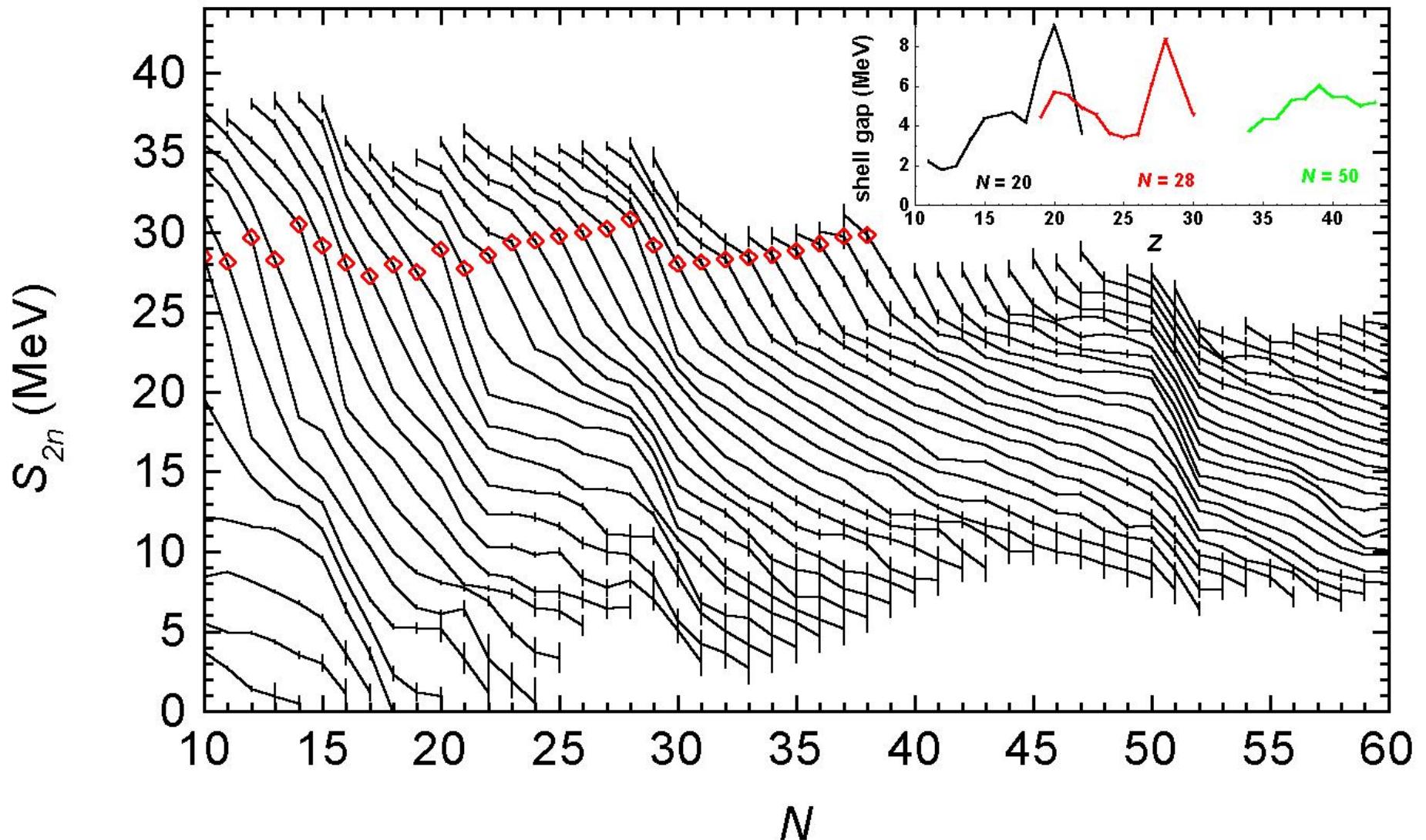


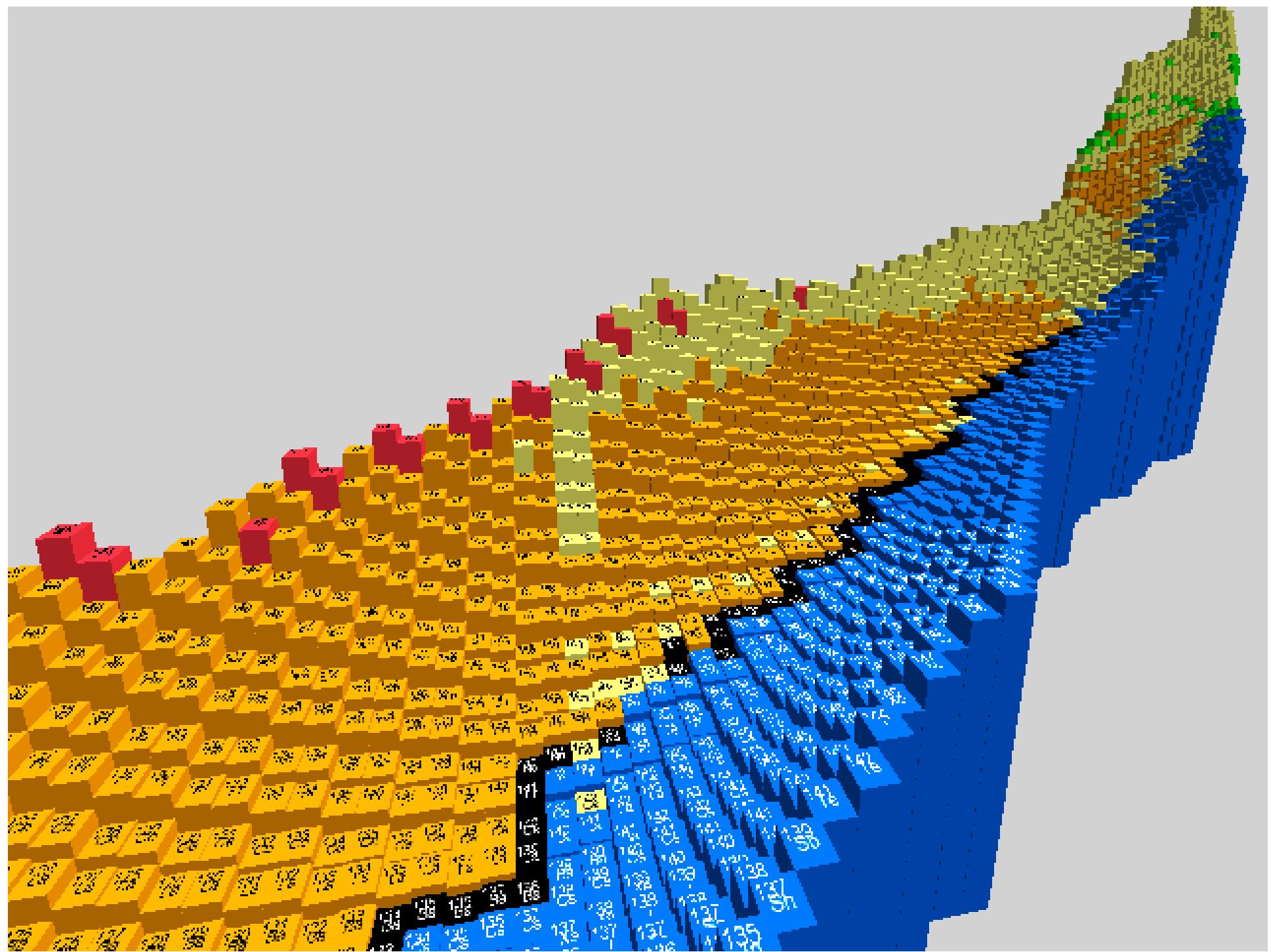
nuclear structure from the mass surface

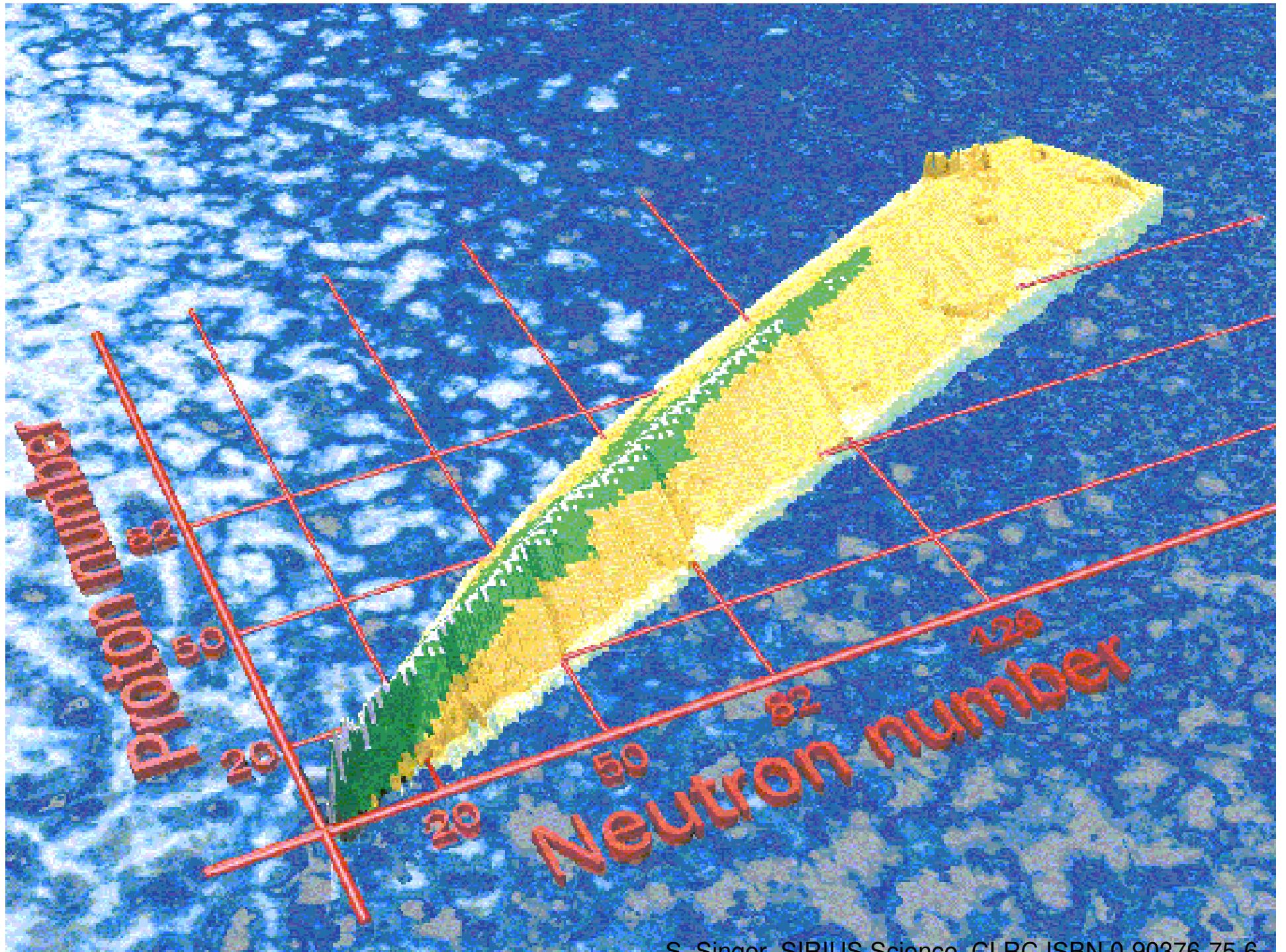


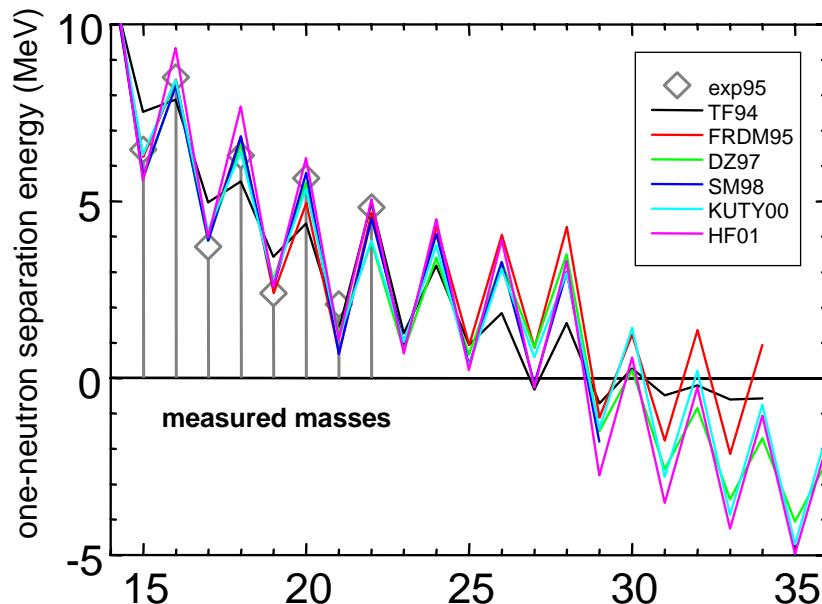
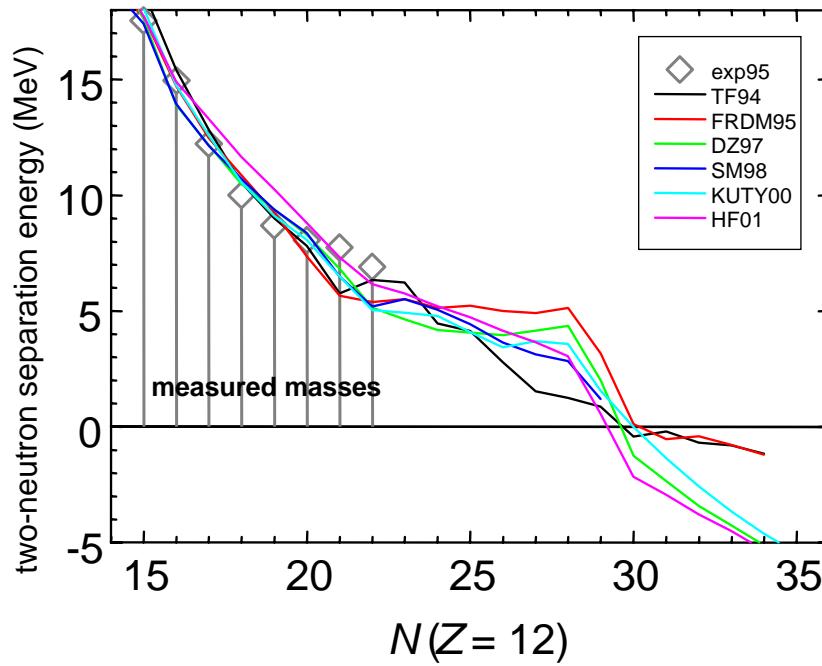
nuclear structure from the mass surface

shell opening and magic number migration

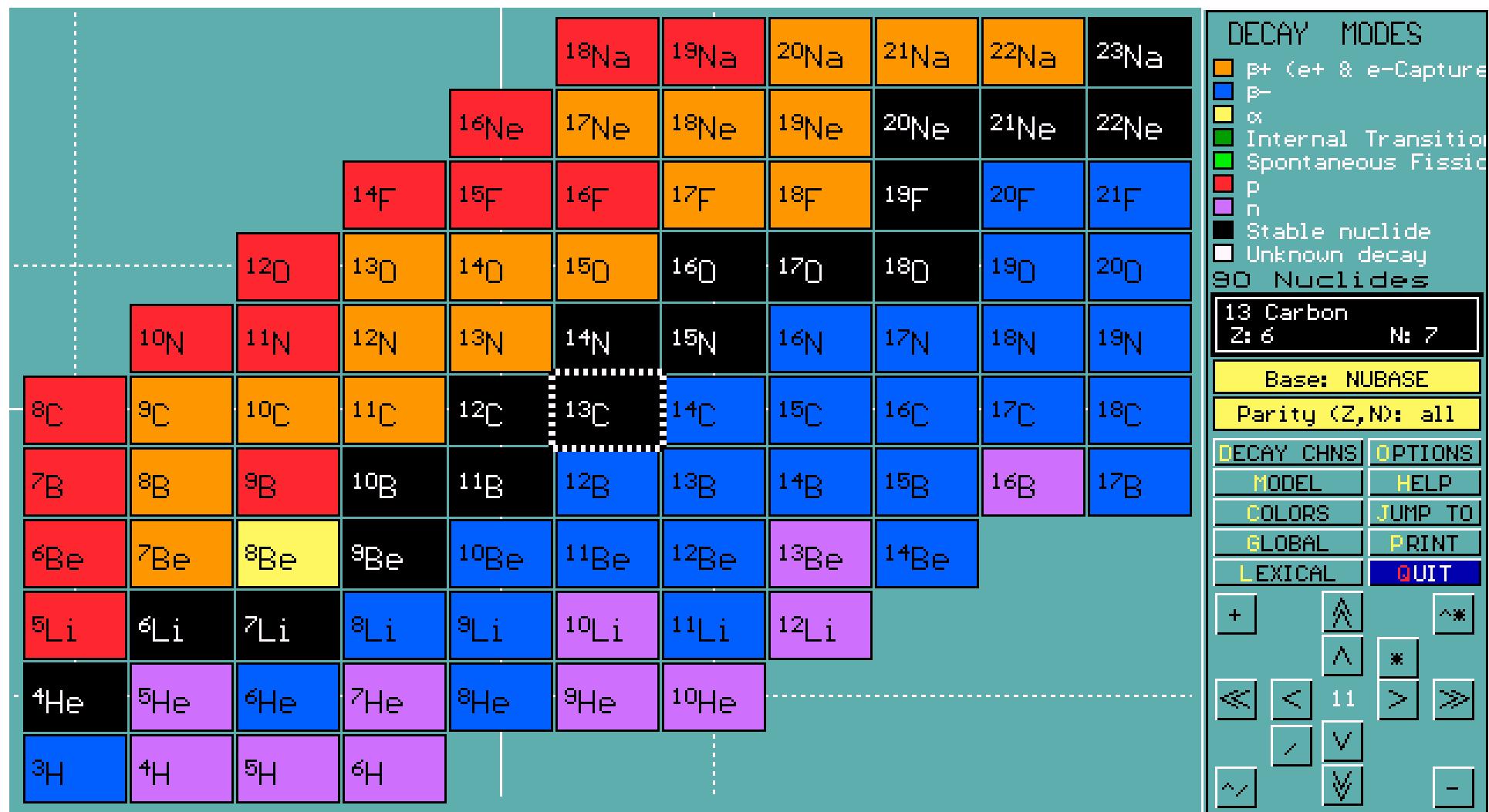




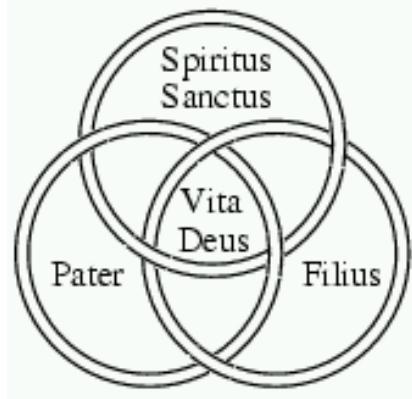
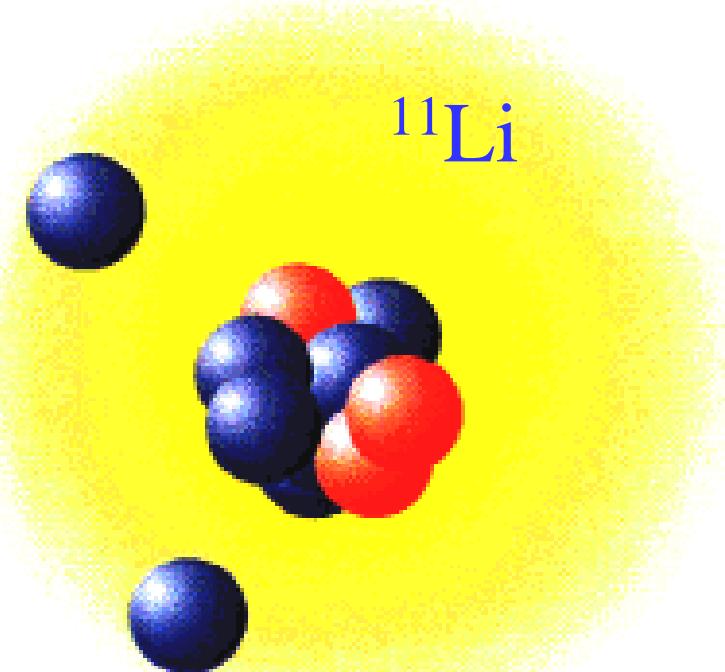


s_n  $N(Z=12)$  $N(Z=12)$ s_{2n}

drip line phenomena - small binding energies



Superlarge nuclides



Borromean system

Simple, illustrative approach
(Hansen and Jonson, 1987)

$$\rho = \hbar / (2\mu S_{2n})^{1/2}$$

For 3-body models:
 S_{2n} is *input* parameter

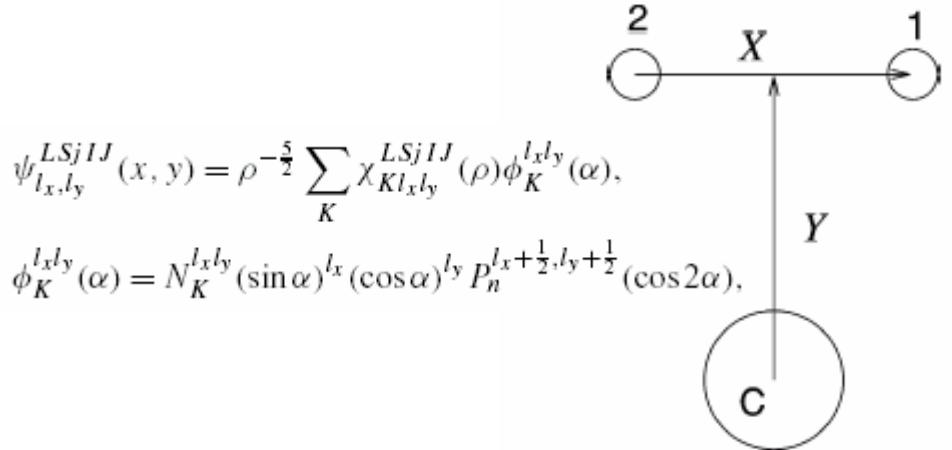
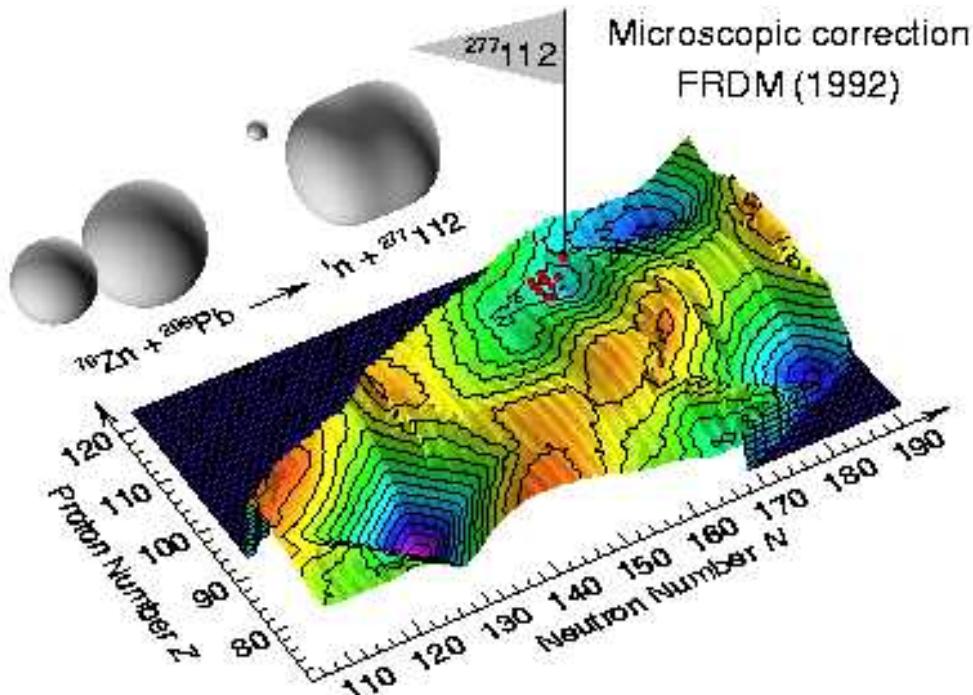
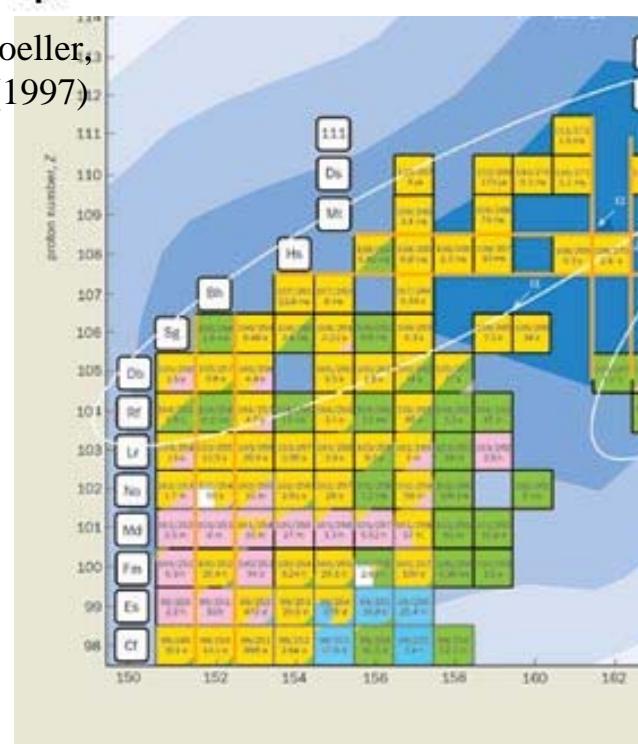


Fig. 1. The T-set of Jacobi coordinates.

$$V_{nc}(r, \theta', \phi') = \frac{V_0}{1 + e^{\frac{r - R(\theta', \phi')}{a}}} - 2 \left(\frac{\hbar^2}{m_\pi c} \right)^2 \frac{V_{ls}}{r} \frac{d}{dr} \frac{1}{1 + e^{\frac{r - R_{ws}}{a_{ws}}}} \mathbf{l} \cdot \mathbf{s}.$$

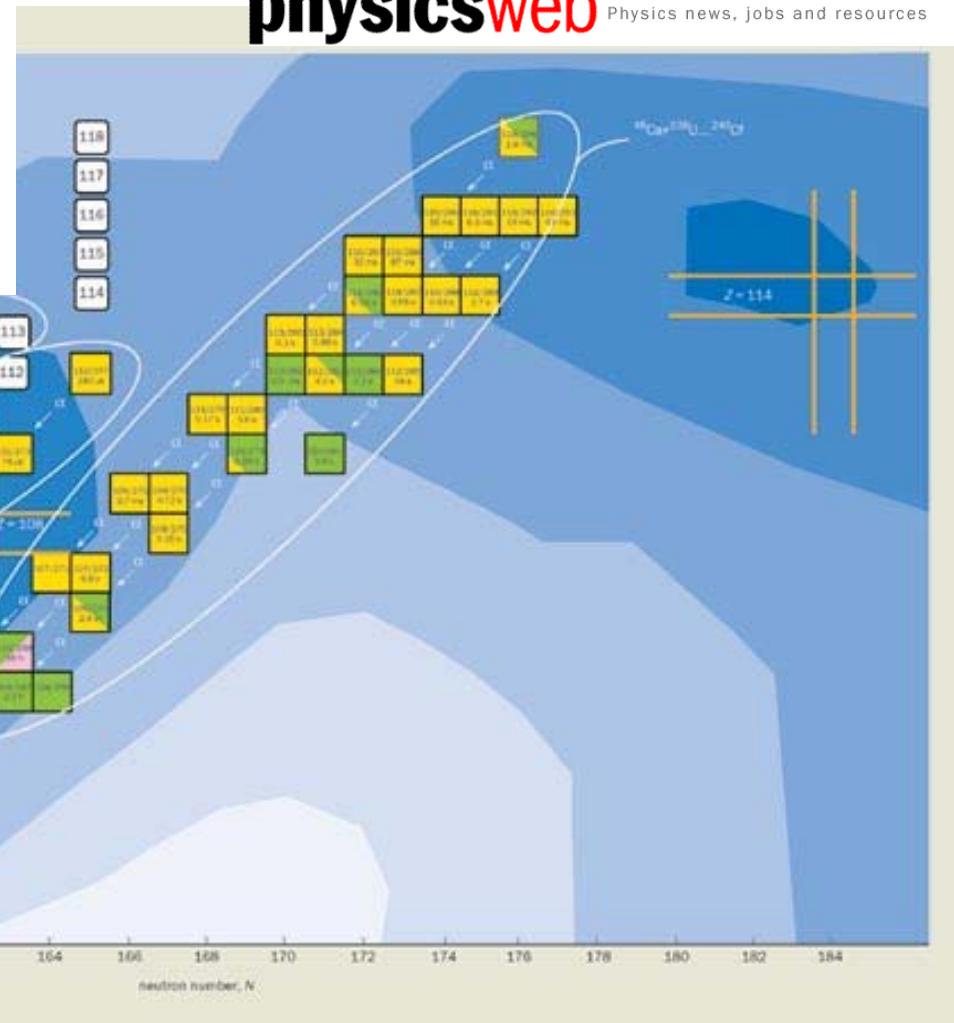


J.R. Nix and P. Moeller,
LA-UR-97-4220 (1997)

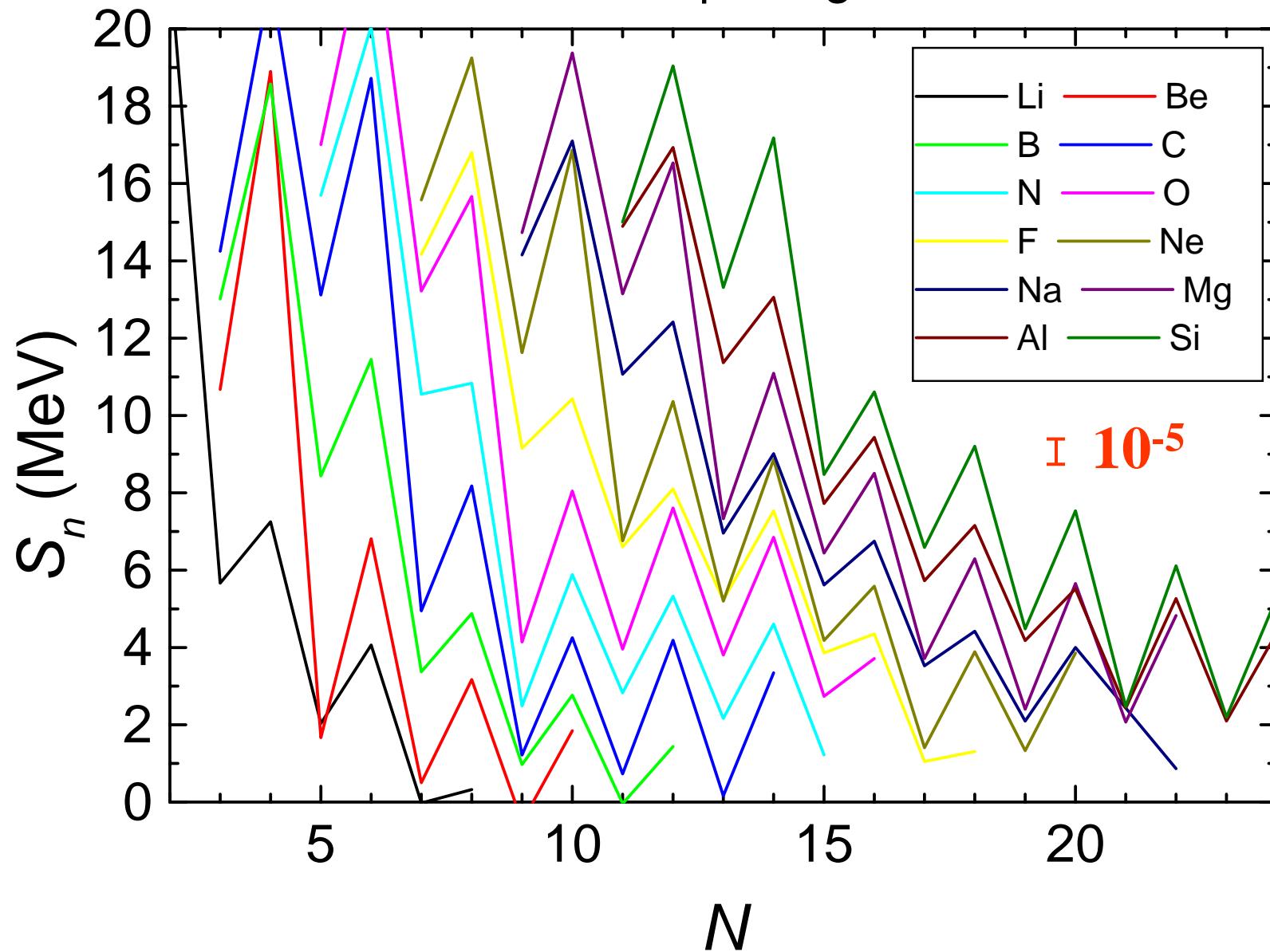


Superheavy Elements

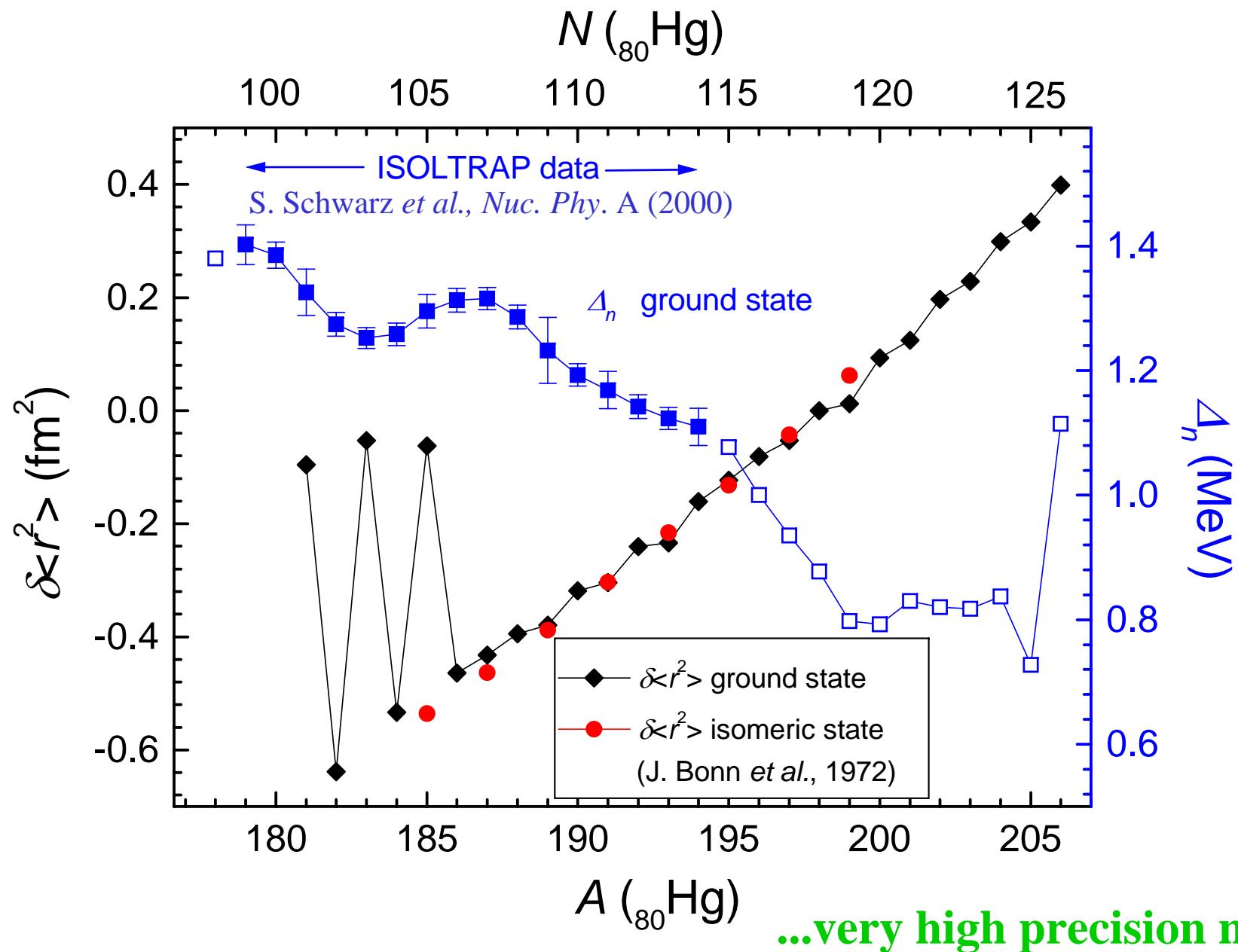
physicsweb Physics news, jobs and resources



Nucleon pairing



pairing energy... $\Delta^{(3)}(N) = \frac{(-1)^N}{2} [B(N-1) + B(N+1) - 2B(N)]$

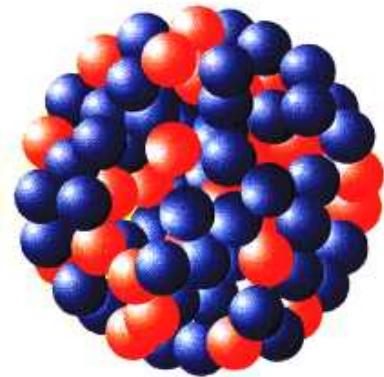


Hancock bldg
(344 m high)



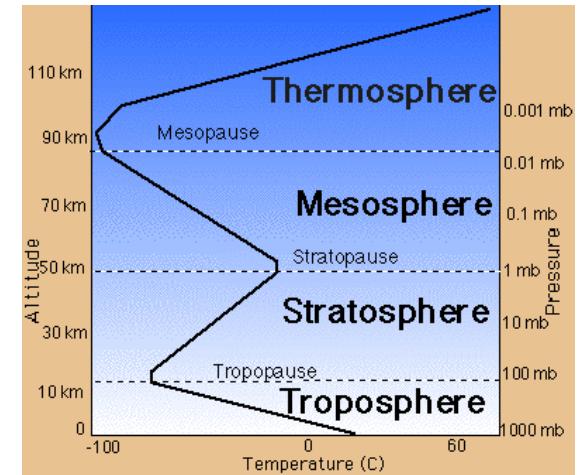
Earth's radius: 6000 km

Shell gap of
 ^{132}Sn ~ 6 MeV

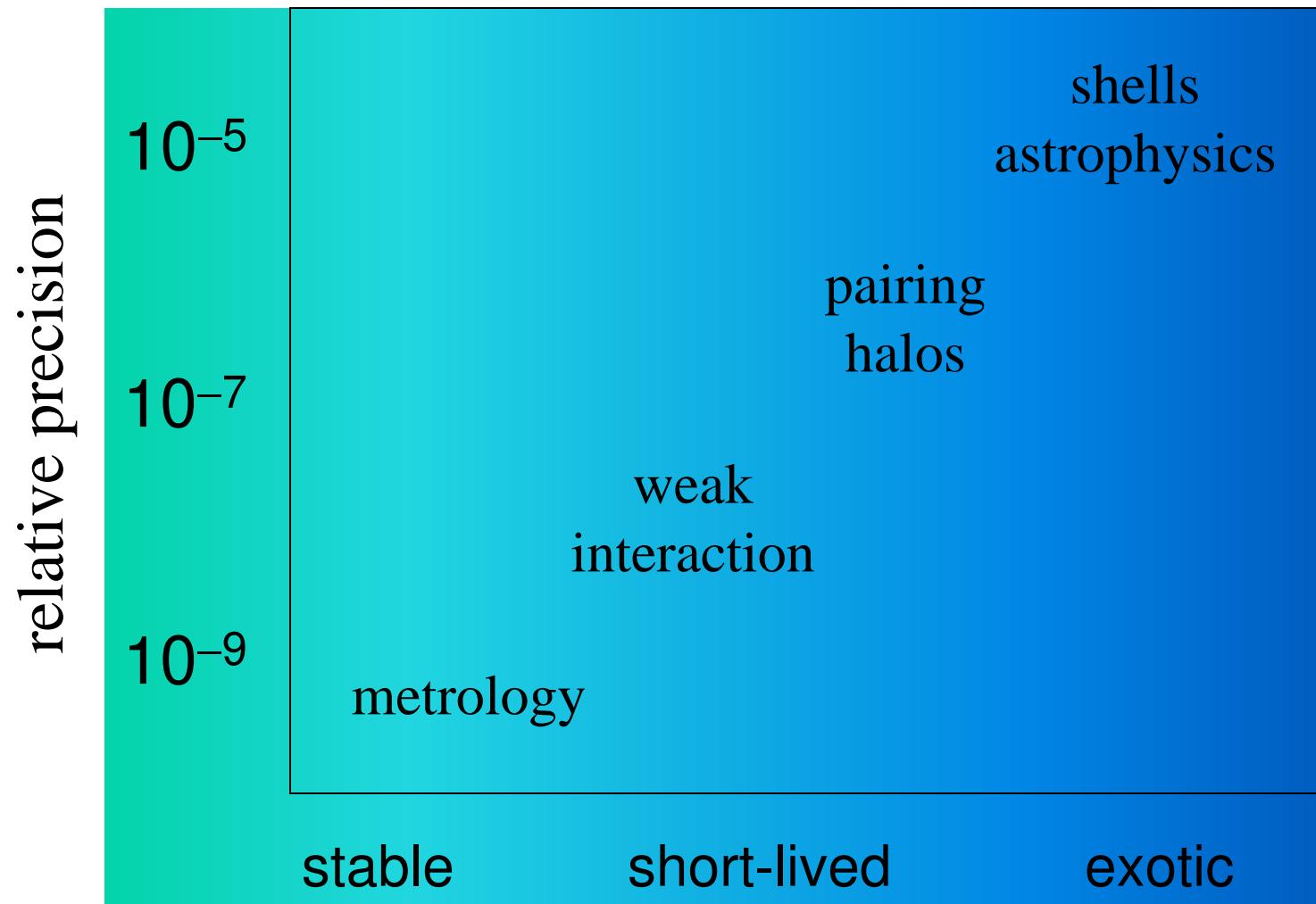


Binding Energy
of ^{132}Sn ~ 1 GeV

Pairing gap: 1 MeV



mass measurements: what you want - what you need



WORLD YEAR OF PHYSICS

A direct test of $E = mc^2$

One of the most striking predictions of Einstein's special theory of relativity is also perhaps the best known formula in all of science: $E = mc^2$. If this equation were found to be even slightly incorrect, the impact would be enormous — given the degree to which special relativity is woven into the theoretical fabric of modern physics and into everyday applications such as global positioning systems. Here we test this mass–energy relationship directly by combining very accurate measurements of atomic-mass difference, Δm , and of γ -ray wavelengths to determine E , the nuclear binding energy, for isotopes of silicon and sulphur. Einstein's relationship is separately confirmed

BETTMANN/CORBIS

in two tests, which yield a combined result of $1 - \Delta m c^2 / E = (-1.4 \pm 4.4) \times 10^{-7}$, indicating that it holds to a level of at least 0.00004%. To our knowledge, this is the most precise direct test of the famous equation yet described.

Our direct test is based on the prediction that when a nucleus captures a neutron and emits a γ -ray, the mass difference Δm between the initial (including unbound neutron) and final nuclear states, multiplied by c^2 (where c is the speed of light), should equal the energy of the emitted γ -ray(s), as determined from Planck's relation $E = hf$ (where h is Planck's constant and f is frequency).

The total energy of the γ -rays emitted as

the daughter nucleus decays to a lower energy state was determined by summing the individual γ -ray energies. These were measured by wave-length calibration of Bragg spectrometers.

The measured mass difference Δm is related to the simultaneous measurements of frequency and wavelength of the γ -ray(s). The proportionality constant depends on the mass difference between the initial and final nuclear states, the period of oscillation of the Penning trap,

undergoing this nuclear reaction, the comparison is expressed in terms of measured quantities as

$$\Delta Mc^2 = (M[^A\text{X}] - M[^{A+1}\text{X}] + M[\text{D}] - M[\text{H}])c^2 = 10^3 N_A h(f_{A+1} - f_{\text{D}}) \text{ mol AMU kg}^{-1} \quad (1)$$

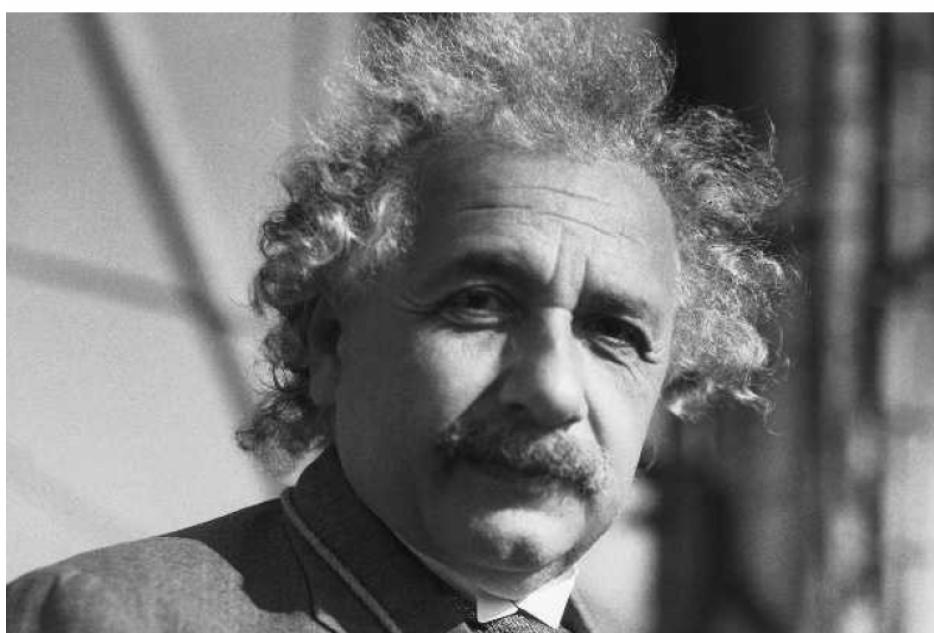
where the Avogadro constant N_A relates the measured mass $M[\text{X}]$ in unified atomic mass units (AMU) to its mass in kilograms $m[\text{X}]$. We made comparisons for $^{A+1}\text{X} = ^{29}\text{Si}$ and $^{A+1}\text{X} = ^{33}\text{S}$. The mass of the neutron $M[n]$ is determined from the masses¹ of hydrogen $M[\text{H}]$ and deuterium $M[\text{D}]$ combined with f_{D} , the frequency of the γ -ray corresponding to the deuteron binding energy². The molar Planck constant is $N_A h = 3.990312716(27) \times 10^{-10} \text{ J s mol}^{-1}$; numbers in parentheses indicate uncertainty on the last digits. This figure has been independently confirmed at about the 5×10^{-8}

Simon Rainville*†, **James K. Thompson***,
Edmund G. Myers‡, **John M. Brown§**,
Maynard S. Dewey||, **Ernest G. Kessler Jr||**,
Richard D. Deslattes||, **Hans G. Börner¶**,
Michael Jentschel¶, **Paolo Mutti¶**,
David E. Pritchard*

*Research Laboratory of Electronics,
MIT-Harvard Center for Ultracold Atoms, and

||National Institute of Standards and Technology,
Gaithersburg, Maryland 20899, USA

¶Institut Laue-Langevin, 38042 Grenoble Cedex,
Because the diffraction angle for a 5-MeV



Motivation from “fundamental” physics



metrology:

*the kilogram: ^{28}Si atomic mass standard and other fundamental constants
(what if they vary with time?!)*



NATURE 2589—26/5/2004—VBICKNELL—104661

A precision measurement of the mass of the top quark

D0 Collaboration*

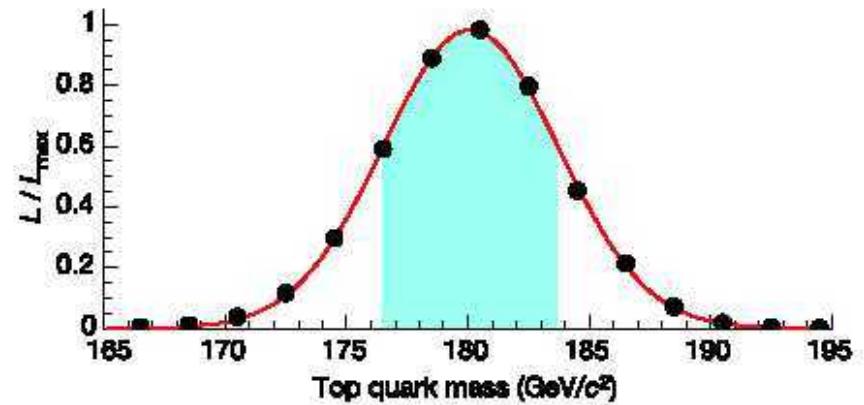


Figure 4 Determination of the mass of the top quark using the maximum-likelihood corresponds to a mass of $180.1 \text{ GeV}/c^2$, which is the new D0 measurement of $M_t \pm 3.6 \text{ GeV}/c^2$ statistical uncertainty of the fit.

What does a relative uncertainty of 10^{-8} mean?

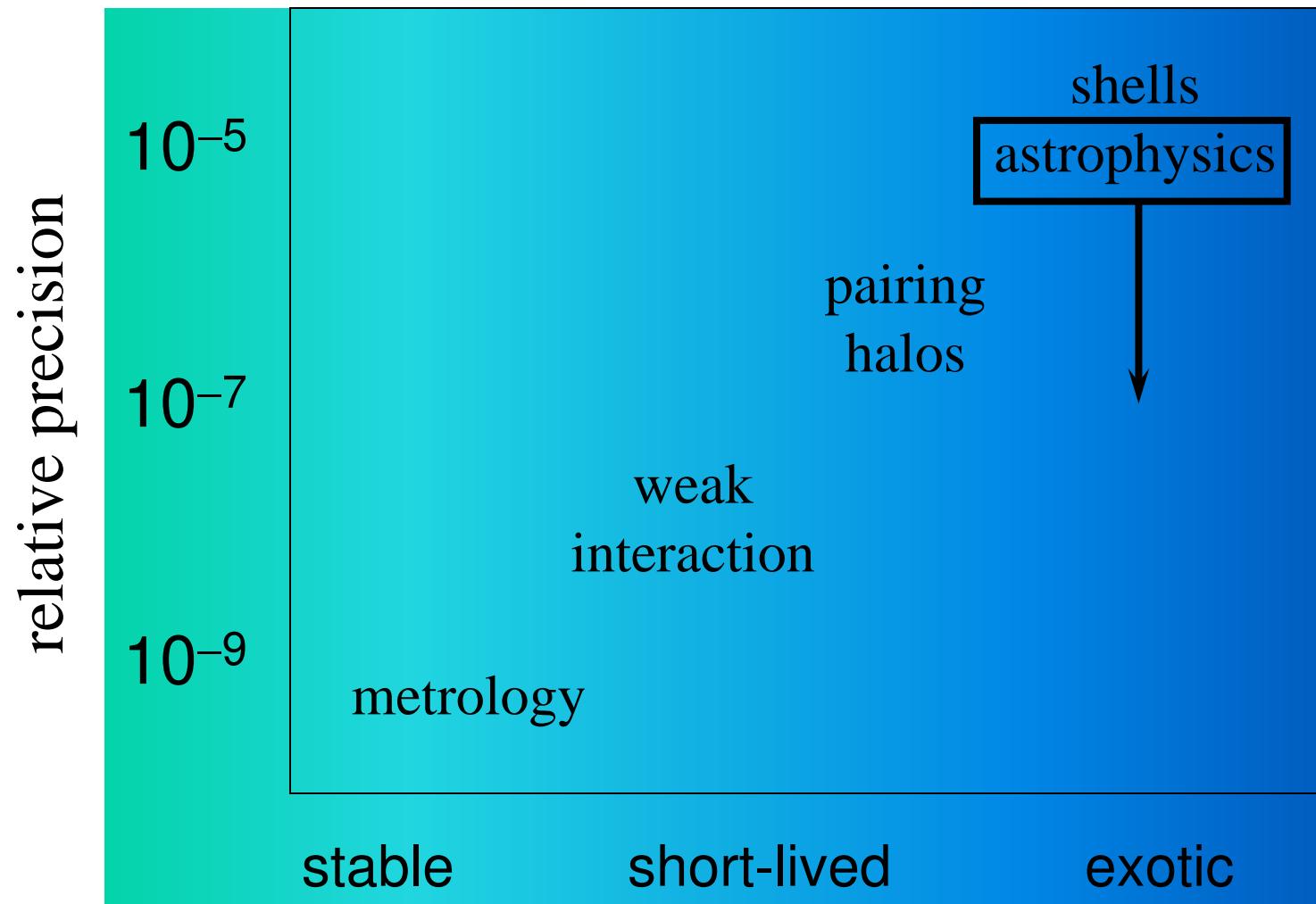


weight (empty): 164000 kg



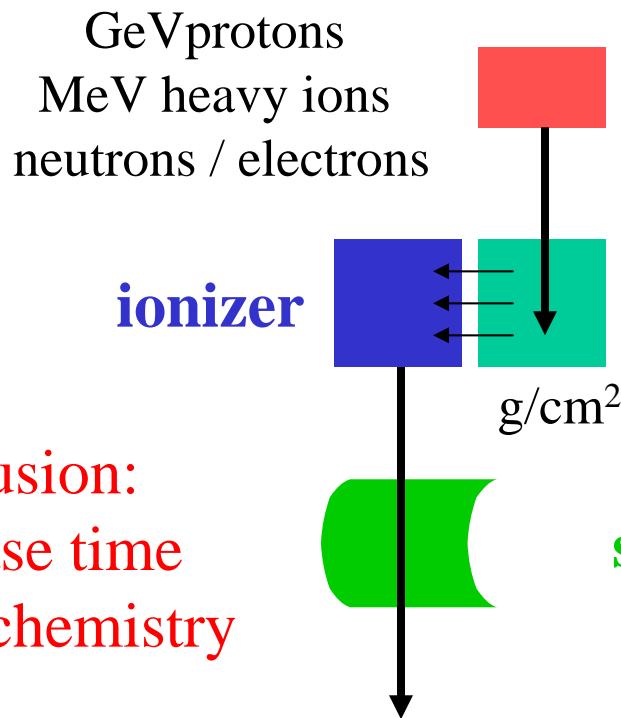
contact lenses?

mass measurements: what you want - what you need

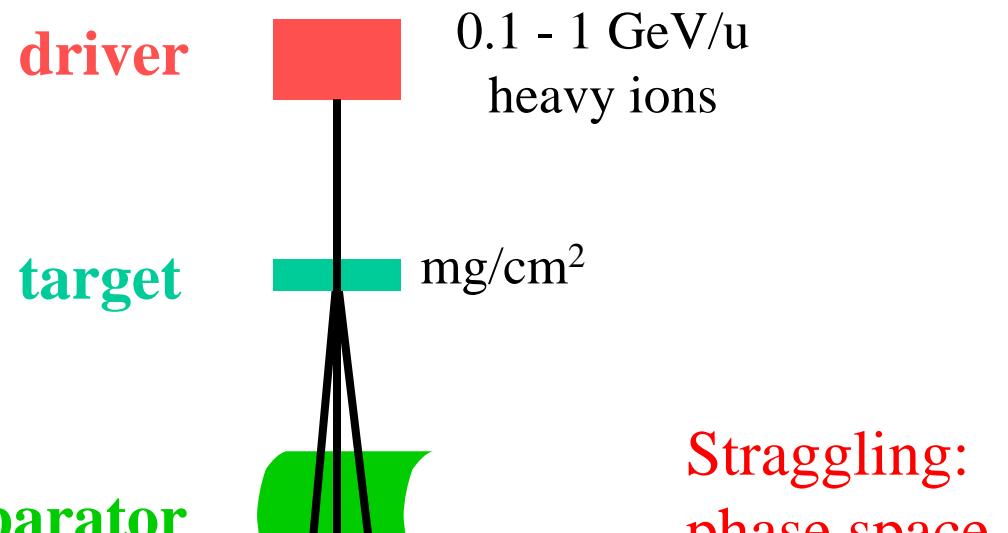


Production (and separation) techniques for exotic nuclides

Isotope Separation On-Line (ISOL)



Fragmentation In-Flight Separation (FIFS)



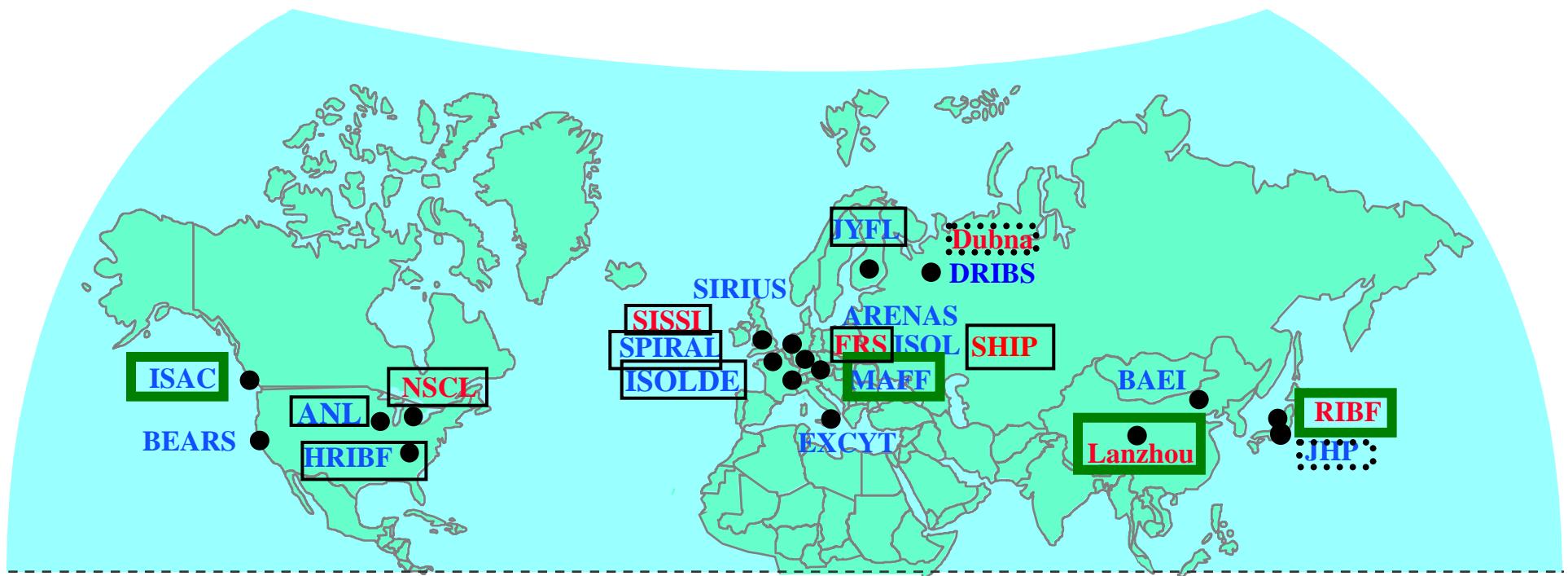
10-100 keV

good beam quality
(charge-breeding)
post-acceleration

0.1-1 GeV

short lived / unbound
deceleration
or stopping

worldwide radioactive ion beam facilities



ISOL thick-target facilities

in-flight separation facilities

MASS MEASUREMENTS

(NEAR) FUTURE

Techniques



*Indirect
(energy)*

reactions:



$$Q = M_A + M_a - M_b - M_B$$

decays:



$$Q_\alpha = M_B - M_A$$

*Direct
(mass spectrometry)*

time of flight:

$$TOF = (m/q) (L/B\rho)$$

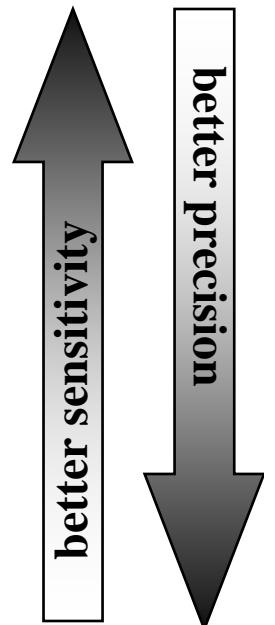
cyclotron frequency:

$$f_c = qB/m$$

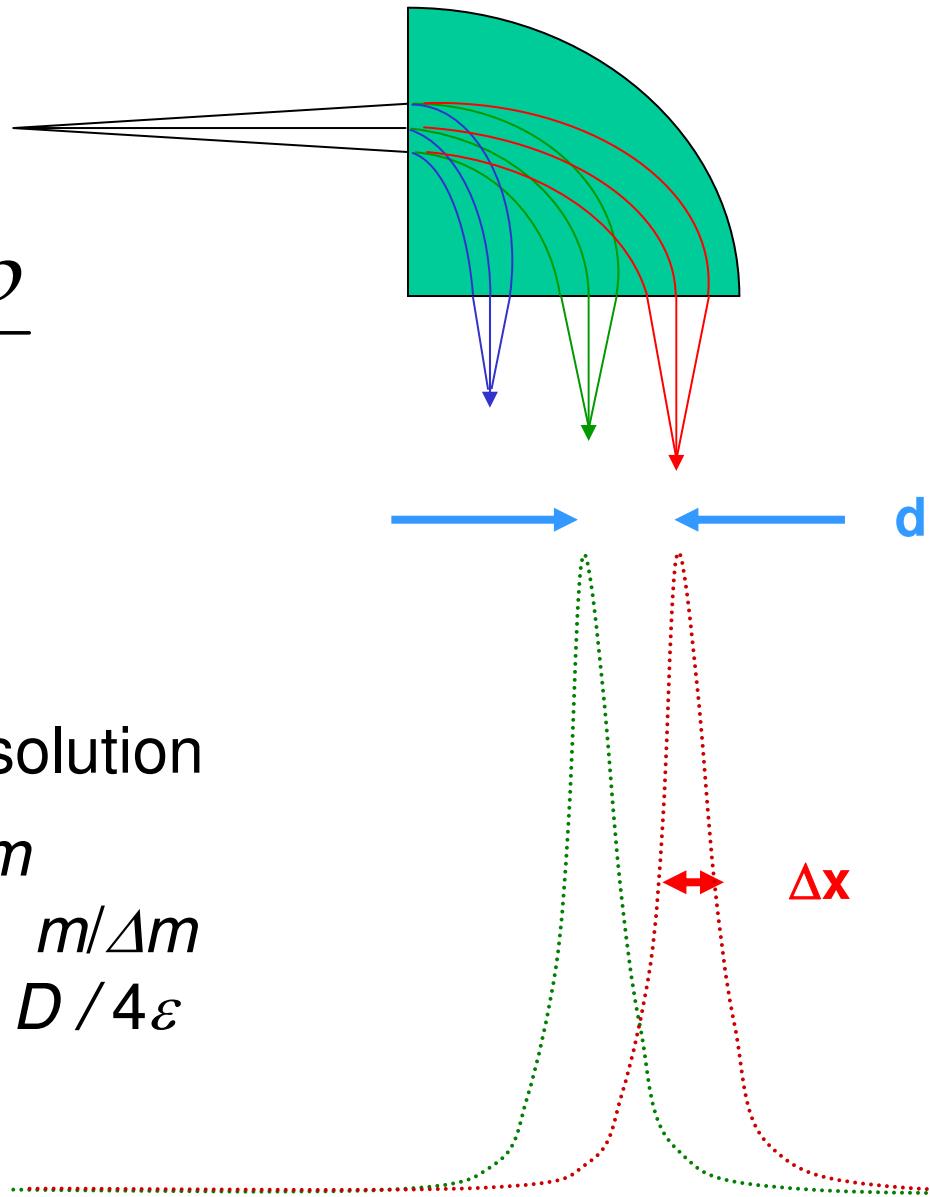
*PRODUCTION
SCHEME*

FIFS
(MeV)

ISOL
(keV)



$$\frac{m}{q} = \frac{B\rho}{v}$$



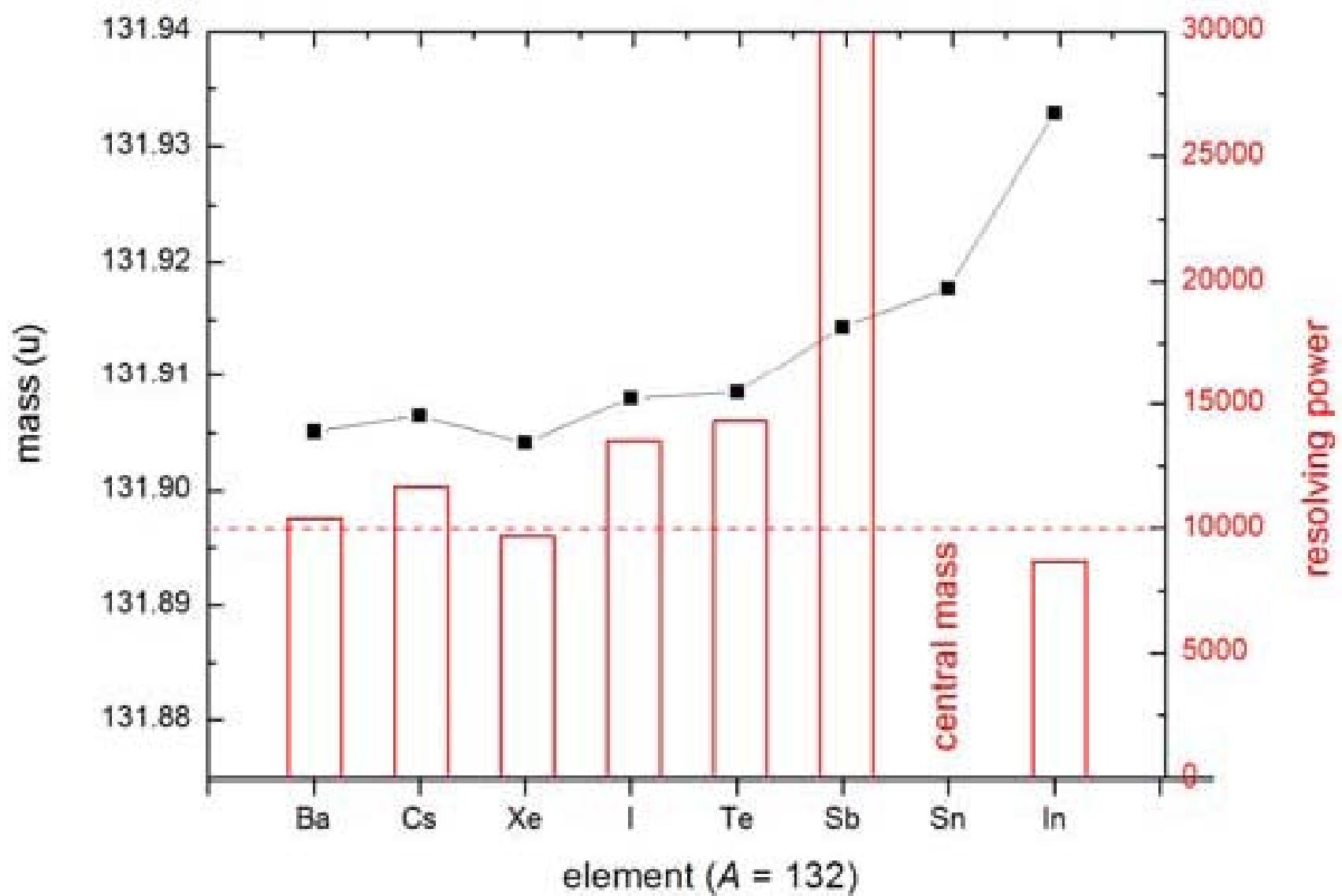
Mass Resolution

$$\begin{aligned} R &= m/\Delta m \\ &= d/\Delta x \quad m/\Delta m \\ &= \pi \Delta a D / 4\varepsilon \end{aligned}$$

Mass separator
-spectroscope
-spectrograph
-spectrometer

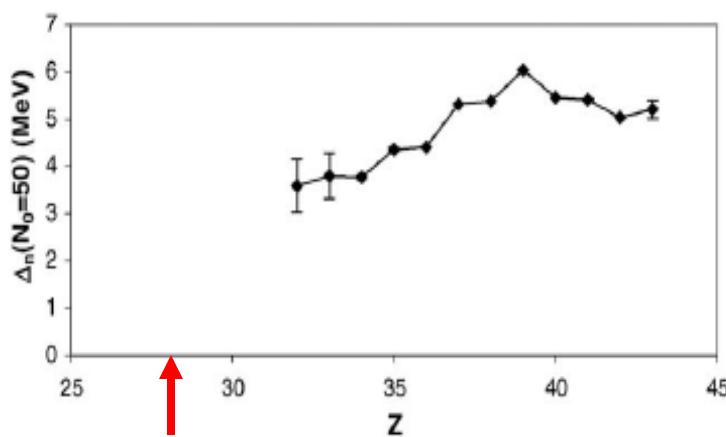
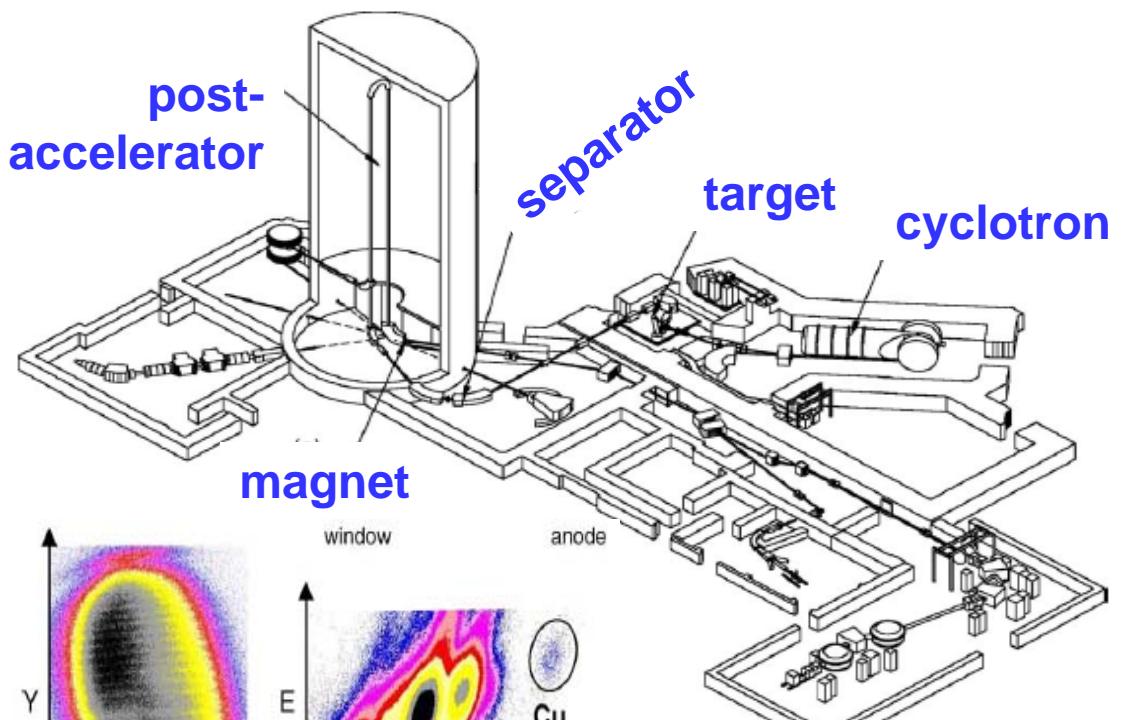
Dispersion
 $D = d m/\Delta m$

high resolution *necessary but not sufficient* for high precision

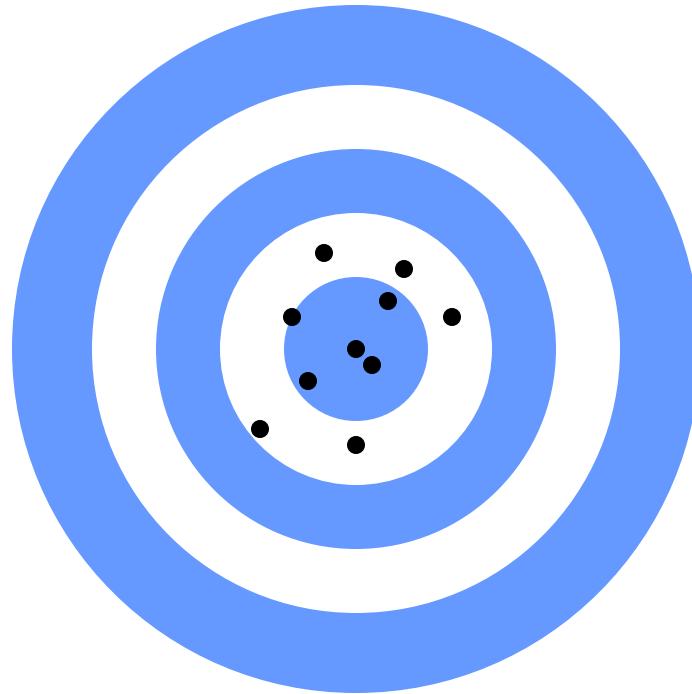


Opportunistic mass measurements at the Holifield Radioactive Ion Beam Facility

P.A. Hausladen^{a,*}, J.R. Beene^a, A. Galindo-Uribarri^a, Y. Larochele^b, J.F. Liang^a,
P.E. Mueller^a, D. Shapira^a, D.W. Stracener^a, J. Thomas^c, R.L. Varner^a, H. Wollnik^a

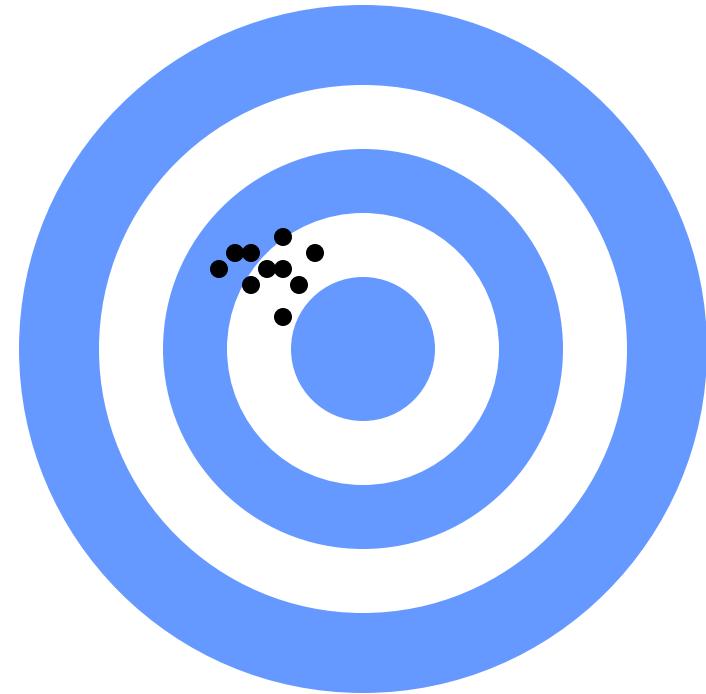


accurate



...but not
precise

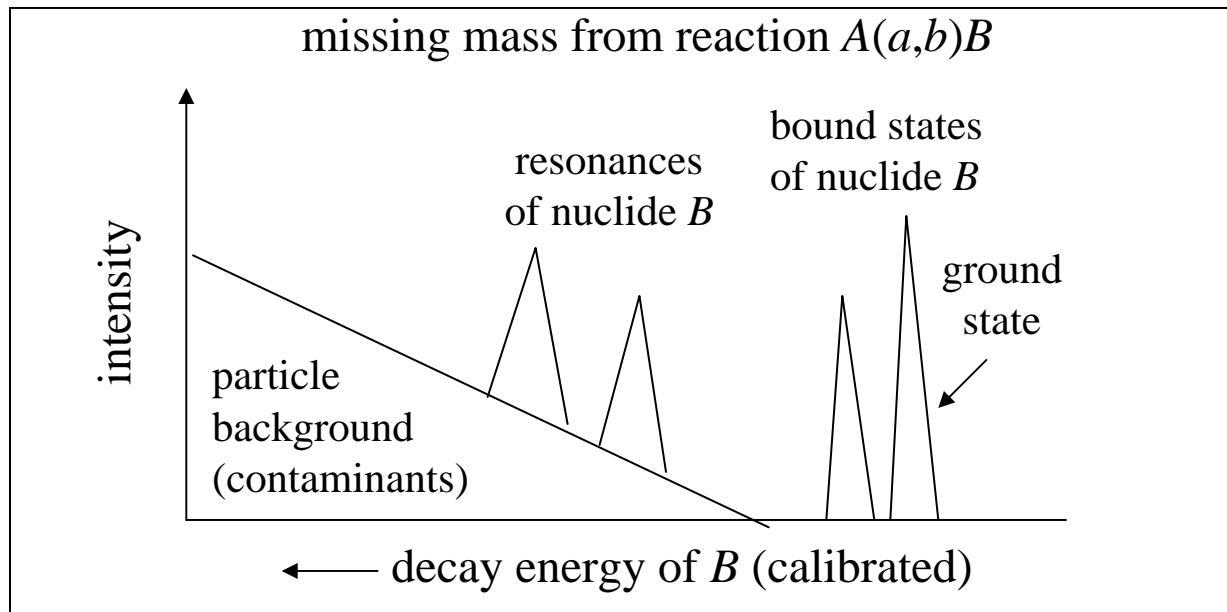
precise



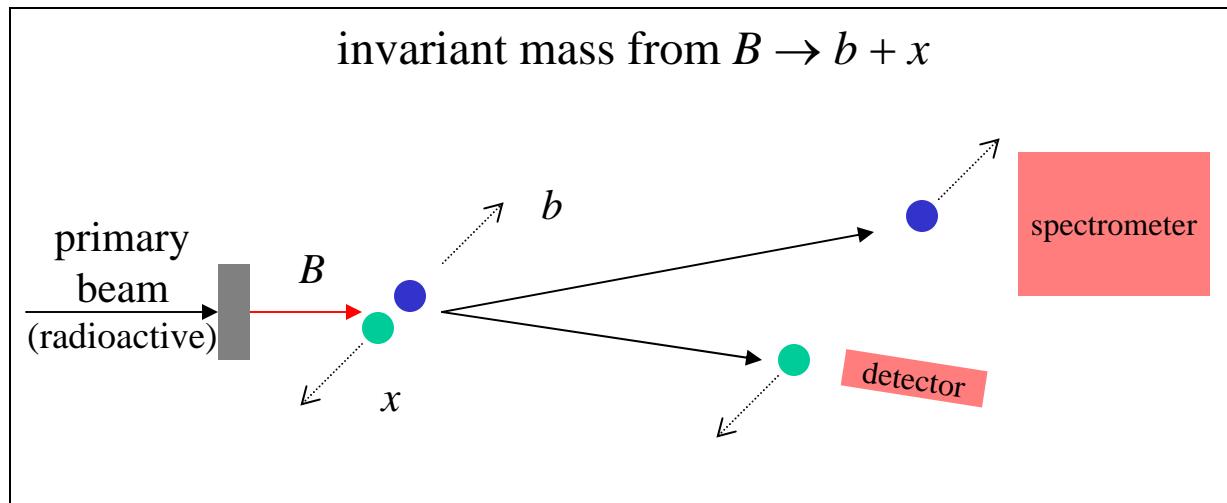
...but not
accurate

high precision *necessary but not sufficient* for high accuracy

Mass measurements by reactions



$$M_B = M_A + M_a - M_b - Q$$

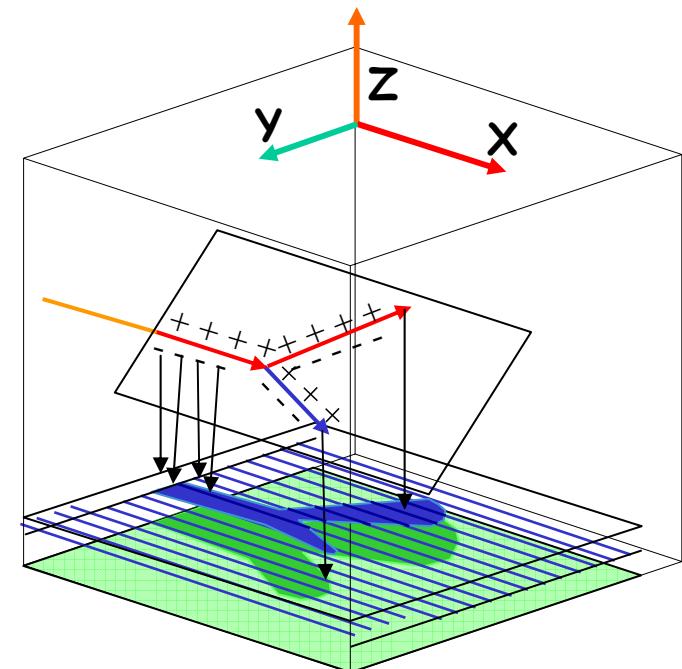
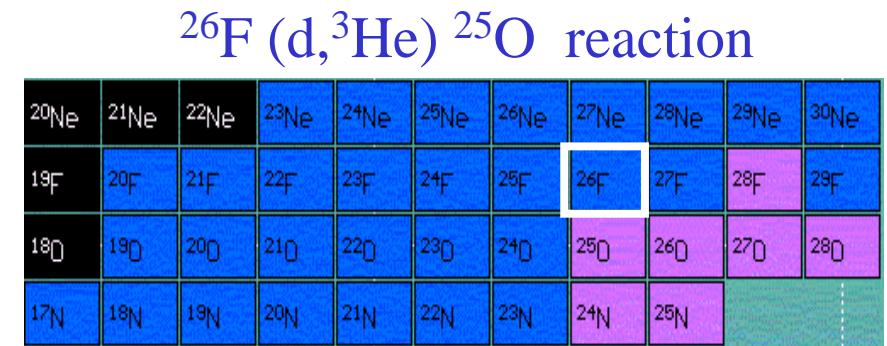
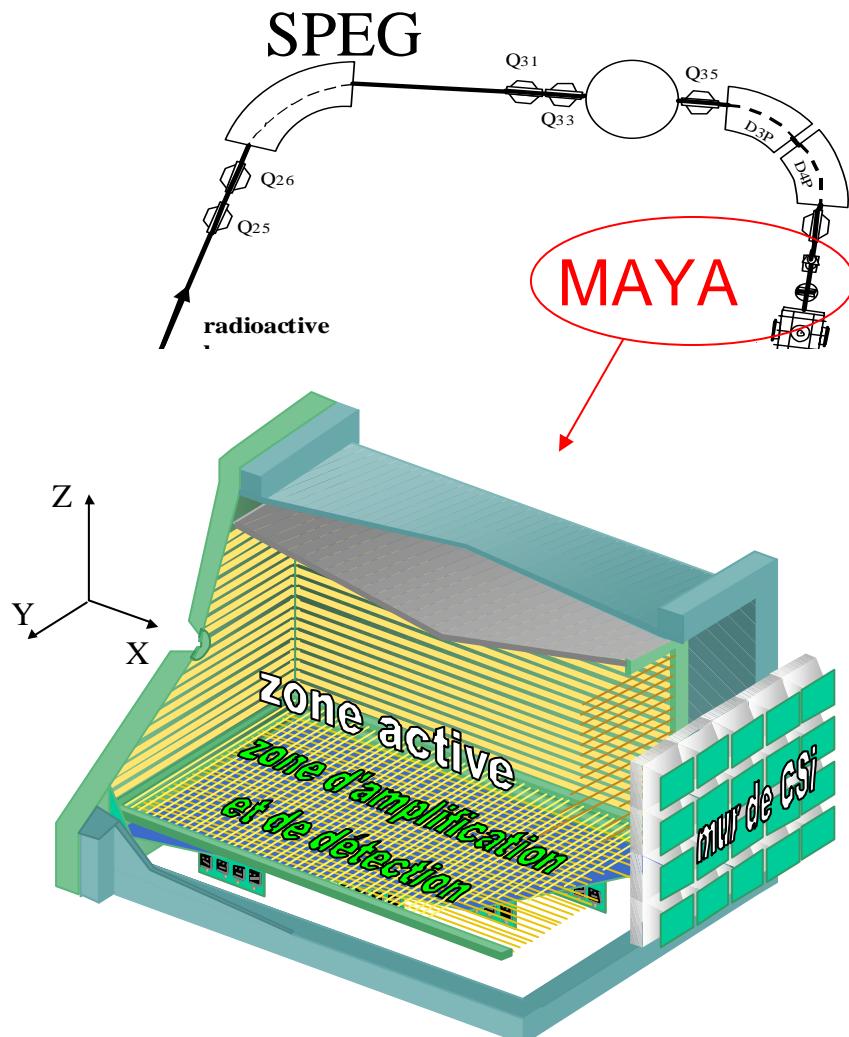


$$M_B = \{ M_x^2 + M_b^2 + 2E_x^{\text{lab}} E_b^{\text{lab}} - 2P_x^{\text{lab}} P_b^{\text{lab}} \}^{1/2}$$

$^{10}\text{Li}, ^{13}\text{Be}, ^{18}\text{Na}$

Somewhat limited but imperative for unbound

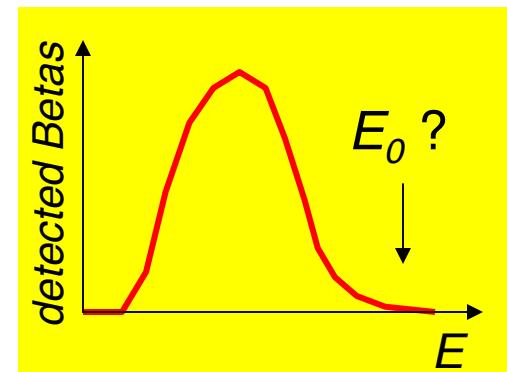
masses of unbound nuclides using MAYA at GANIL



C.-E. Demonchy Ph.D. (2003)

Mass measurements by Beta decay: $Q_\beta = M_{parent} - M_{daughter}$

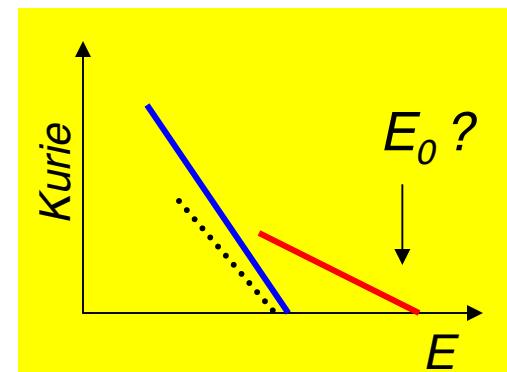
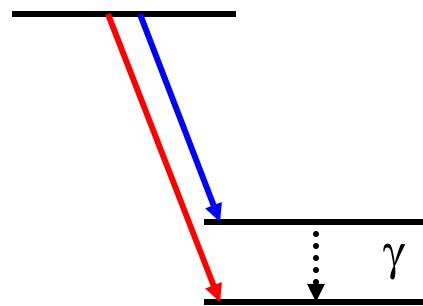
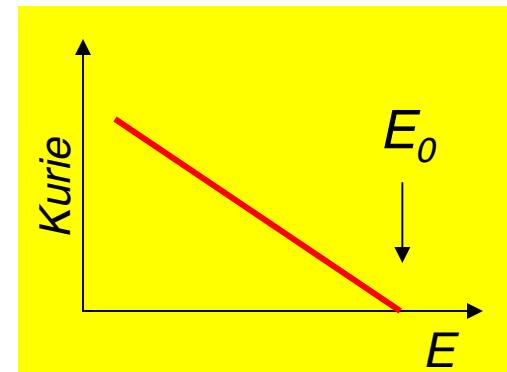
$$P(p) dp = \frac{G^2 |M_{if}|^2}{2\pi^3 \hbar^7 C^3} p^2 (E_0 - E)^2 F(Z, E)$$



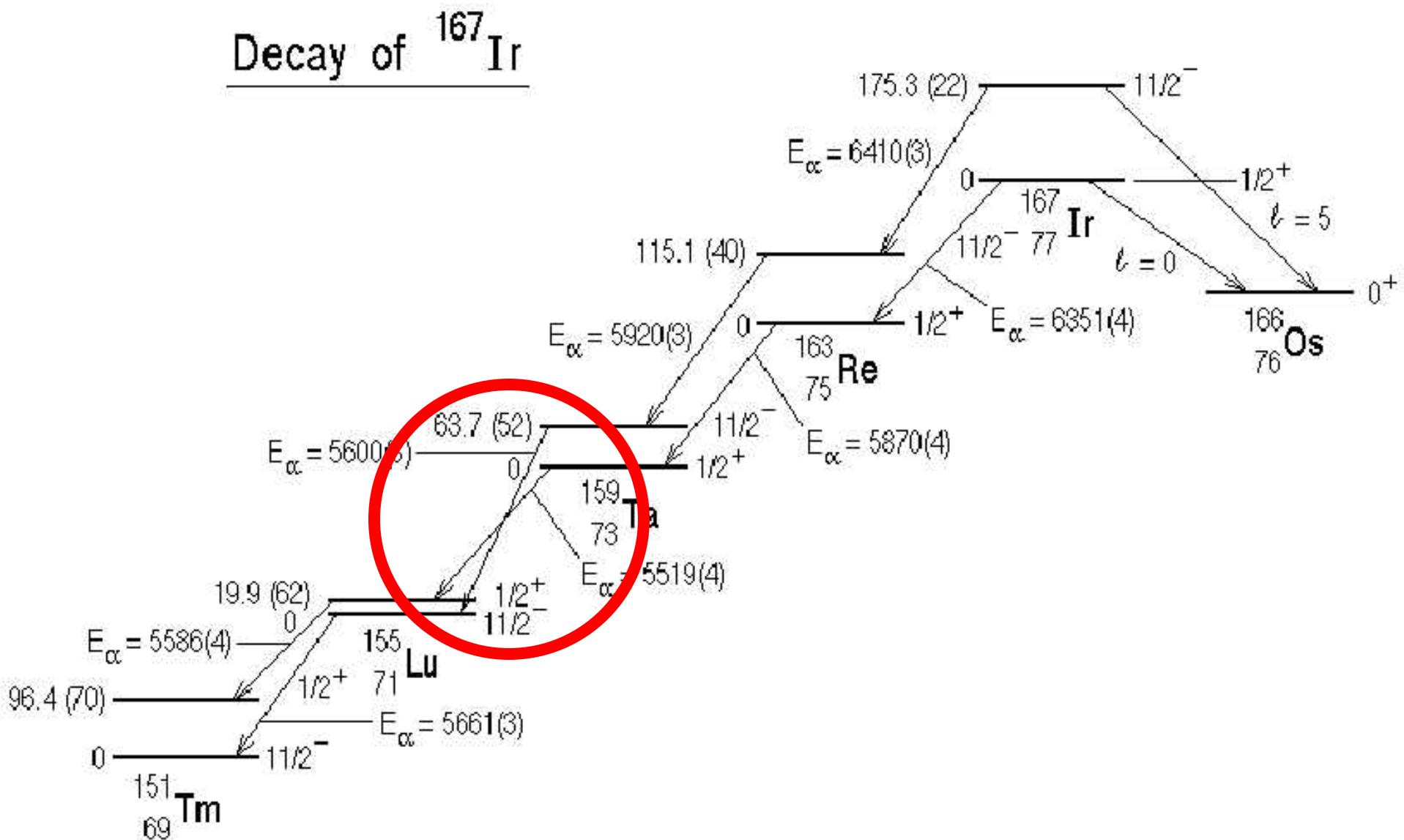
Kurie Plot: $[P(p) / p^2 F(Z, E)]^{1/2}$ vs. E

Instrumentation effects (response function)

Decay Branching (detailed spectroscopy)



Mass measurements by alpha and proton decay



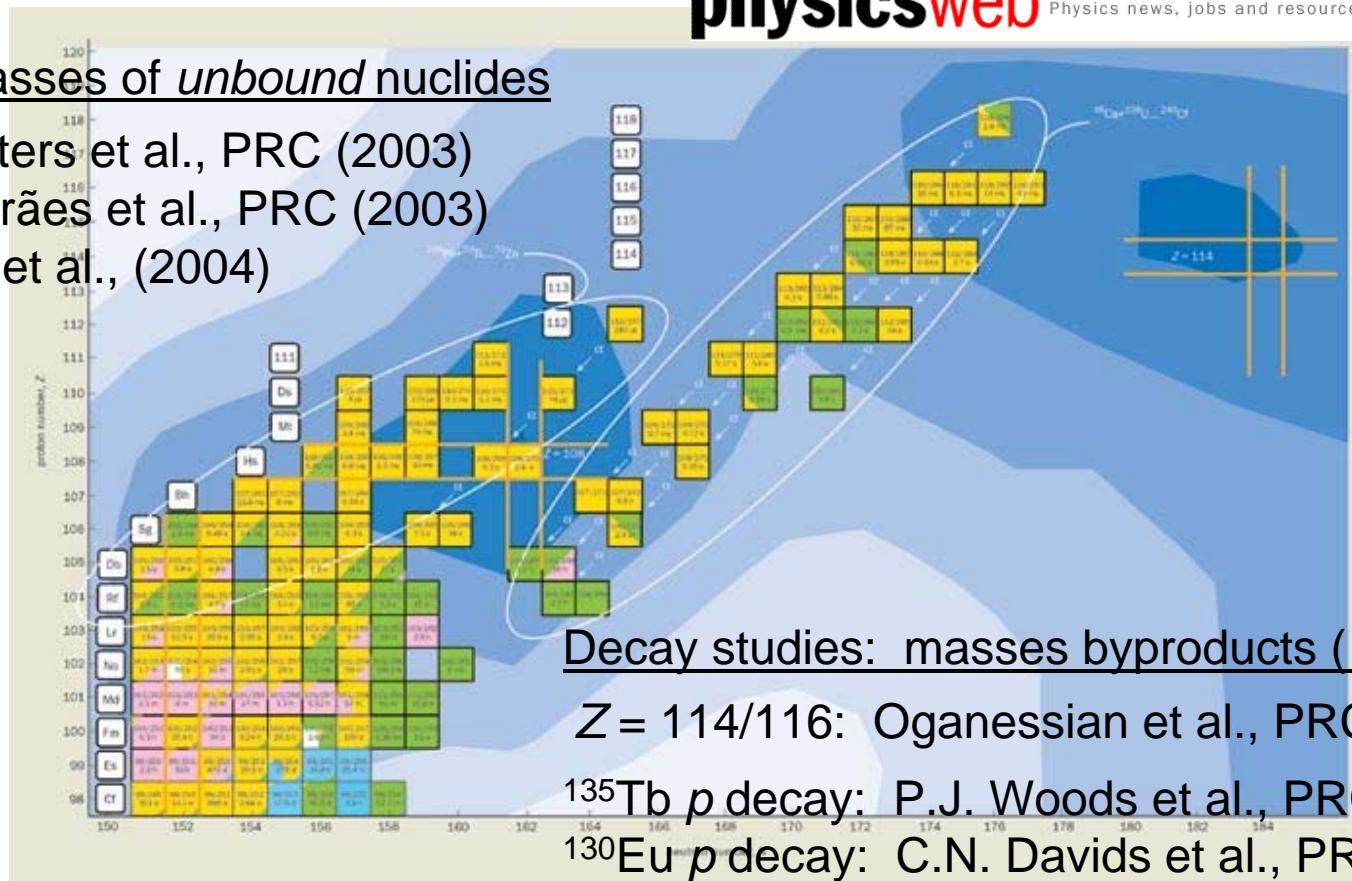
reactions and decays (so-called ‘indirect’ techniques)

Reactions: masses of unbound nuclides

^{15}F : W. A. Peters et al., PRC (2003)

^{11}N : V. Guimarães et al., PRC (2003)

^{25}O : W. Mittig et al., (2004)



Decay studies: masses byproducts (Q-values)

$Z = 114/116$: Oganessian et al., PRC (2004)

^{135}Tb ρ decay: P.J. Woods et al., PRC (2004)

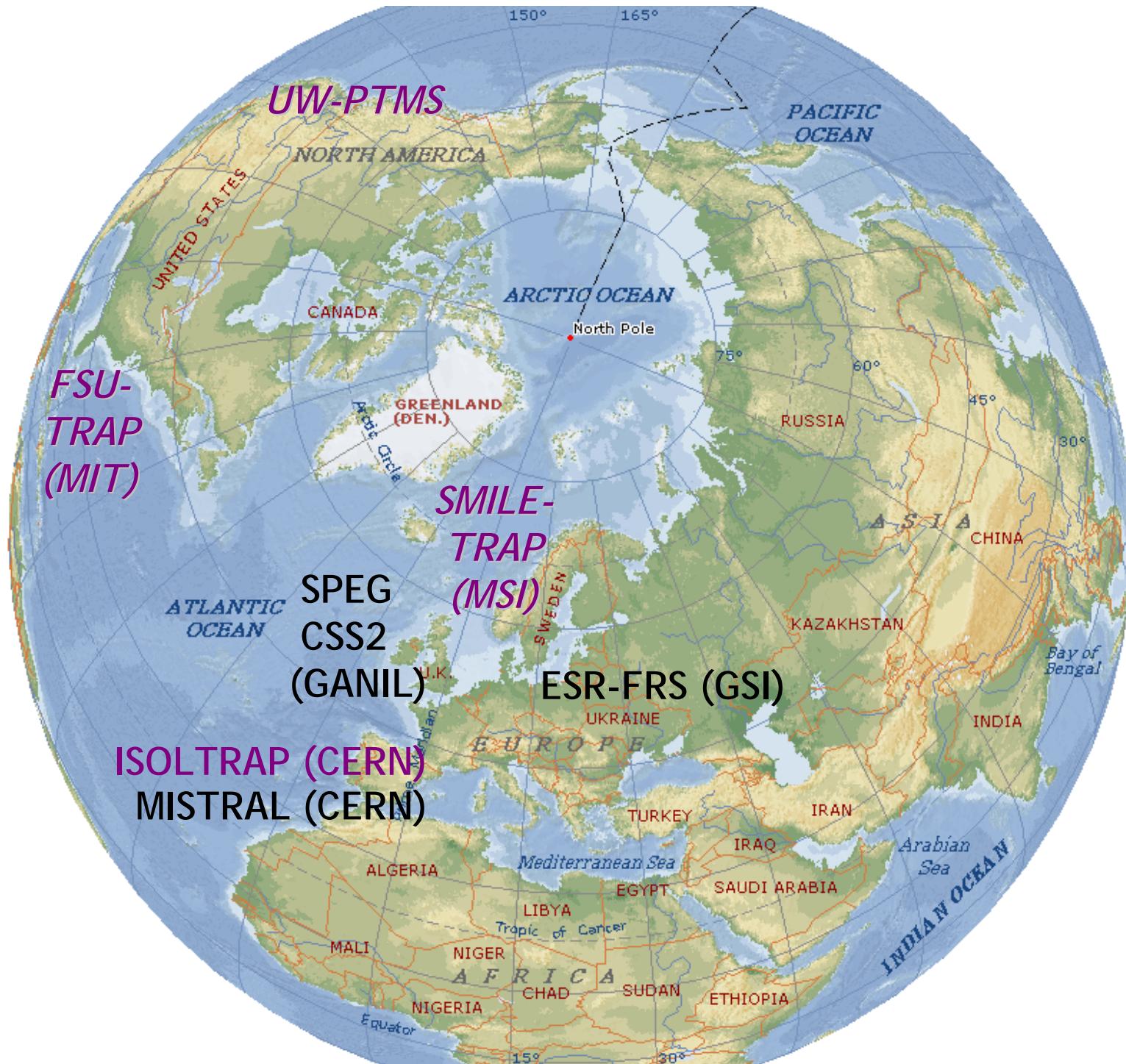
^{130}Eu ρ decay: C.N. Davids et al., PRC (2004)

^{233}Am α decay: M. Sakama et al., PRC (2004)

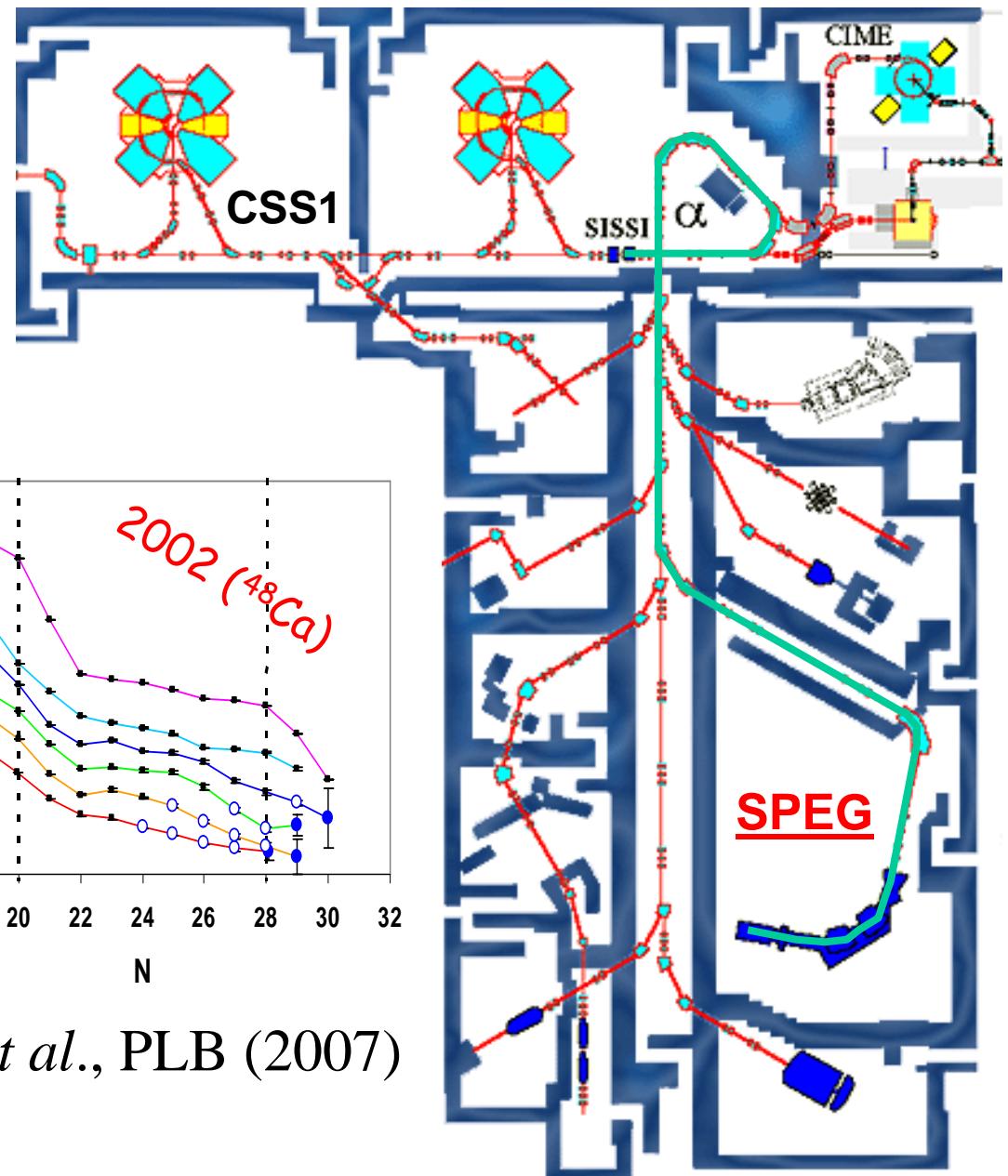
^{265}Bh α decay: Z.G. Gan et al., EPJA (2004)

^{130}Cd β decay: I. Dillmann et al., PRL (2003)

Mass values for the most exotic species



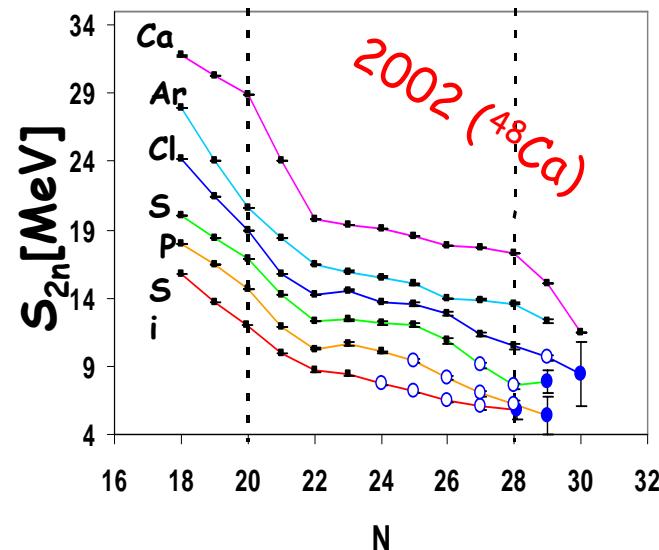
mass measurement programs at *GANIL*



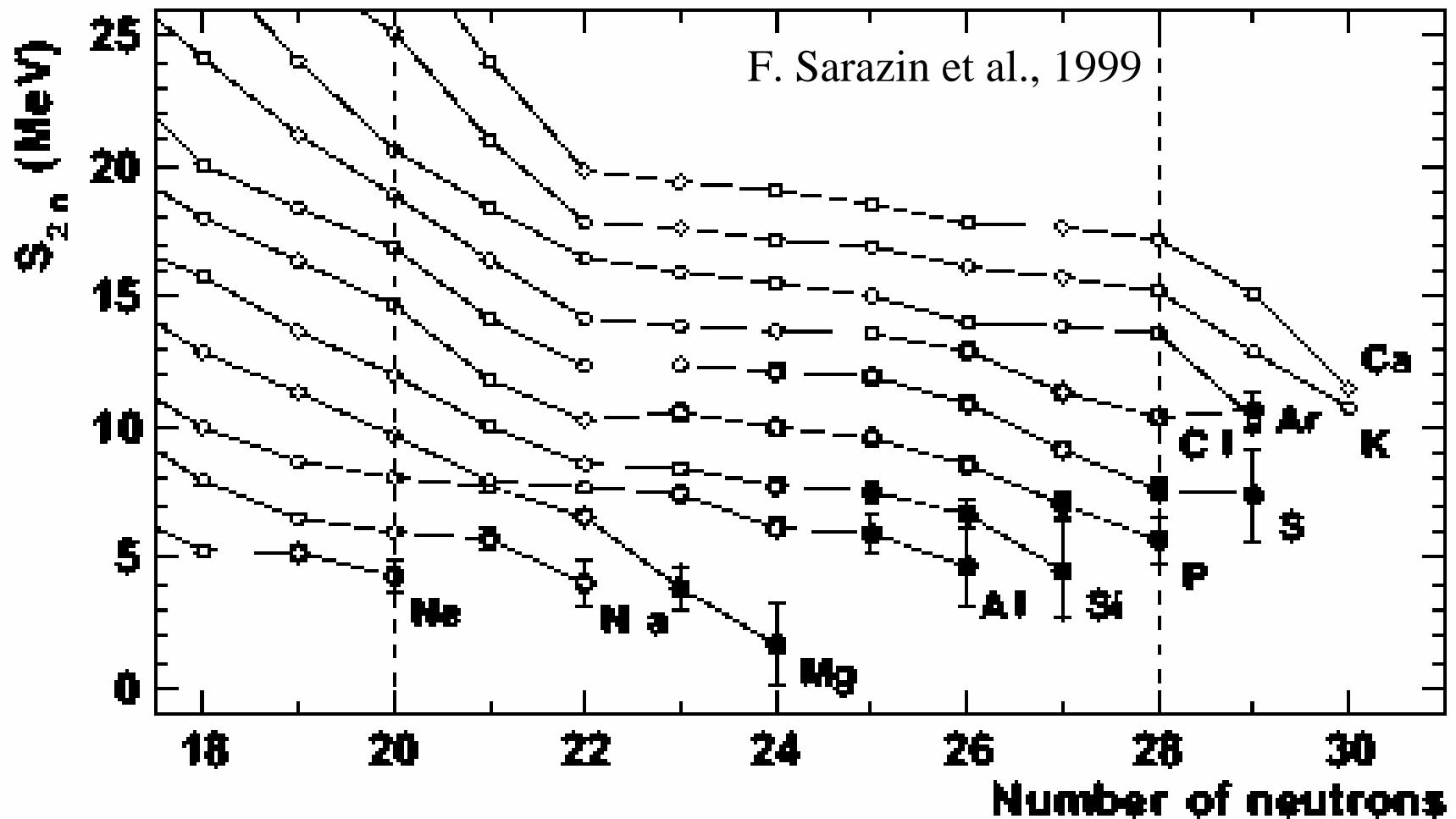
SPEG

time-of-flight
+ magnetic rigidity
 $m = q B \rho T / L$

Resolving power: 10^4
extremely sensitive

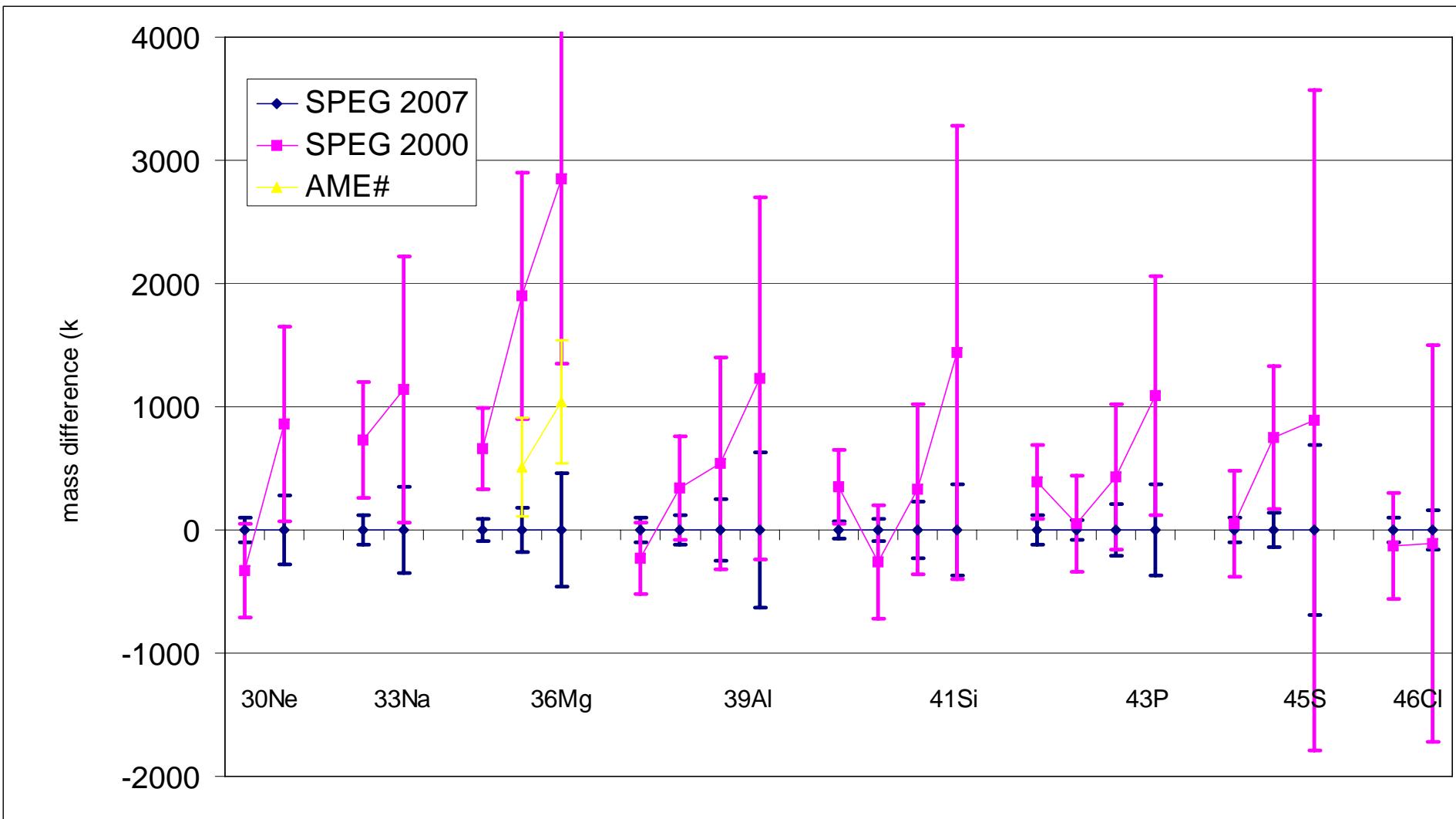


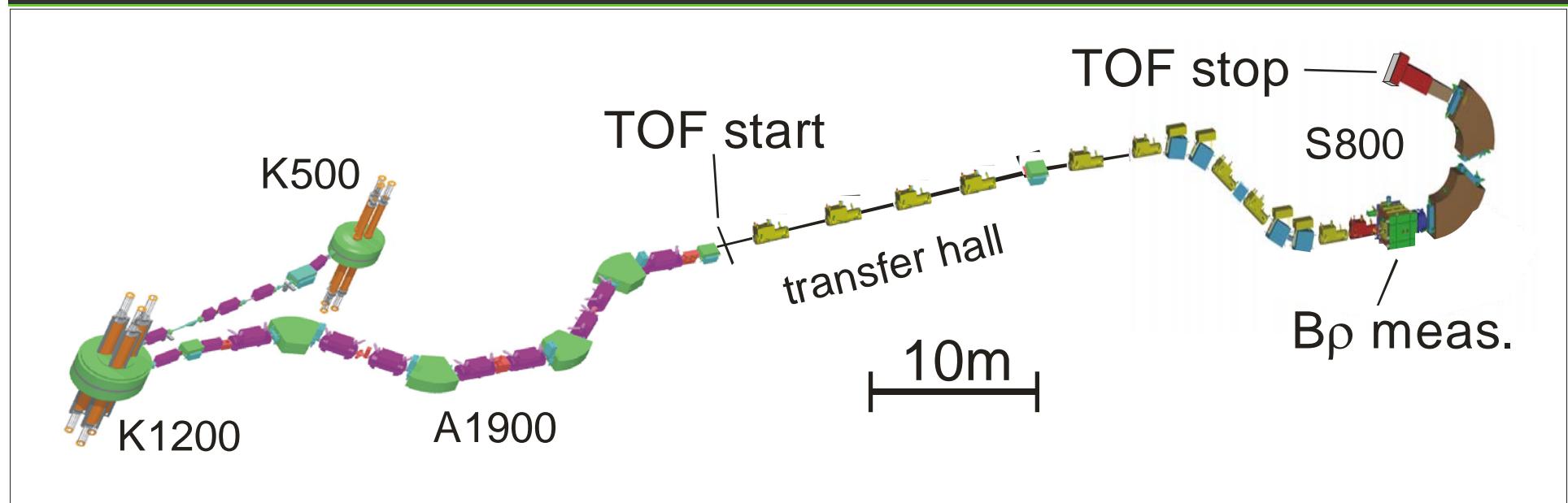
B. Jurado, H. Savajols *et al.*, PLB (2007)



SPEG

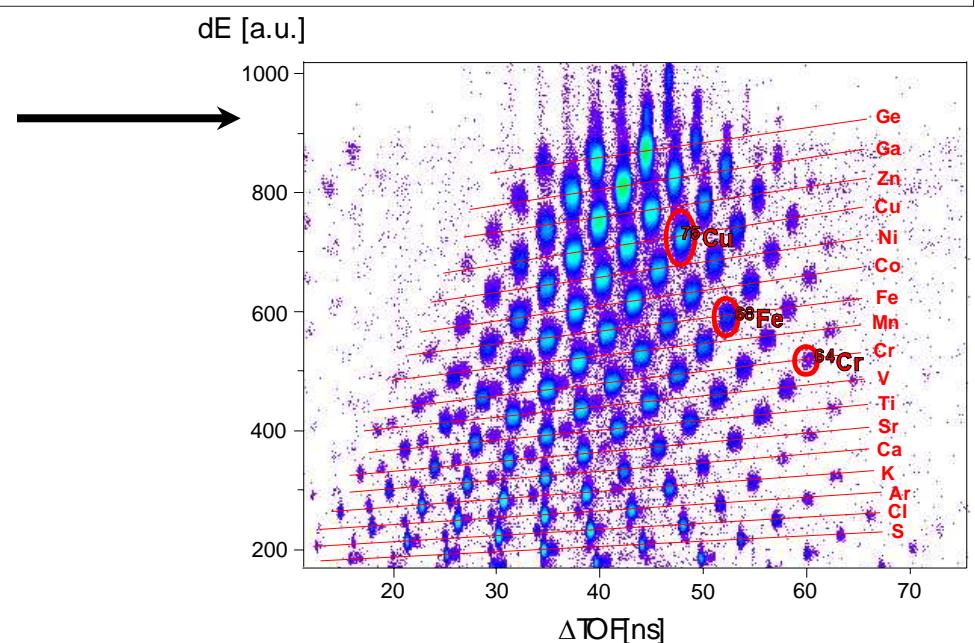
resolving ~ 5000
sensitivity ~ 0.01 /s





M. Matoš (CGS-12, Notre Dame)
AIP Conf. Proc. 819 (2006) 164

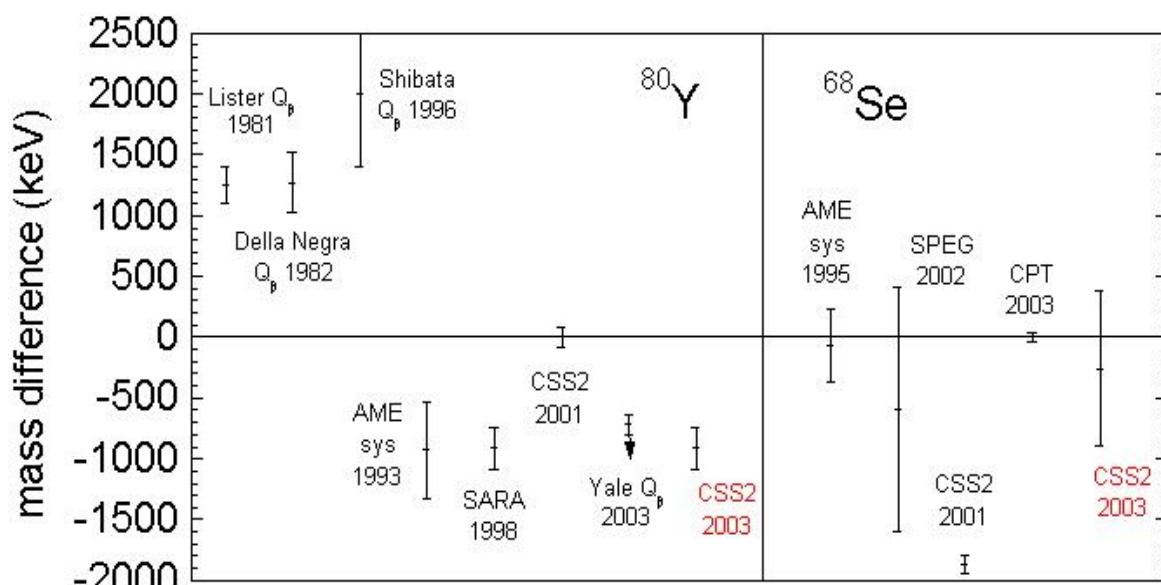
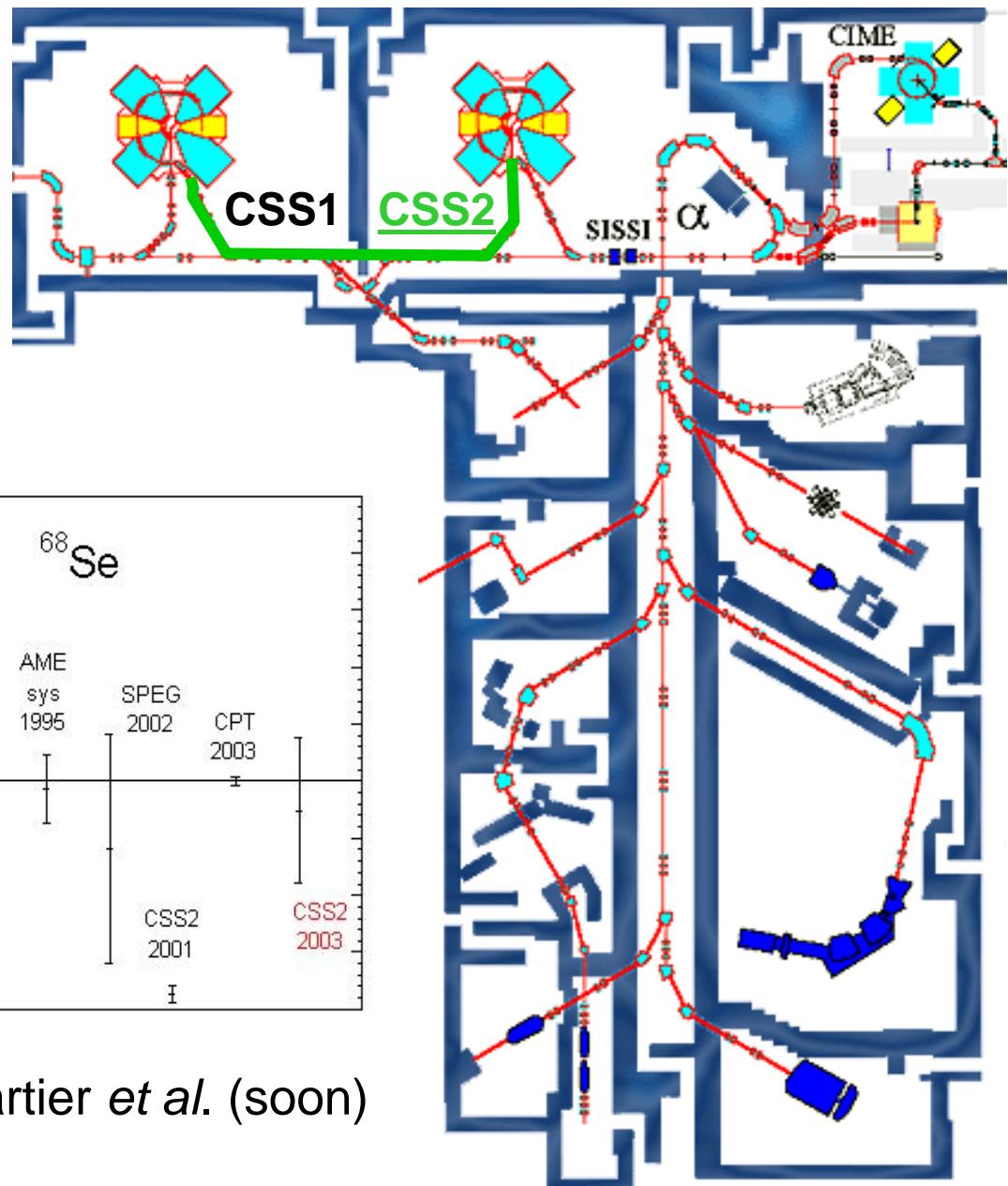
A. Estrade (NiC-IX, CERN)
Proceedings of Science (2006)



mass measurement programs at *GANIL*

CSS2

time-of-flight:
phase difference
with acceleration
(longer flight path)

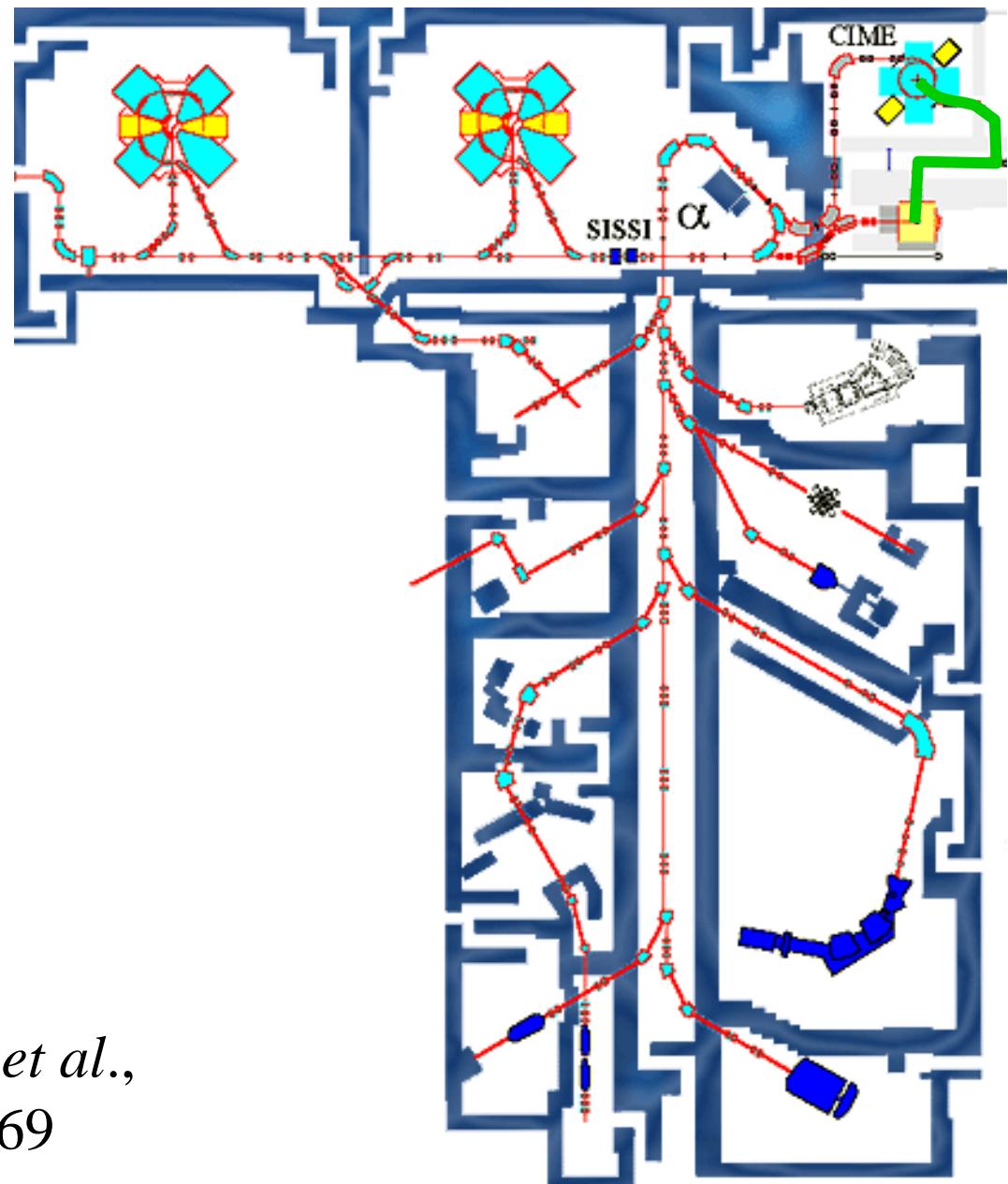
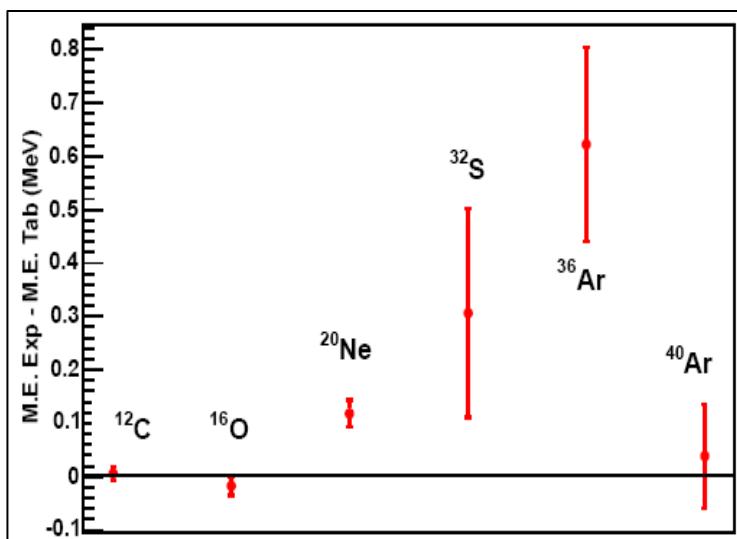


M.B. Gomez Hornillos, M. Chartier *et al.* (soon)

mass measurement programs at *GANIL*

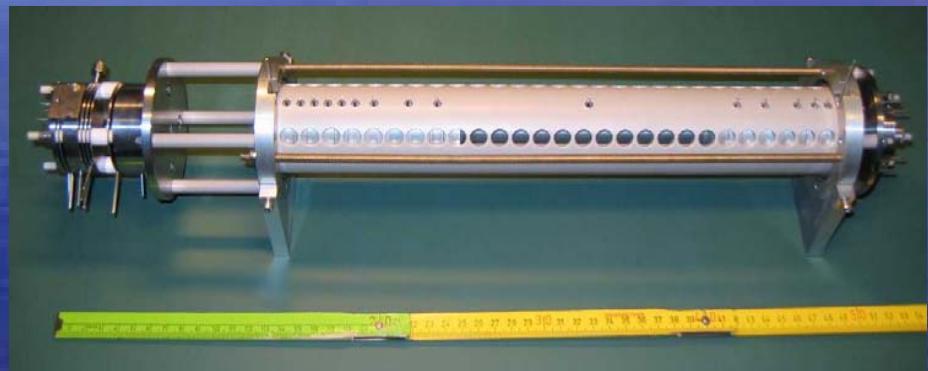
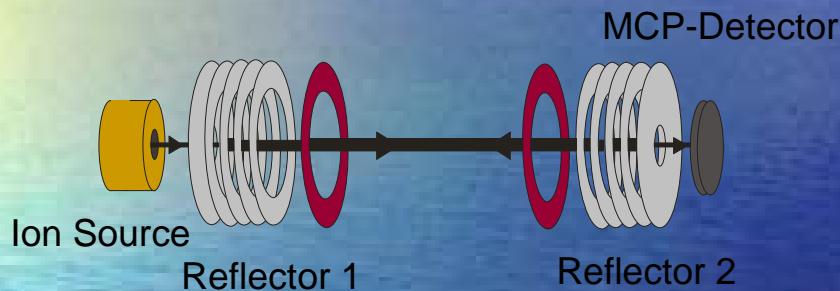
CIME (SPIRAL)

time-of-flight:
variable RF
acceleration



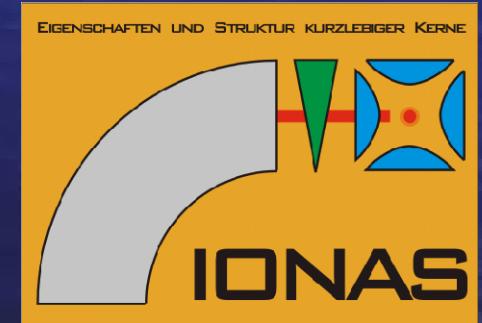
M.-B. Gomes Hornillos *et al.*,
J. Phy. G 31 (2005) S1869

Multiple-Reflection TOF-MS

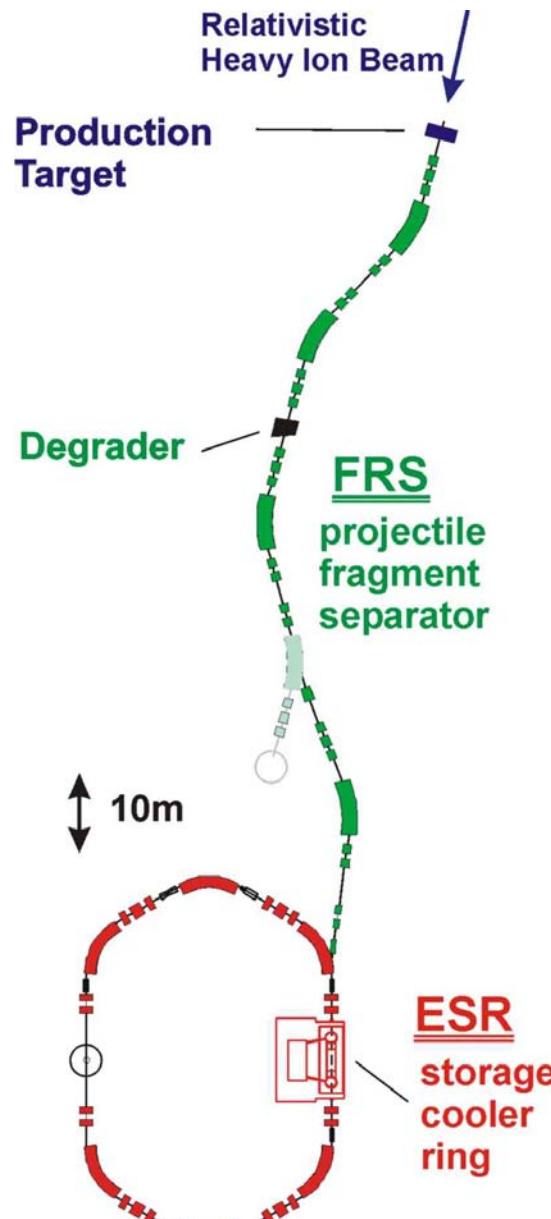


mass measurement accuracy (\sim ppm)
short measurement durations (< 1 ms)

Casares, Geissel, Plass, Scheidenberger, Wollnik *et al.*
(*Proc. 48th ASMS Conf. Mass Spectrom. Allied Topics*, Long Beach, CA, 2000)



mass measurement programs at GSI



Experimental Storage Ring:

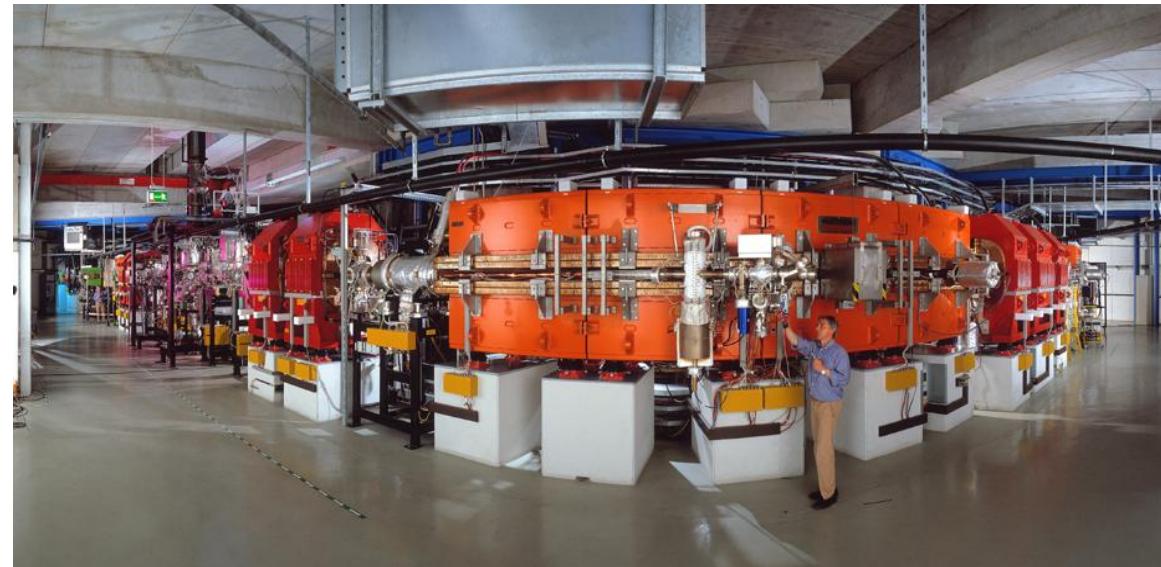
$$\Delta m/m = \gamma_t^2 \Delta f/f + (\gamma_t^2 - \gamma^2) \Delta v/v$$

Schottky Mode

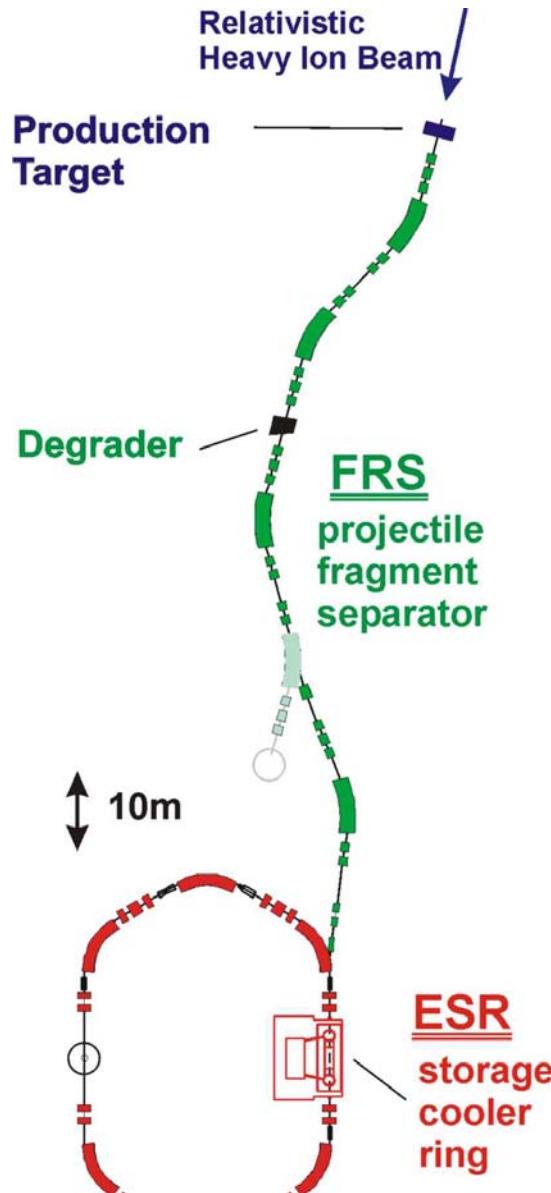
very precise
but cooling slow

Isochronous Mode

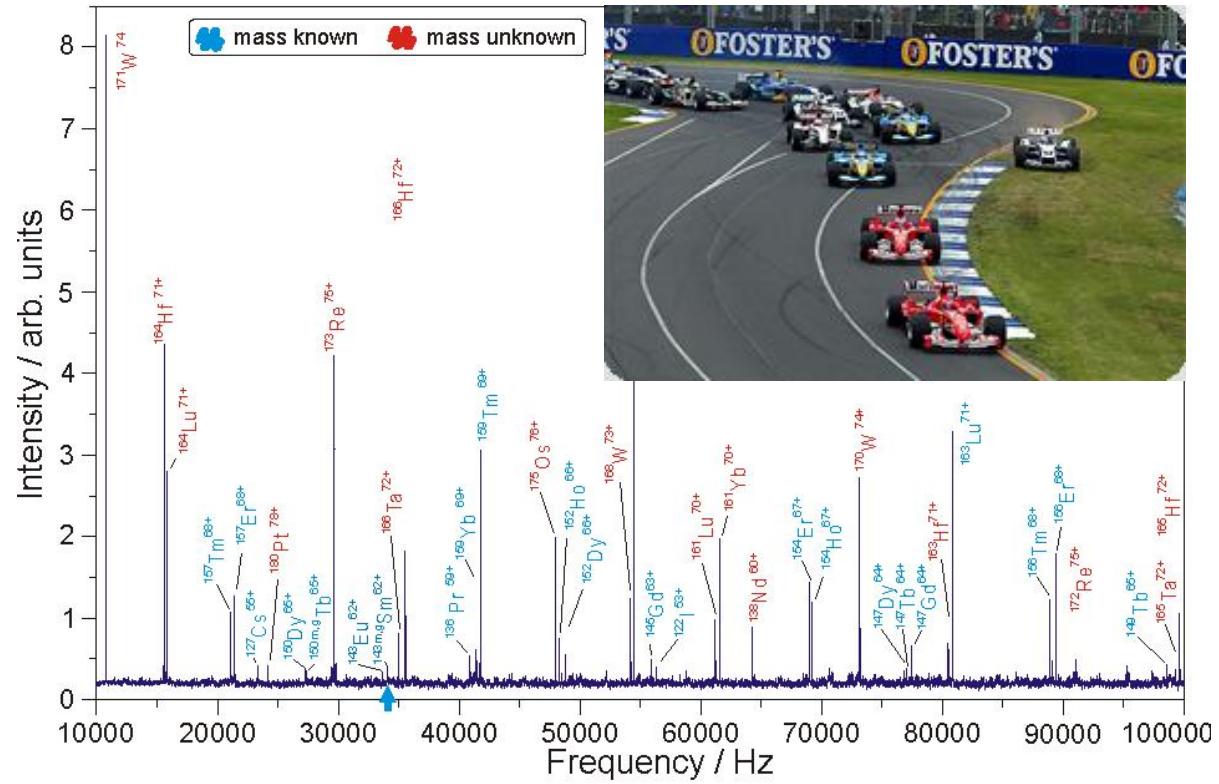
very fast
but not so precise



mass measurement programs at GSI



Experimental Storage Ring:
stripped, H- and He-like ions



Nuclear Physics in Storage Rings

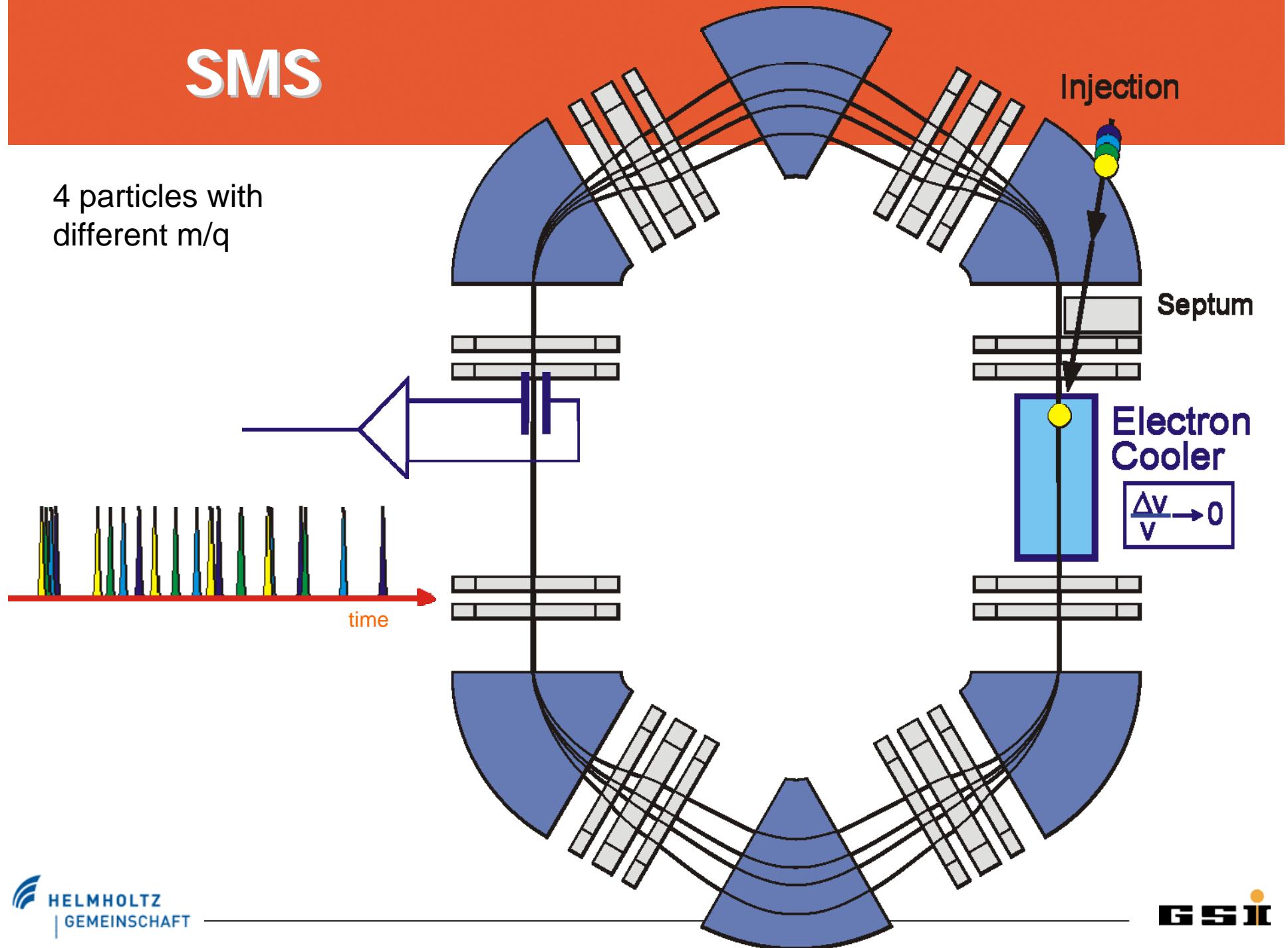
Mass Measurements and Decay Studies in the ESR
Reaction studies in the ESR

Yuri A. Litvinov
Arbeitstreffen Kernphysik, Schleching
22 February 2007

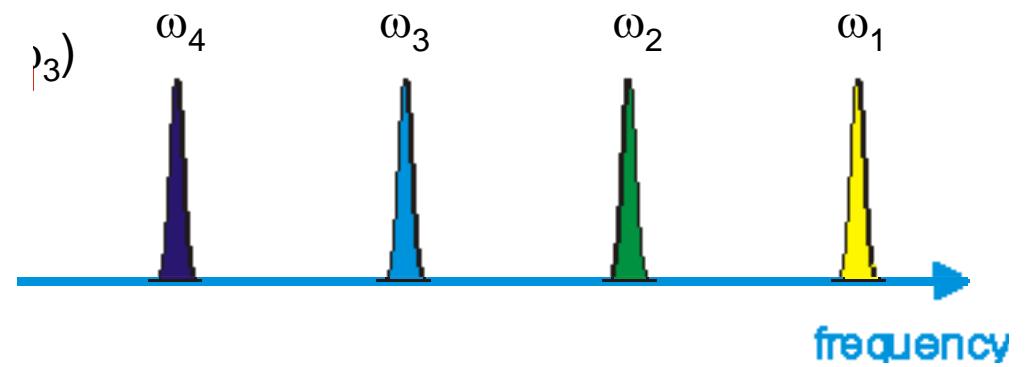
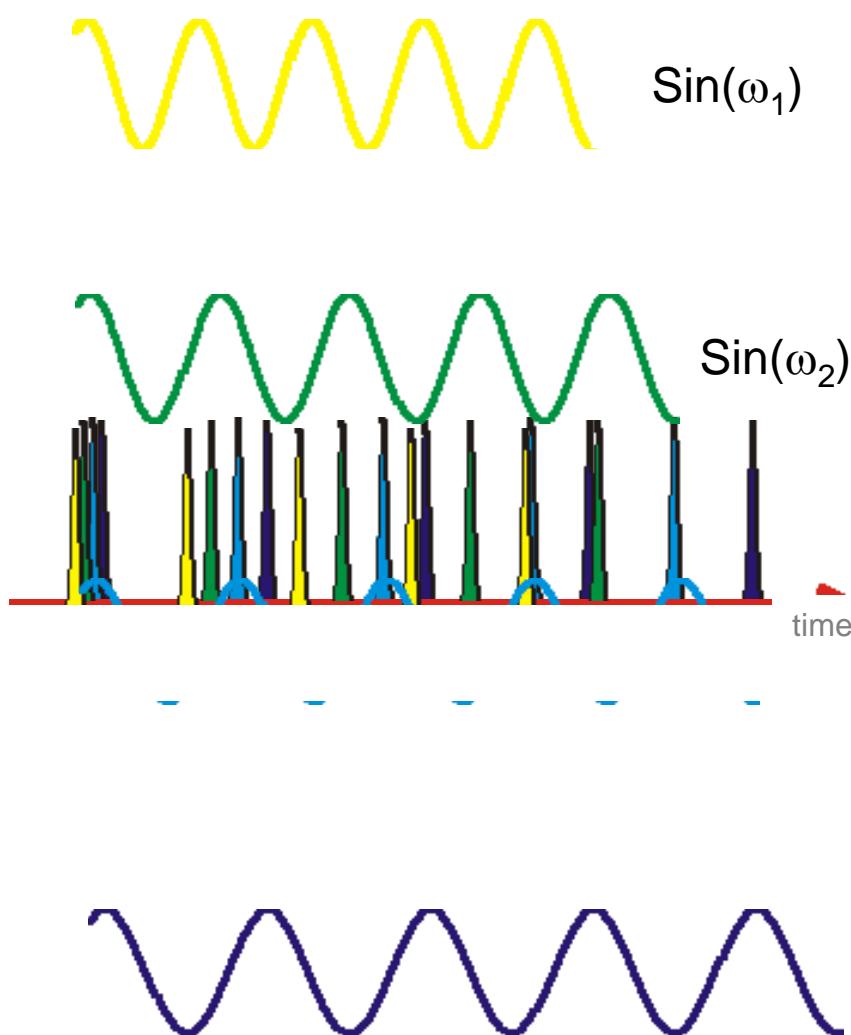
**Mass
matters !**



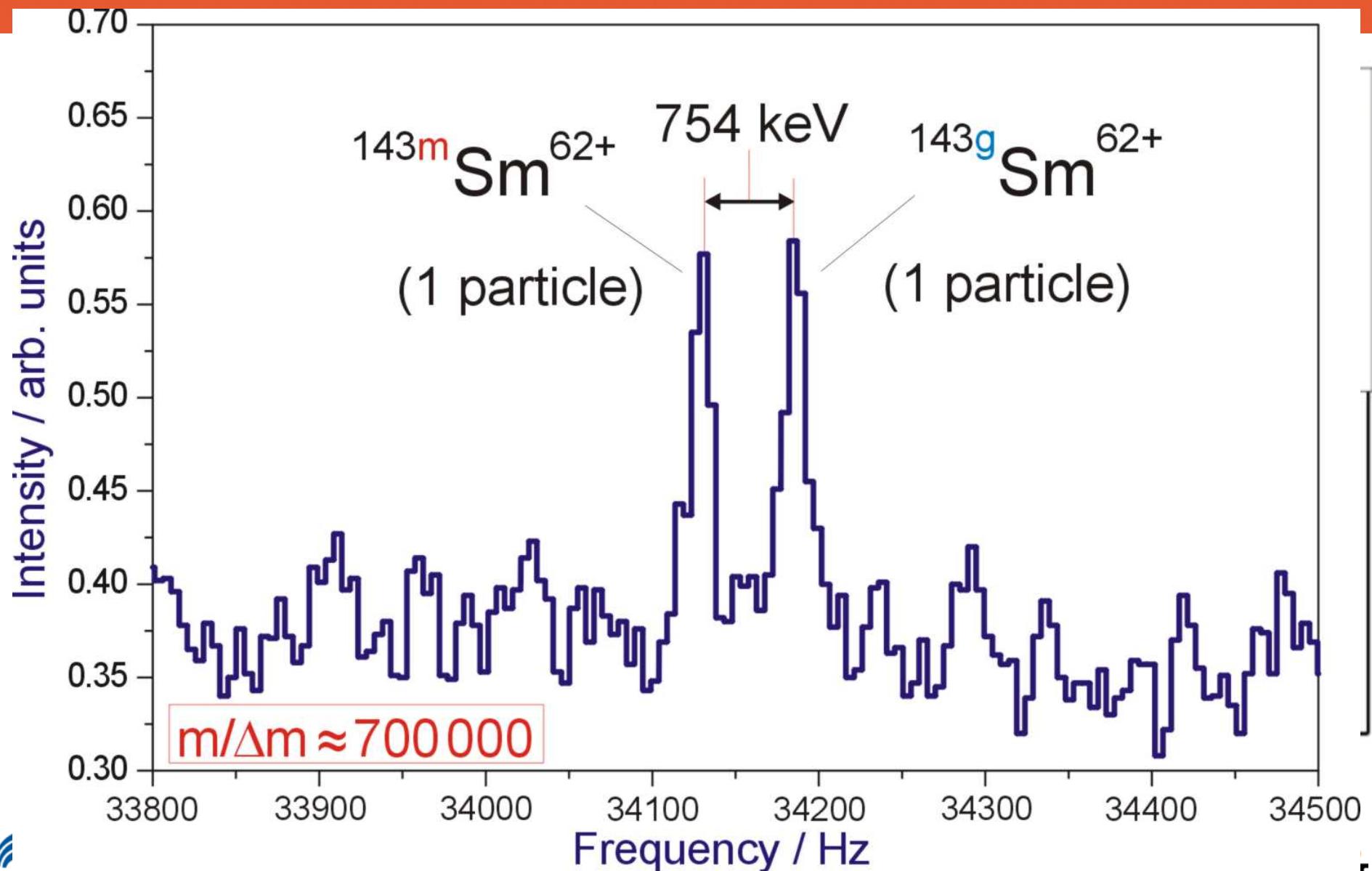
SMS



SMS

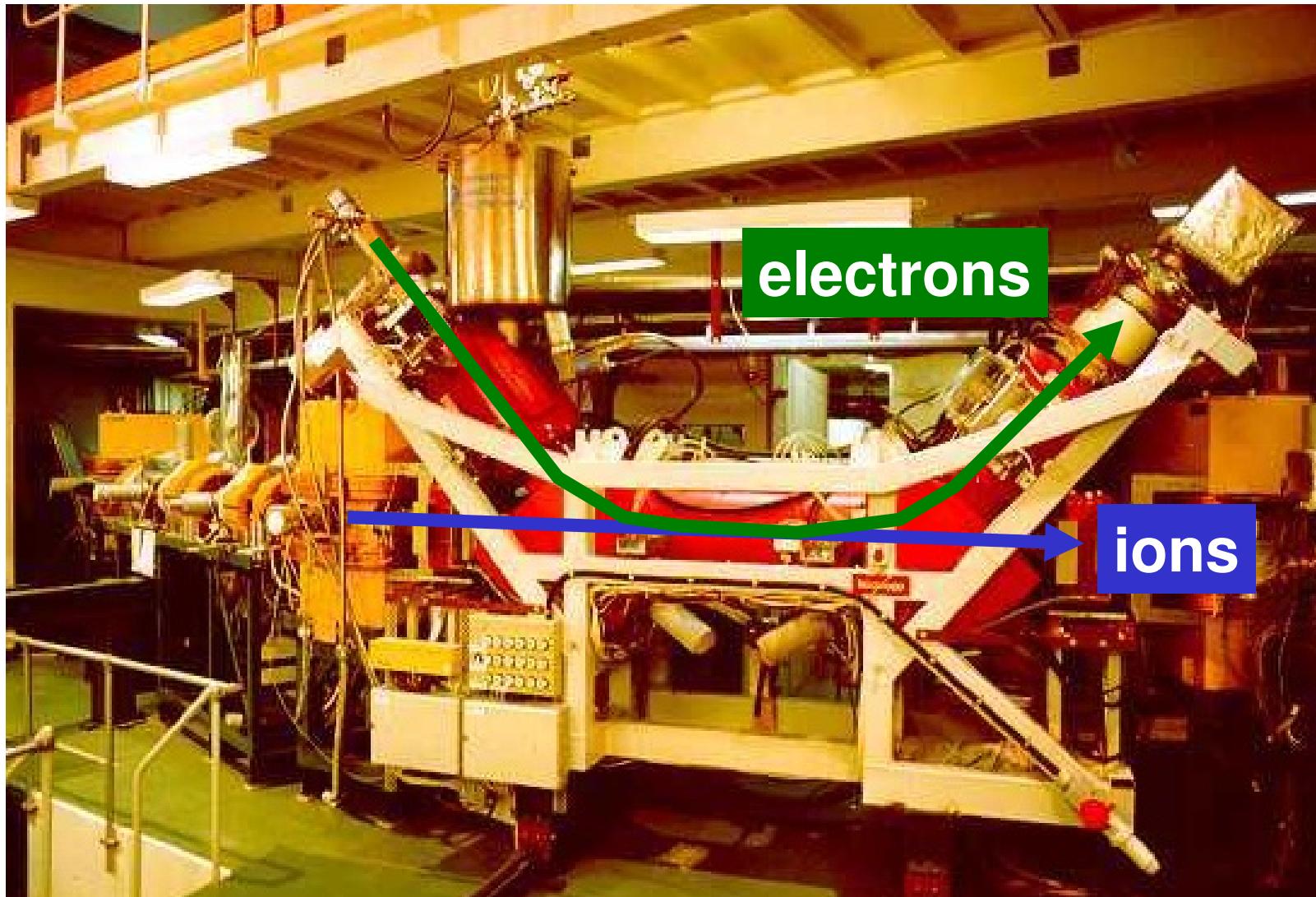


Broad-band Schottky Frequency Spectra



GEMEINSCHAFT



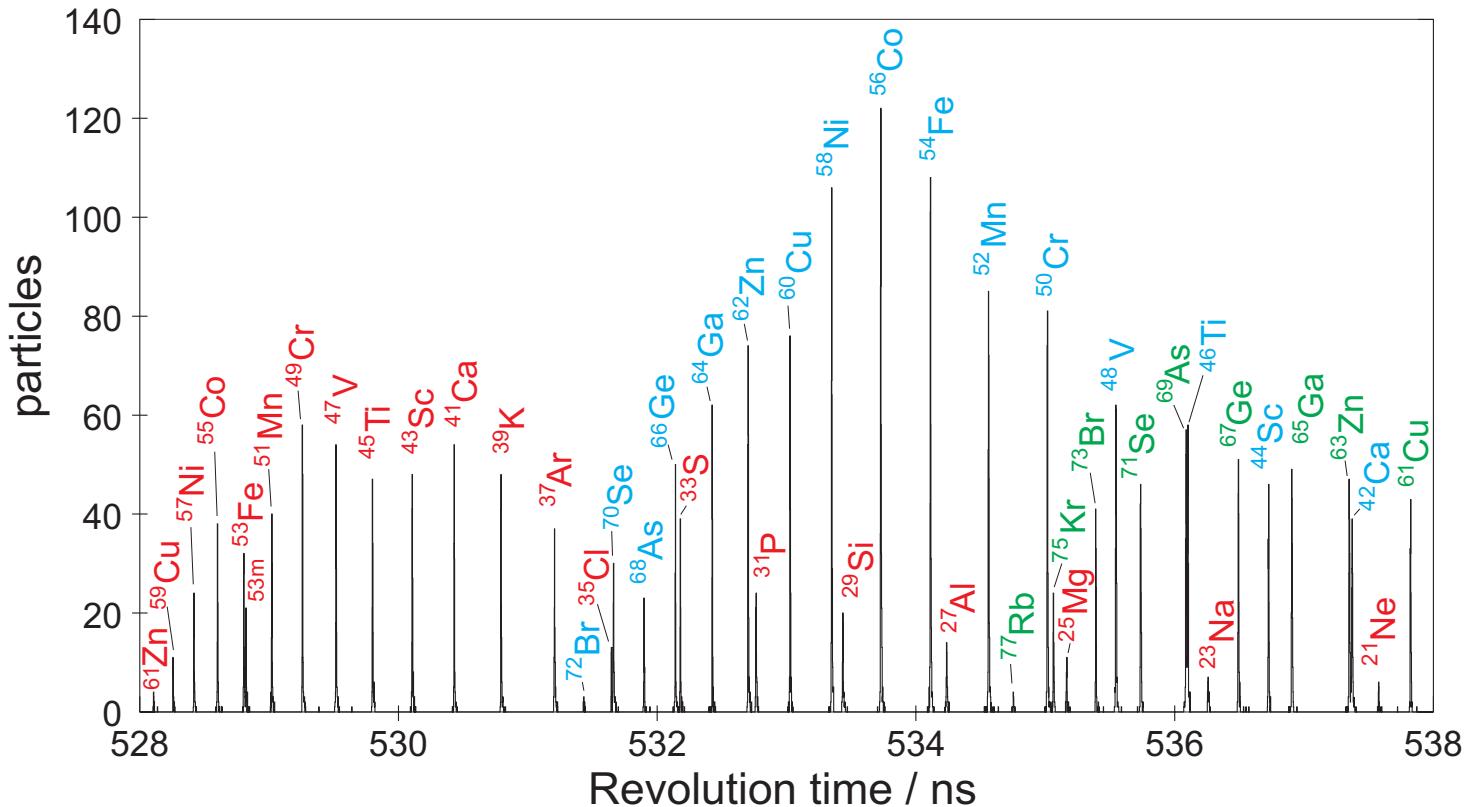


Electron cooling of fast ion beams (CRYRING at MSI, Stockholm)

IMS: Time-of-Flight Spectra

Nuclei with half-lives as short as 20 microseconds are accessible

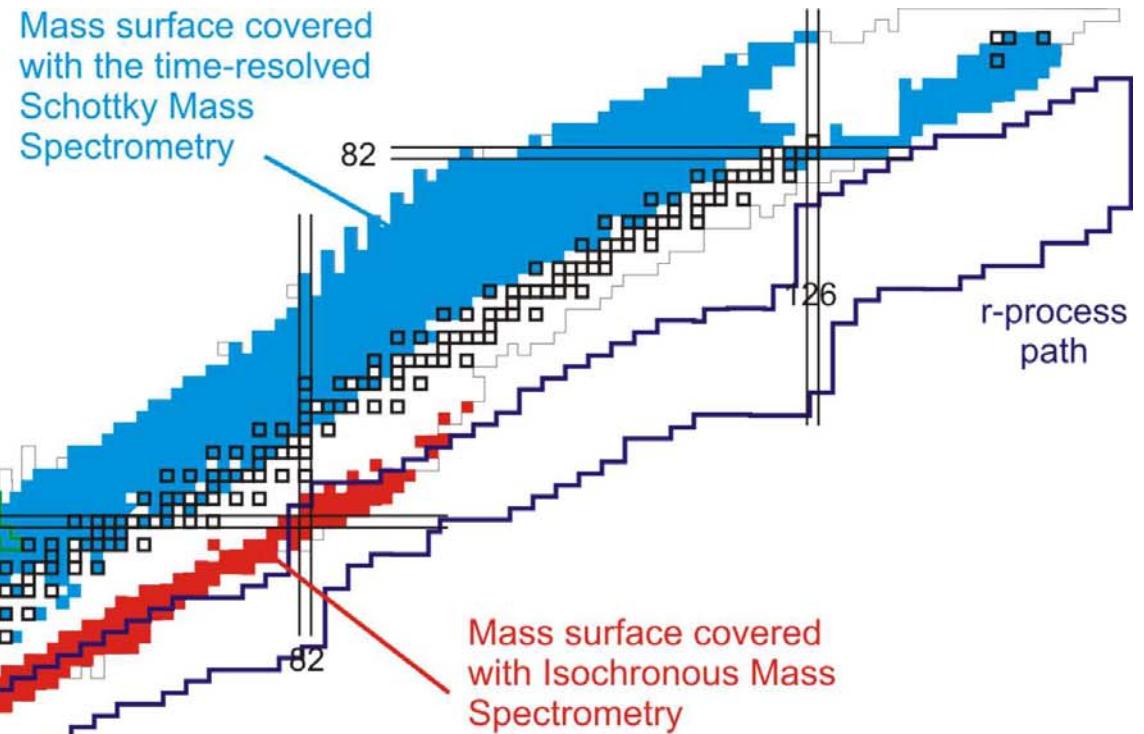
About 13% in mass-over-charge range



M. Hausmann et al., Hyperfine Interactions 132 (2001) 291

Measured Mass Surface

Masses of more than 1100 Nuclides were measured
Mass accuracy:
SMS $1.5 \cdot 10^{-7}$ up to $4 \cdot 10^{-8}$
IMS $\sim 1 \cdot 10^{-6}$
Results: ~ 350 new masses
In addition more than 300 improved mass values



Present Knowledge of Atomic Masses

■ stable nuclei

■ nuclides with known masses

G.Audi et al., Nucl. Phys. A729 (2003) 3

■ nuclides with known masses

G.Audi et al., Nucl. Phys. A595 (1995) 409

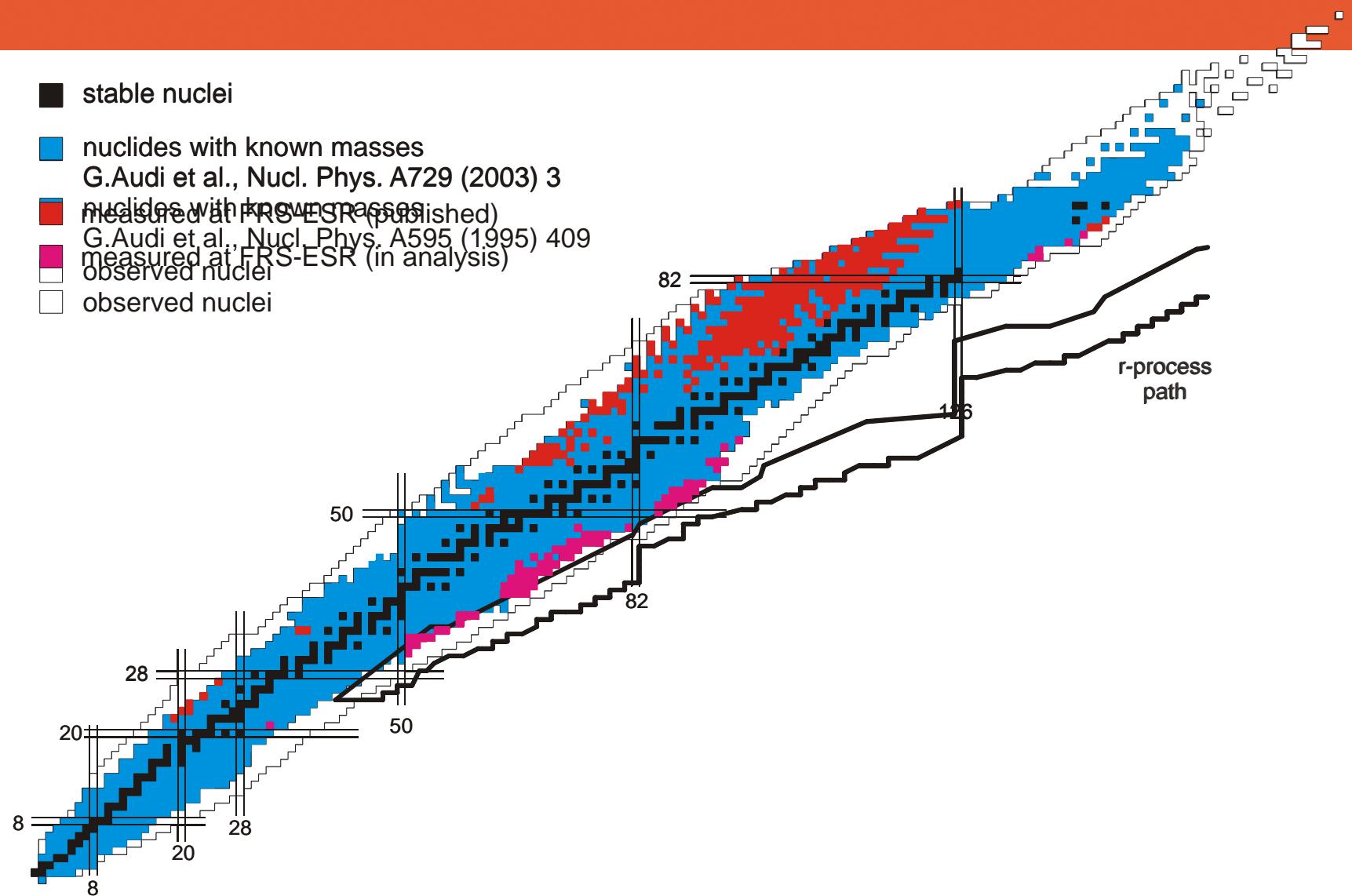
■ measured at FRS-ESR (published)

G.Audi et al., Nucl. Phys. A595 (1995) 409

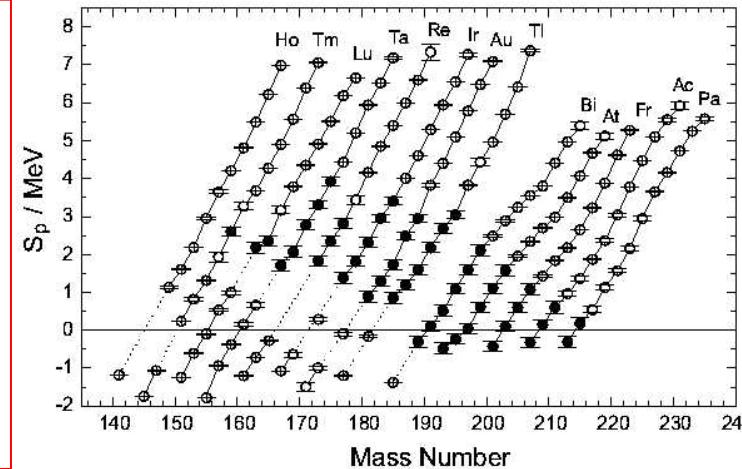
■ measured at FRS-ESR (in analysis)

■ observed nuclei

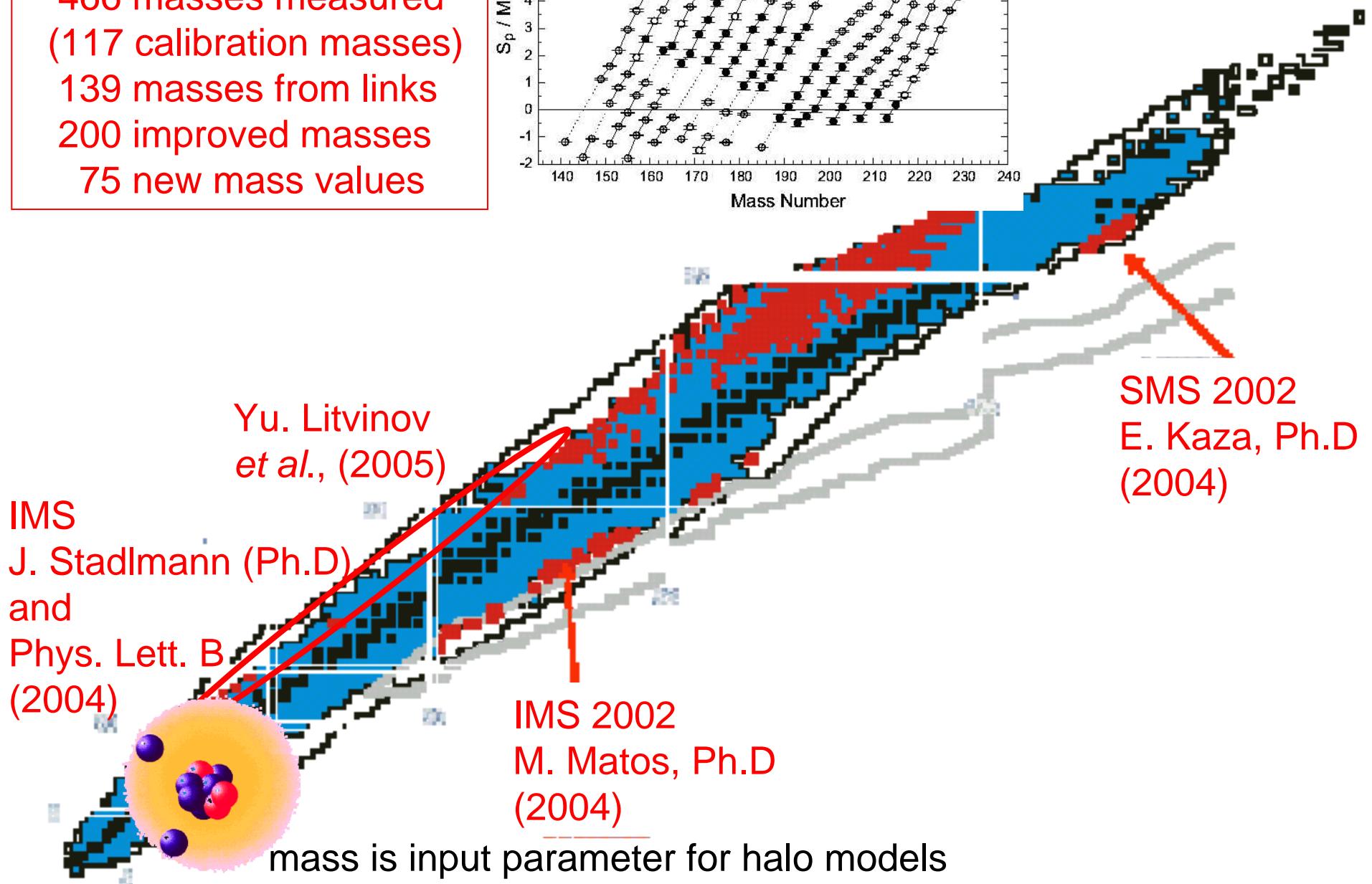
■ observed nuclei



Yu. Litvinov, Ph.D. (2003):
~ 600 species in the ring
466 masses measured
(117 calibration masses)
139 masses from links
200 improved masses
75 new mass values

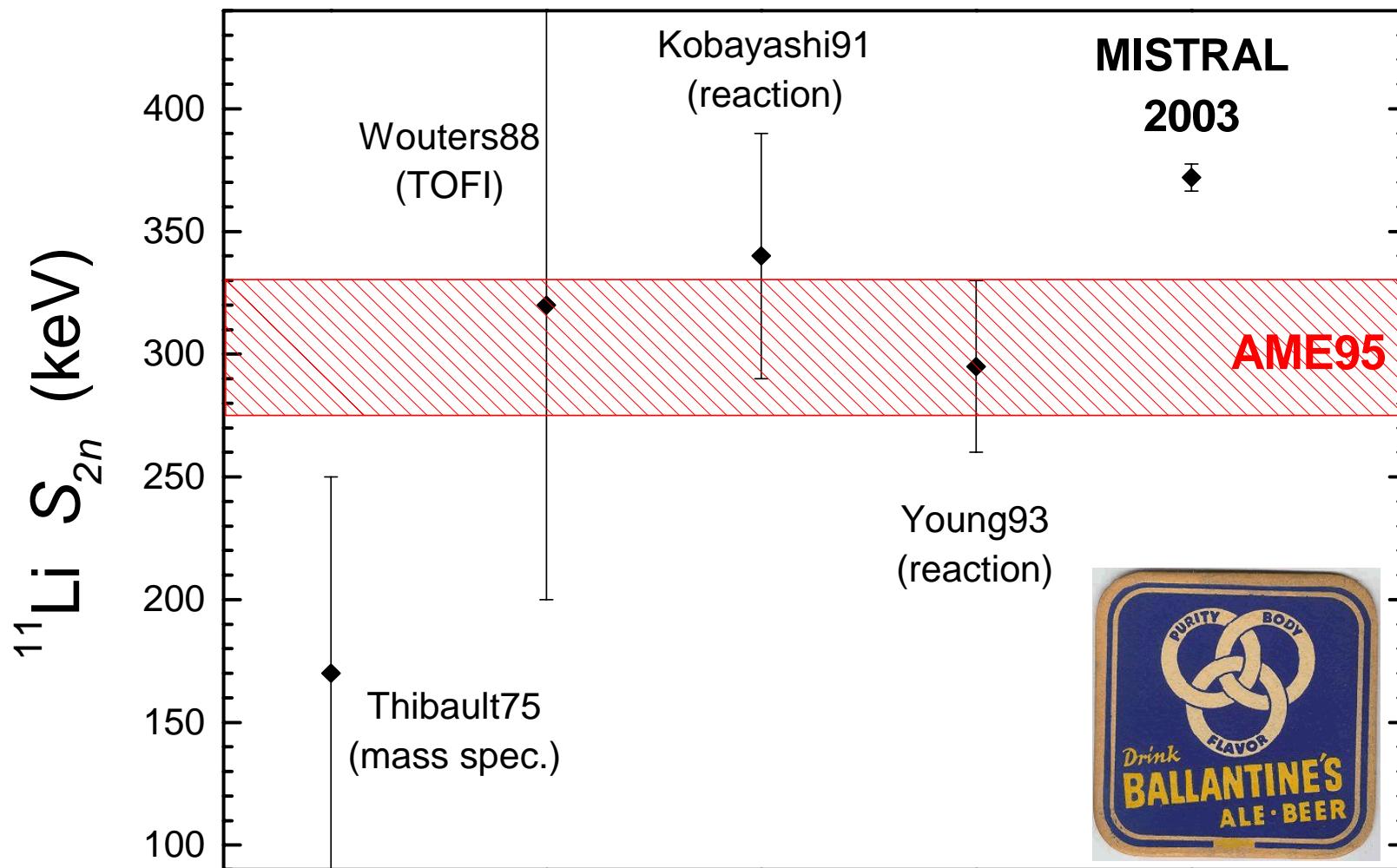


Yu. Novikov *et al.*,
Nucl Phys A (2002)

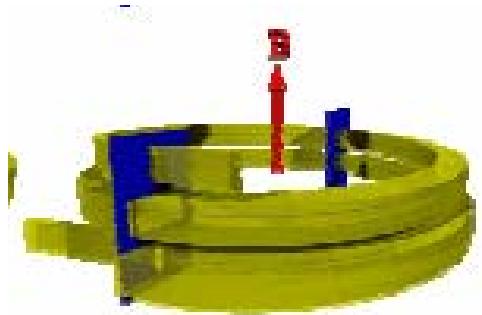




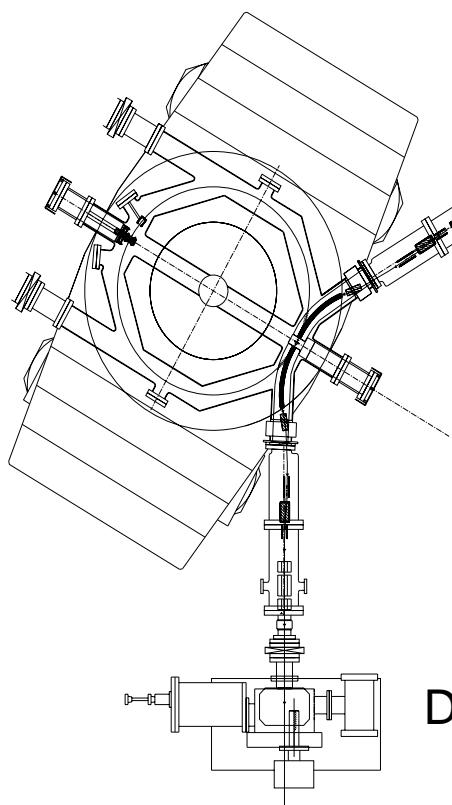
A new binding energy for the ^{11}Li halo



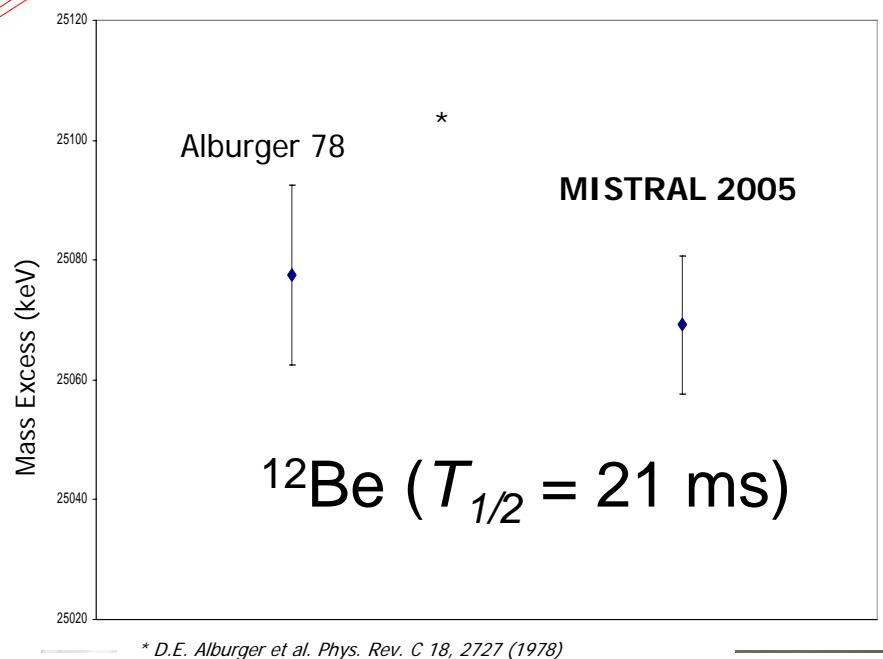
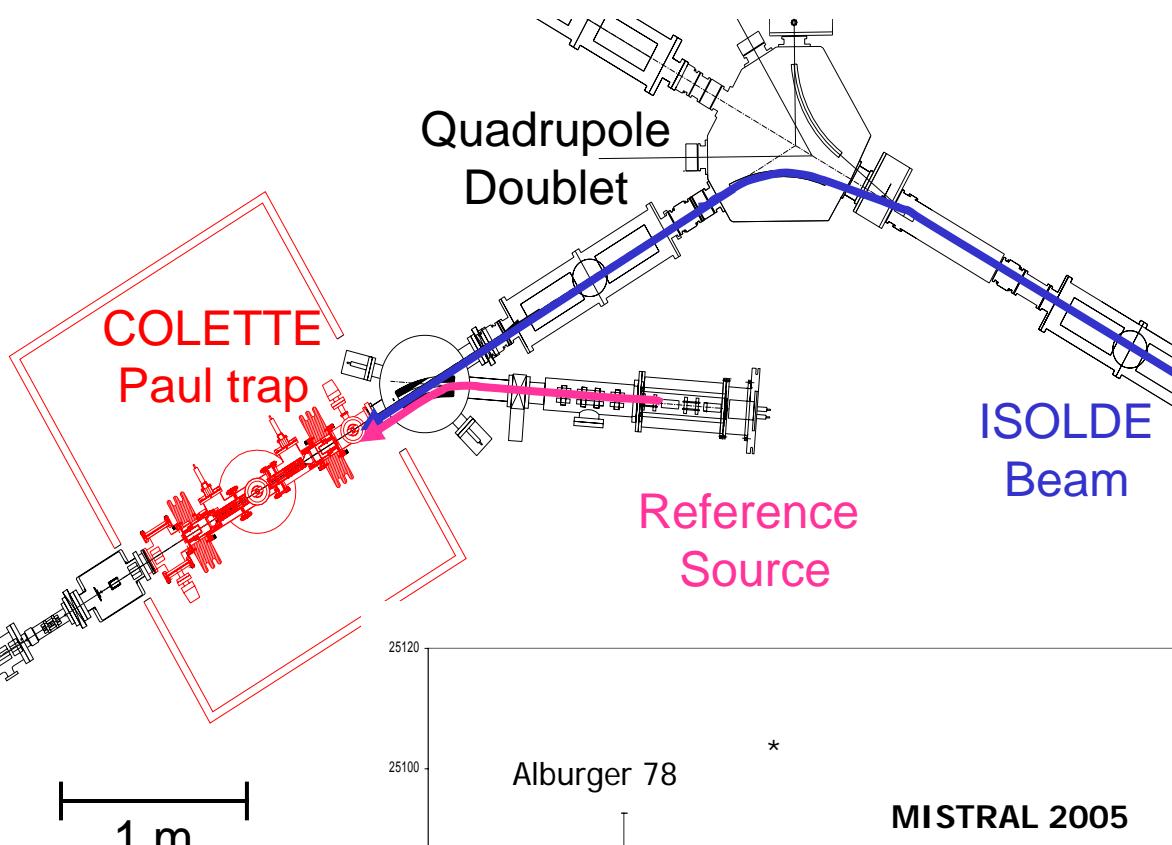
23% higher than currently used to adjust models...

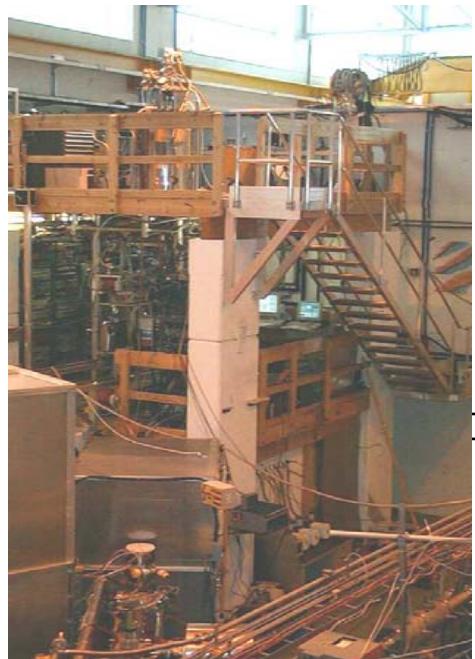


MISTRAL



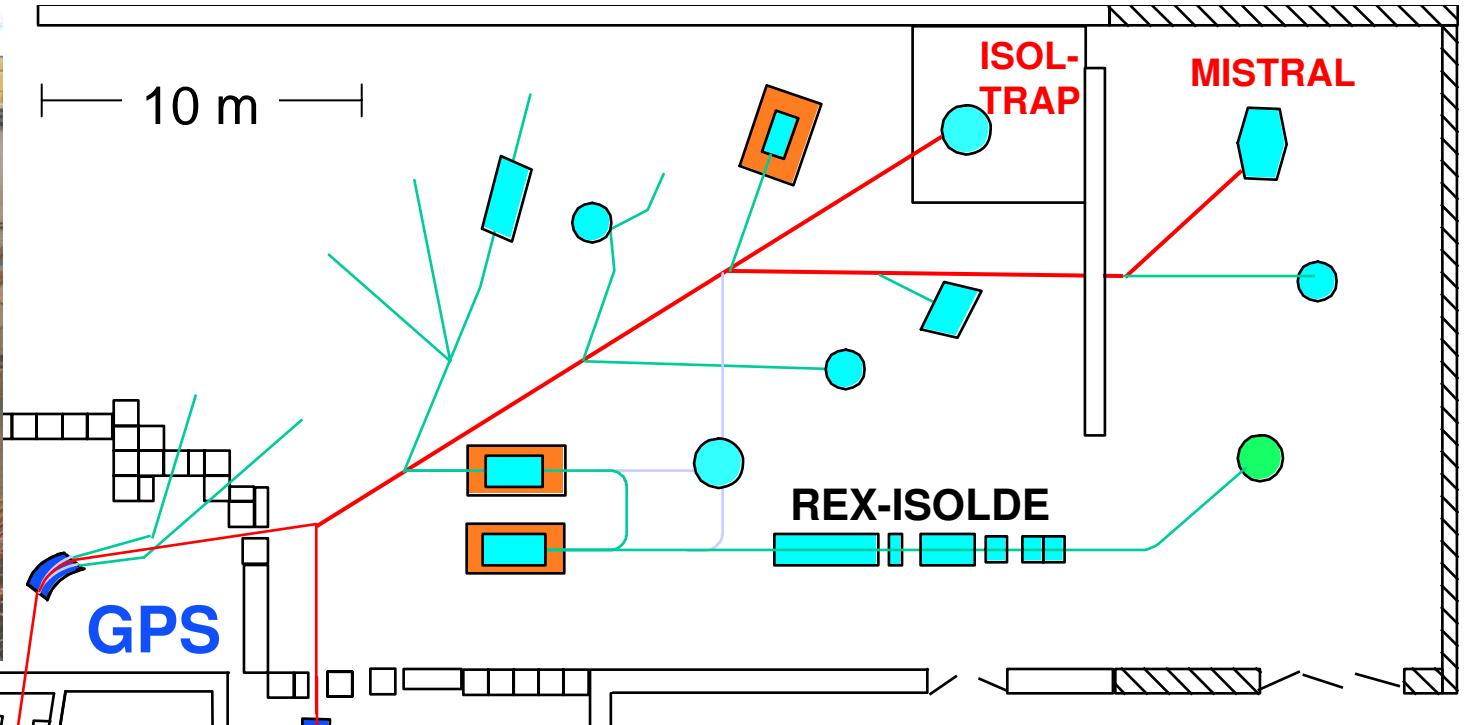
Detector



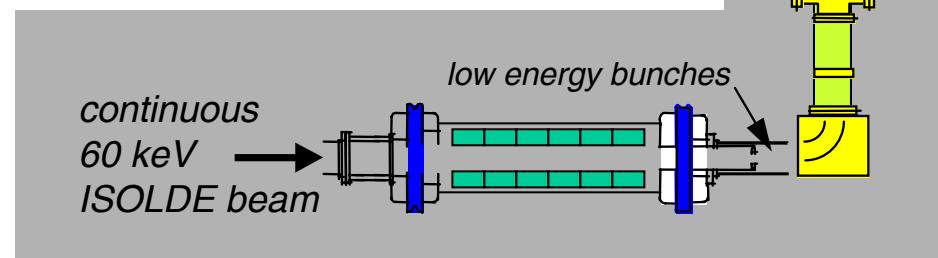
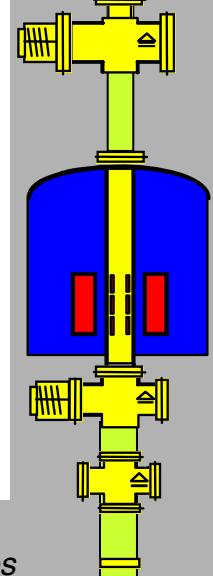
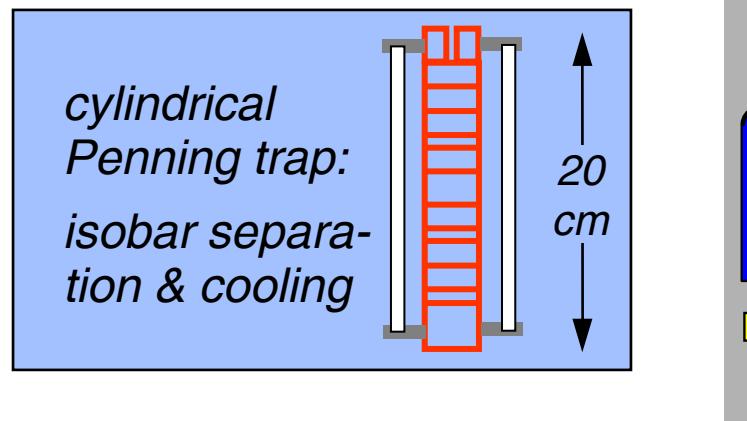
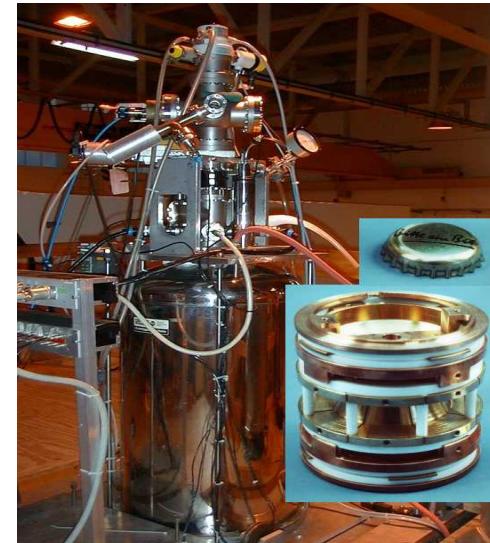
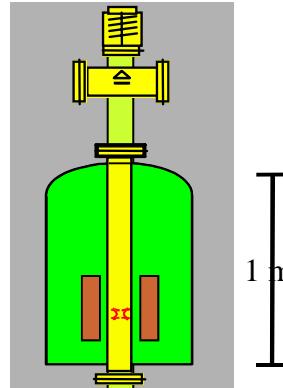
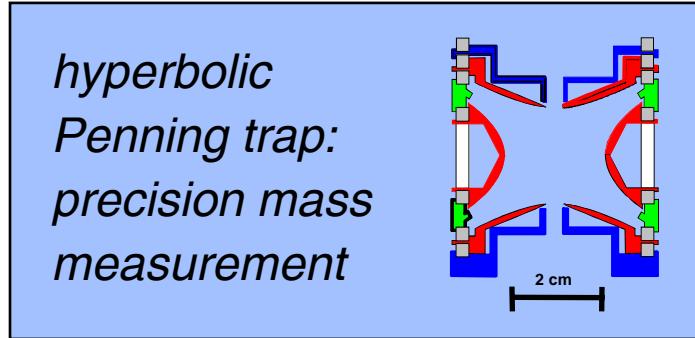


proton beam
1 GeV

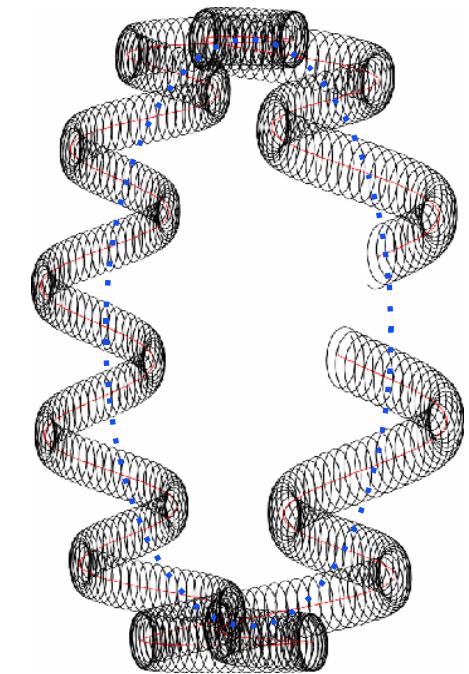
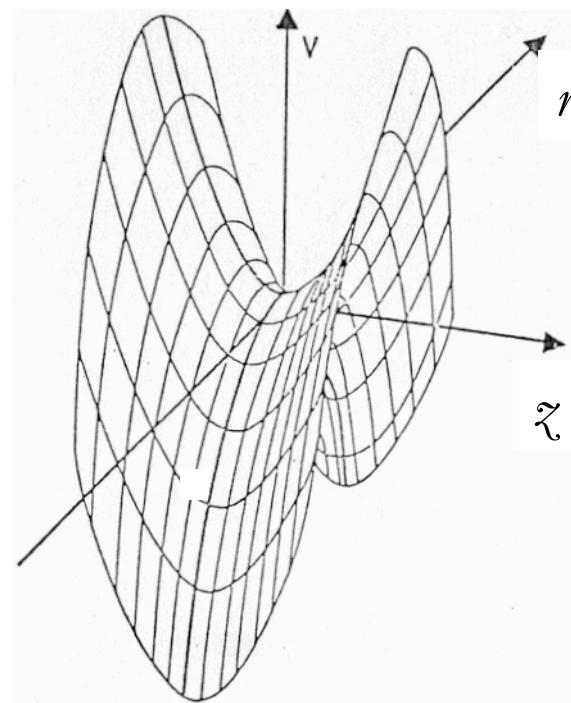
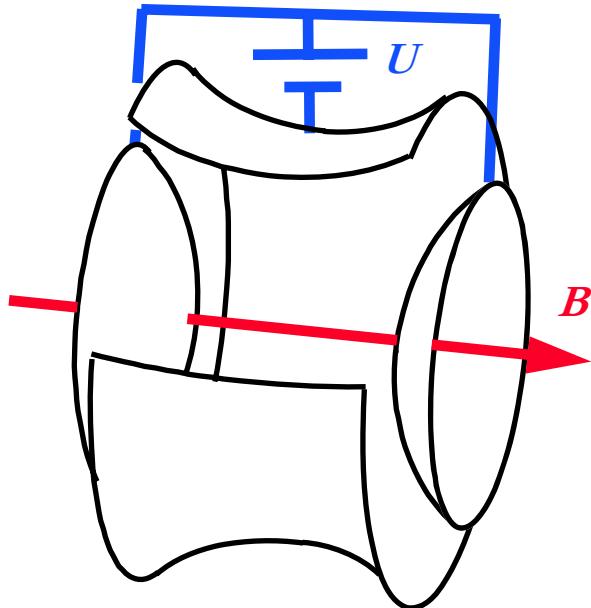
ISOLDE
CERN, Geneva



The mass spectrometer **ISOLTRAP**



Penning Trap



$$\omega_c = qB/2\pi m$$

ω_z SHM

mass independent

$$\omega_c = \omega_+ + \omega_-$$

in a quadrupole field

Nucleosynthesis in neutrino heated matter: The νp -process and the r-process

G. Martinez-Pinedo^a, A. Kelić, K. Langanke, K.-H. Schmidt

Gesellschaft für Schwerionenforschung,

D-64291 Darmstadt, Germany

E-mail: g.martinez@gsi.de

D. Mocelj, C. Fröhlich, F.-K. Thielemann, I. Panov, T. Rauscher, M. Liebendörfer

Department of Physics and Astronomy, University of Basel

Klingelbergstrasse 82, CH-4056 Basel, Switzerland

N. T. Zinner

Institute for Physics and Astronomy, University of Århus,

DK-8000 Århus C, Denmark

B. Pfeiffer

Institute for Nuclear Chemistry, University of Mainz

Fritz-Straßmann-Weg 2, D-55128 Mainz, Germany

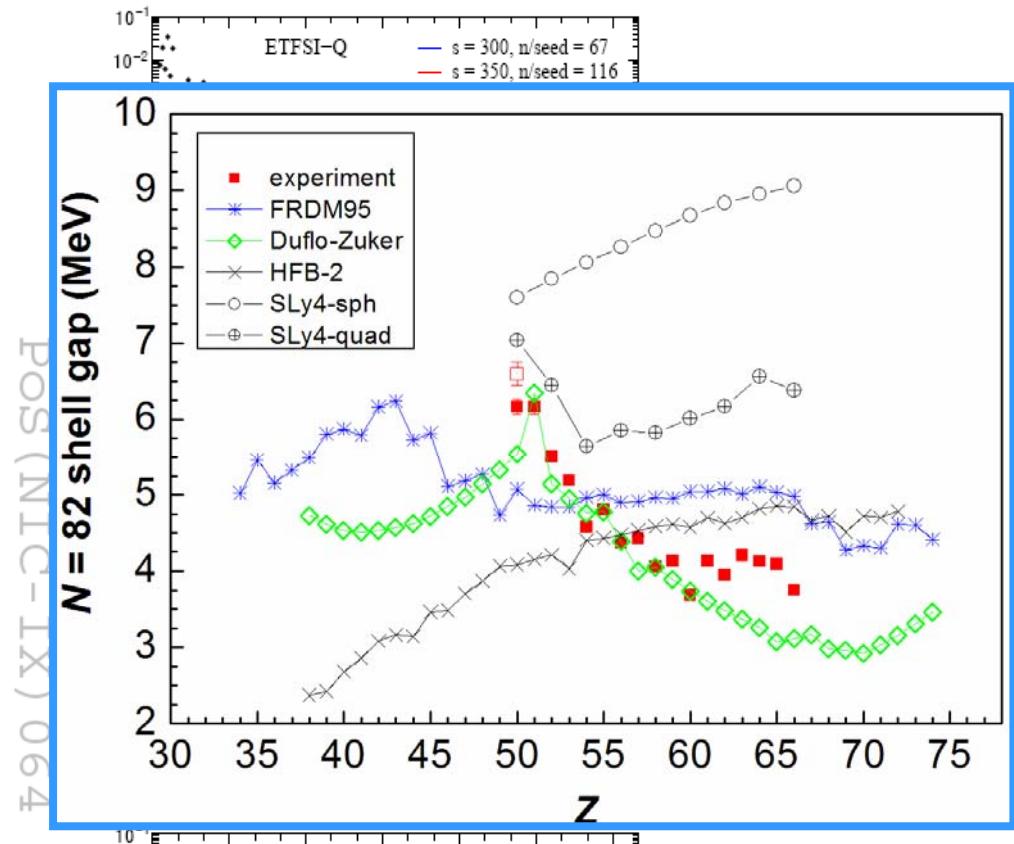
R. Buras and H.-Th. Janka

Max-Planck-Institut für Astrophysik, Karl-Schwarzschild-Strasse 1,

D-85741 Garching, Germany

This manuscript reviews recent progress in our understanding of the r- and heavy elements in supernovae. Recent hydrodynamical models of supernovae show that a large amount of proton rich matter is ejected under strong shock waves. This matter constitutes the site of the νp -process where antineutrino absorption drives the nucleosynthesis of nuclei with $A > 64$. Supernovae are also responsible for the synthesis of the heaviest elements in nature. Fission and alpha decay play a major role in determining the final abundance pattern and in explaining features seen in metal-poor r-process-rich stars.

International Symposium on Nuclear Astrophysics - Nuclei in the Cosmos -
25-30 June 2006
CERN



APS/123-QED

Restoration of the $N = 82$ shell gap from direct mass measurements of $^{132,134}\text{Sn}$

M. Dworschak^{1*}, G. Audi², K. Blaum^{1,3}, P. Delahaye⁴, S. George^{1,3}, U. Hager⁵, F. Herfurth¹, A. Herlert⁴, A. Kellerbauer⁶, H.-J. Kluge^{1,7}, D. Lunney², L. Schweikhard⁸, and C. Yazidjian¹

¹*GSI, Planckstraße 1, 64291 Darmstadt, Germany*

²*CSNSM-IN2P3-CNRS, Université de Paris Sud, 91405 Orsay, France*

³*Johannes Gutenberg-Universität, Institut für Physik, 55099 Mainz, Germany*

⁴*CERN, Physics Department, 1211 Geneva 23, Switzerland*

⁵*University of Jyväskylä, Department of Physics, P.O. Box 35 (YFL), 40014 Jyväskylä, Finland*

⁶*Max Planck Institute for Nuclear Physics, P.O. Box 103980, 69029 Heidelberg, Germany*

⁷*Ruprecht-Karls-Universität, Institut für Physik, 69120 Heidelberg, Germany and*

⁸*Ernst-Moritz-Arndt-Universität, Institut für Physik, 17487 Greifswald, Germany*

(Dated: May 8, 2007)

Techniques



Indirect

reactions:



$$Q = M_A + M_a - M_b - M_B$$

decays:



$$Q_\alpha = M_B - M_A$$

Direct

(mass spectrometry)

time of flight:

*SPEG/CSS2, GANIL
ESR, GSI*

cyclotron frequency:

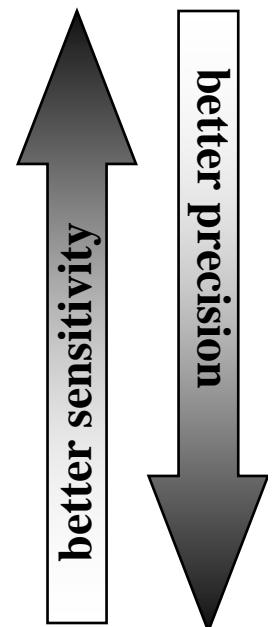
*ISOLTRAP, ISOLDE
MISTRAL, ISOLDE*

*PRODUCTION
SCHEME*

FIFS
(MeV)

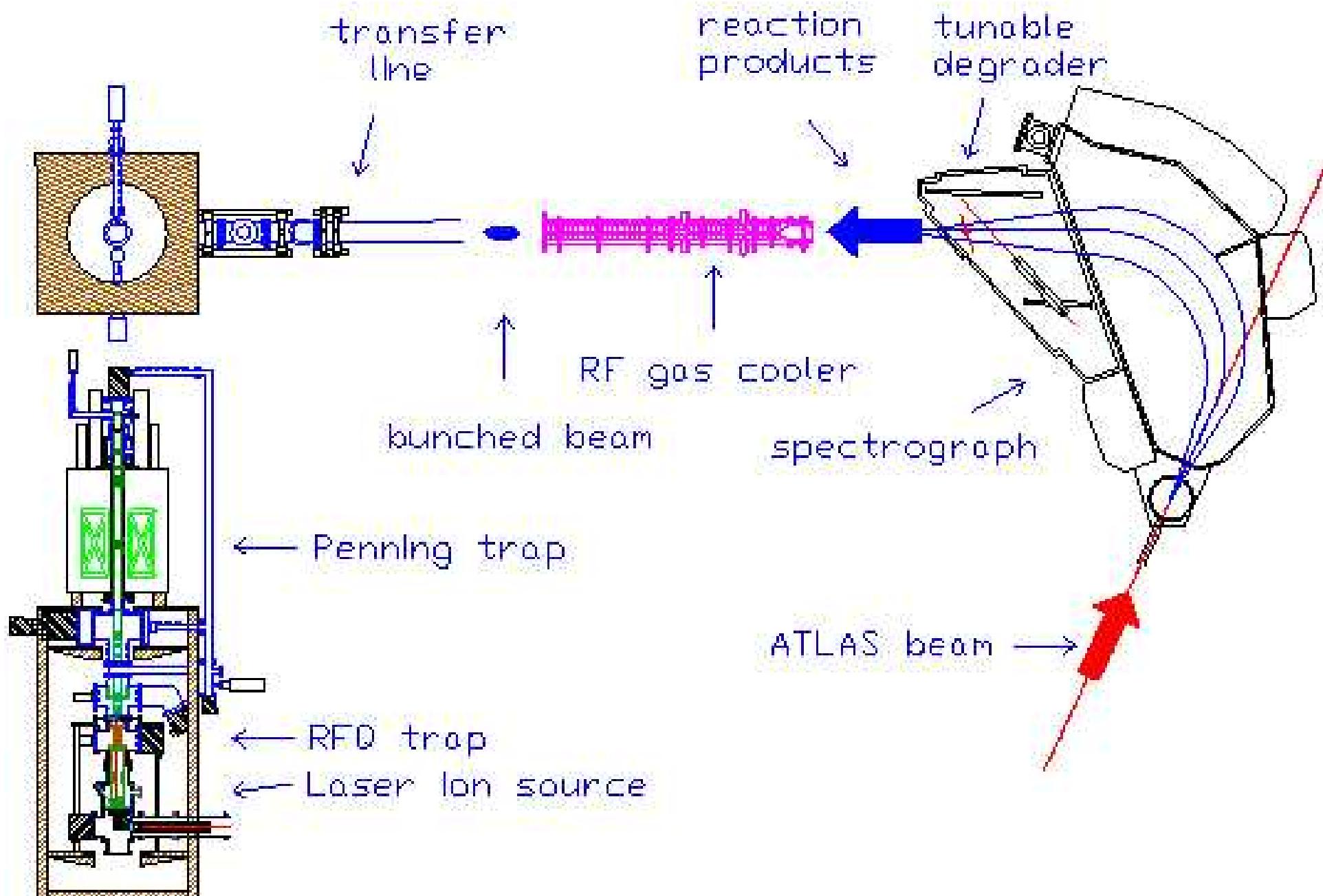
gas cell
RFQ

ISOL
(keV)



'the best of both worlds'
→ *CPT at ANL*

Canadian Penning Trap (CPT) facility at ANL



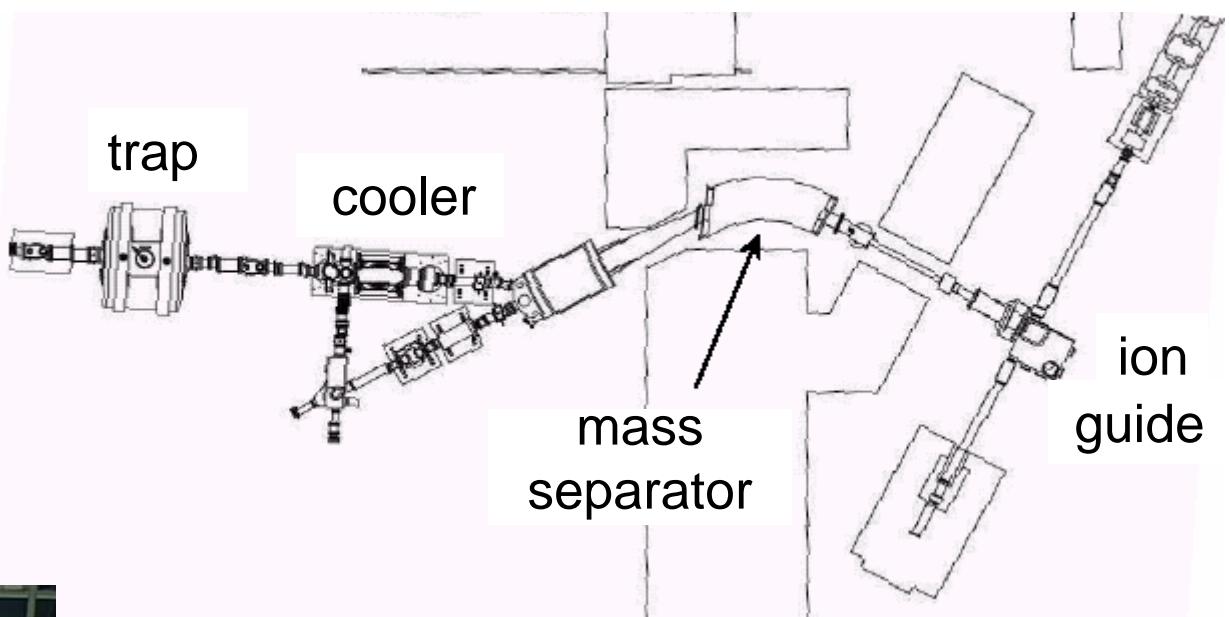


Before there were Backstreet Boys...
Before the other guys got 'N Sync...
Danny, Jordan, Johnny, Donnie and Joey changed the rules...

NEW KIDS ON THE BLOCK
or "what ISOLTRAP hath wrought"



JYFLTRAP at the IGISOL facility in Jyväskylä



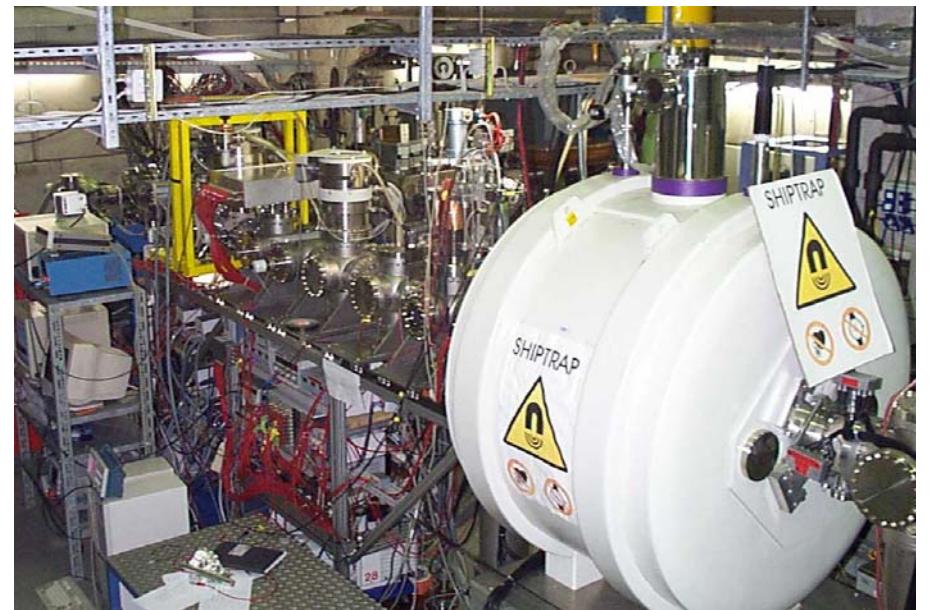
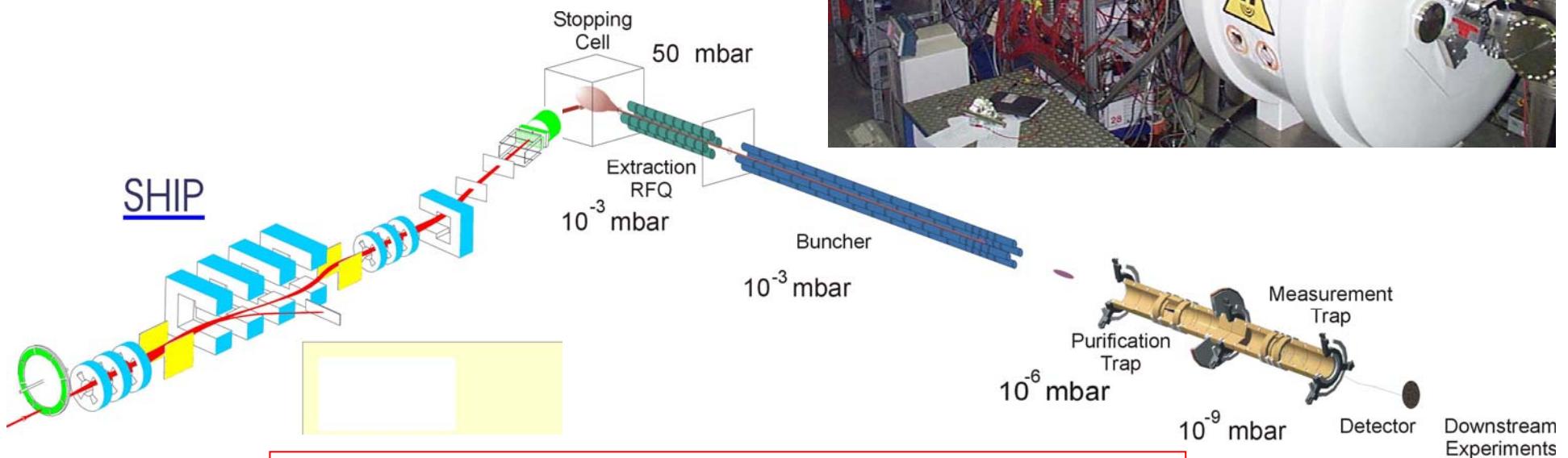
JYFLTRAP masses from IGISOL:
V. Kolhinen, NIMB (2004) & Ph.D.
S. Rinta-Antila et al., PRC (2004)
A. Jokinen, ENAM04 (2004)

H	S. Anttila et al., PRIS (2001) A. Jokinen, ENAM04 (2004)														He
Li	Be														B
Na	Mg														C
K	Ca	Sc	Ti	V	Cr	Mn	Fe	Co	Ni	Cu	Zn	Ga	Ge	As	Se
Rb	Sr	Y	Zr	Nb	Mo	Tc	Ru	Rh	Pd	Ag	Cd	In	Sn	Sb	Te
Cs	Ba	La	Hf	Ta	W	Re	Os	Ir	Pt	Au	Hg	Tl	Pb	Bi	Po
Fr	Ra	Ac													At
LANTHANIDES		Ce	Pr	Nd	Pm	Sm	Eu	Gd	Tb	Dy	Ho	Er	Tm	Yb	Lu
ACTINIDES		Th	Pa	U	Np	Pu	Am	Cm	Bk	Cf	Es	Fm	Md	No	Lr

SHIPTRAP facility at GSI

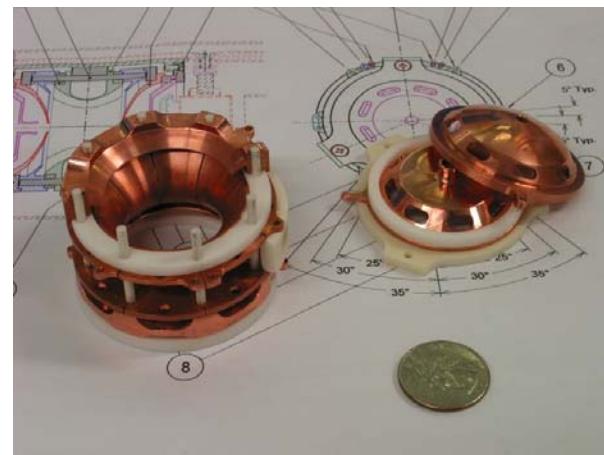
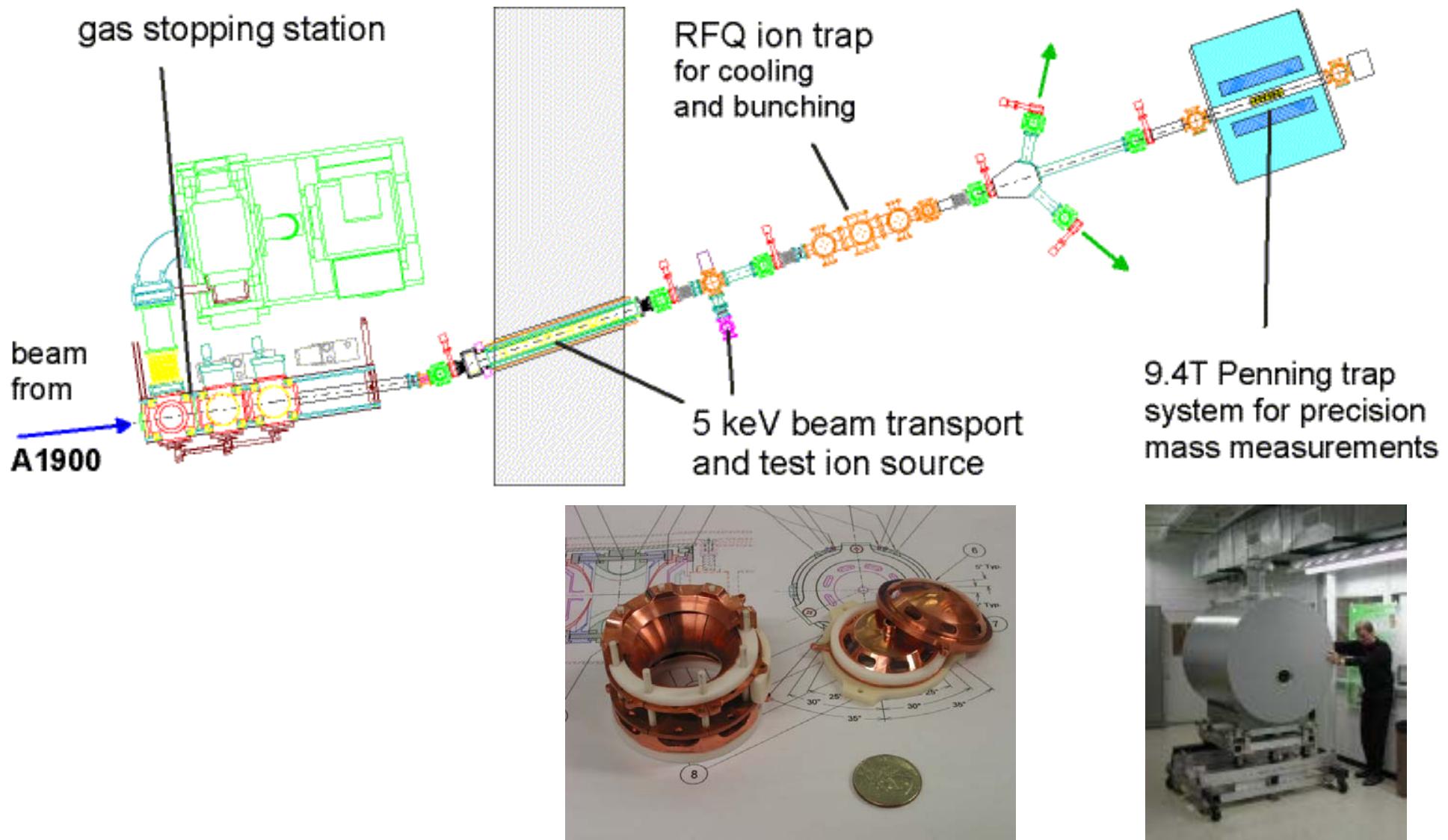
ISOL facility for transuranium nuclides

for
Nuclear Physics
Chemistry
Atomic Physics
Mass Measurements



$^{92}\text{Mo} ({}^{58}\text{Ni}, \text{xpyn}) {}^{147}\text{Ho}$
→ new masses for ${}^{147}\text{Ho}$, ${}^{147,148}\text{Er}$ ($\sim 10^{-6}$)
(M. Bloch *et al.*, ENAM04) → Ana Martin!

Low Energy Beam & Ion Trap (LEBIT) facility at NSCL/MSU



G. Bollen EMIS/ENAM proceedings

Let's pause and catch our breath...

How do all these (different?) programs compare?

Are they really different?

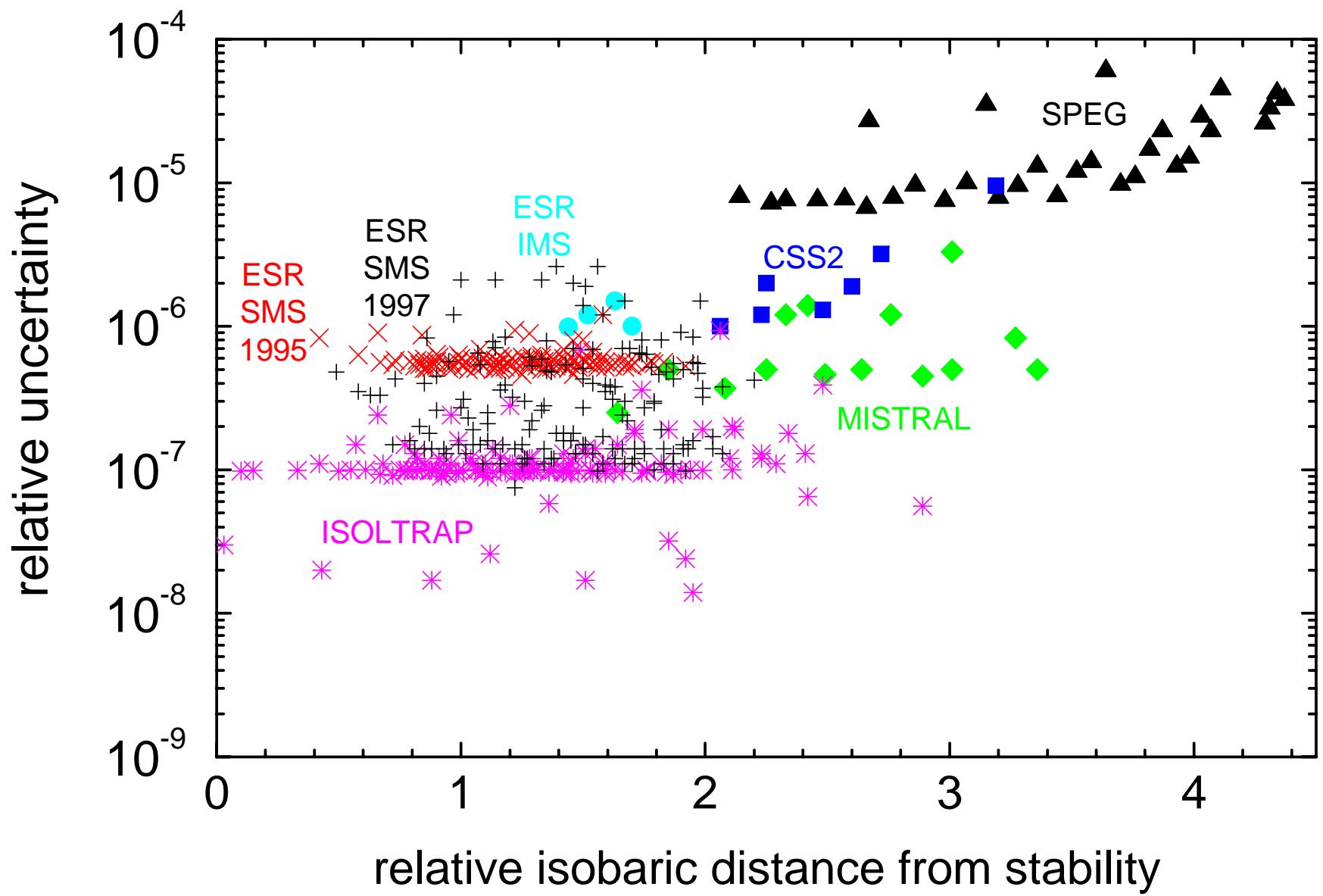
Are they complementary?

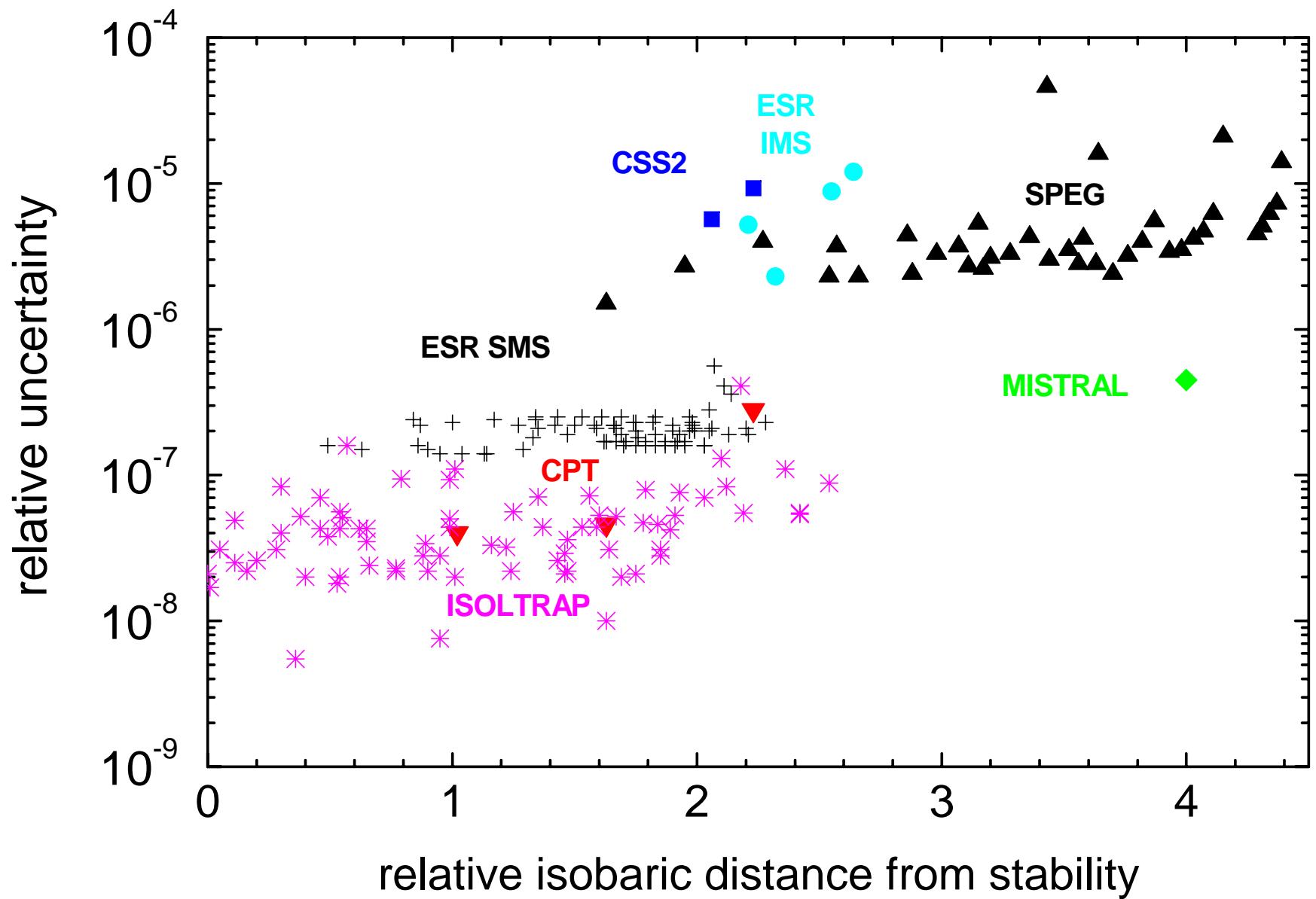
(no one facility has enough beam time...

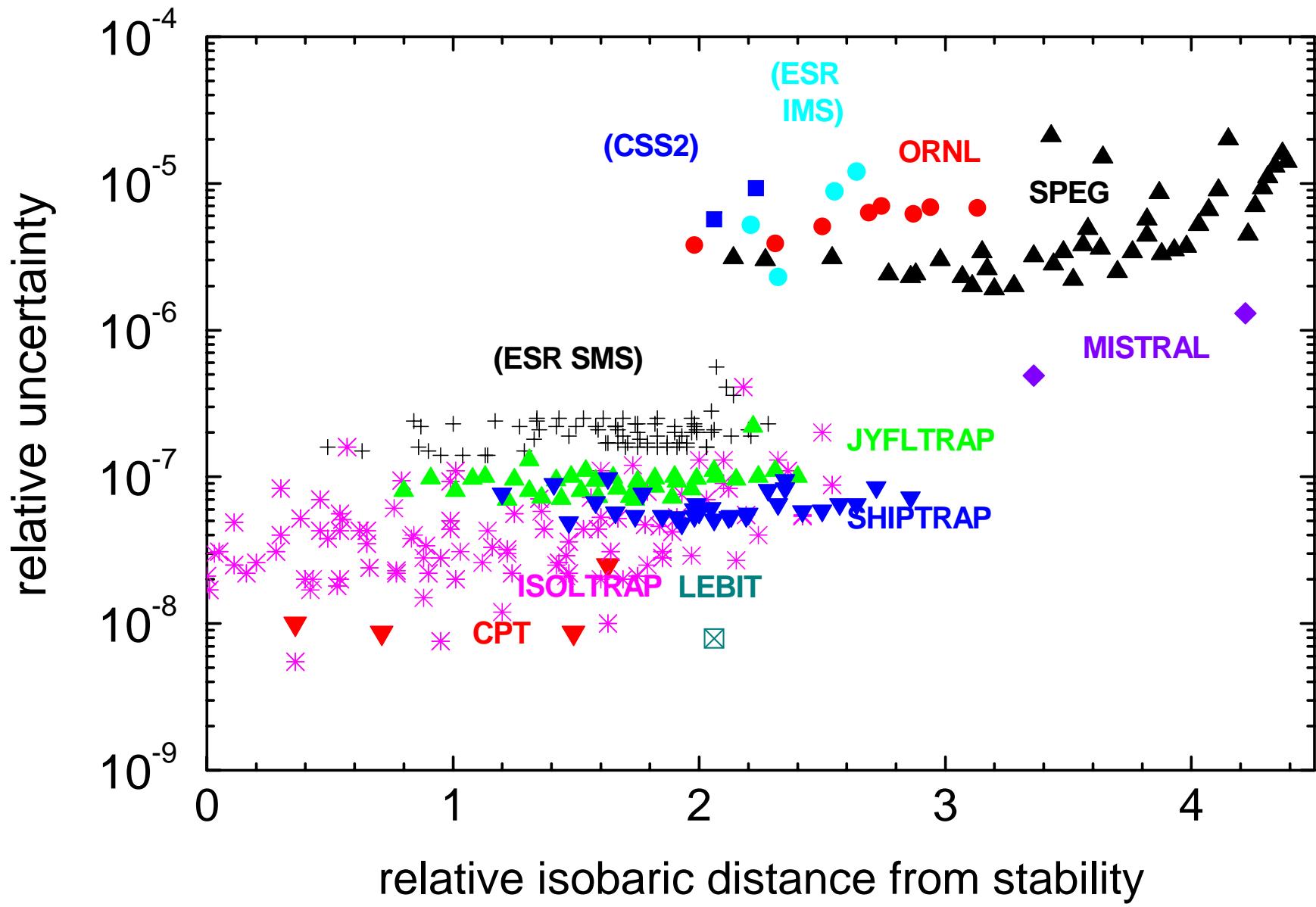
...or students to analyze the data!)

comparison of current (direct) mass measurement programs

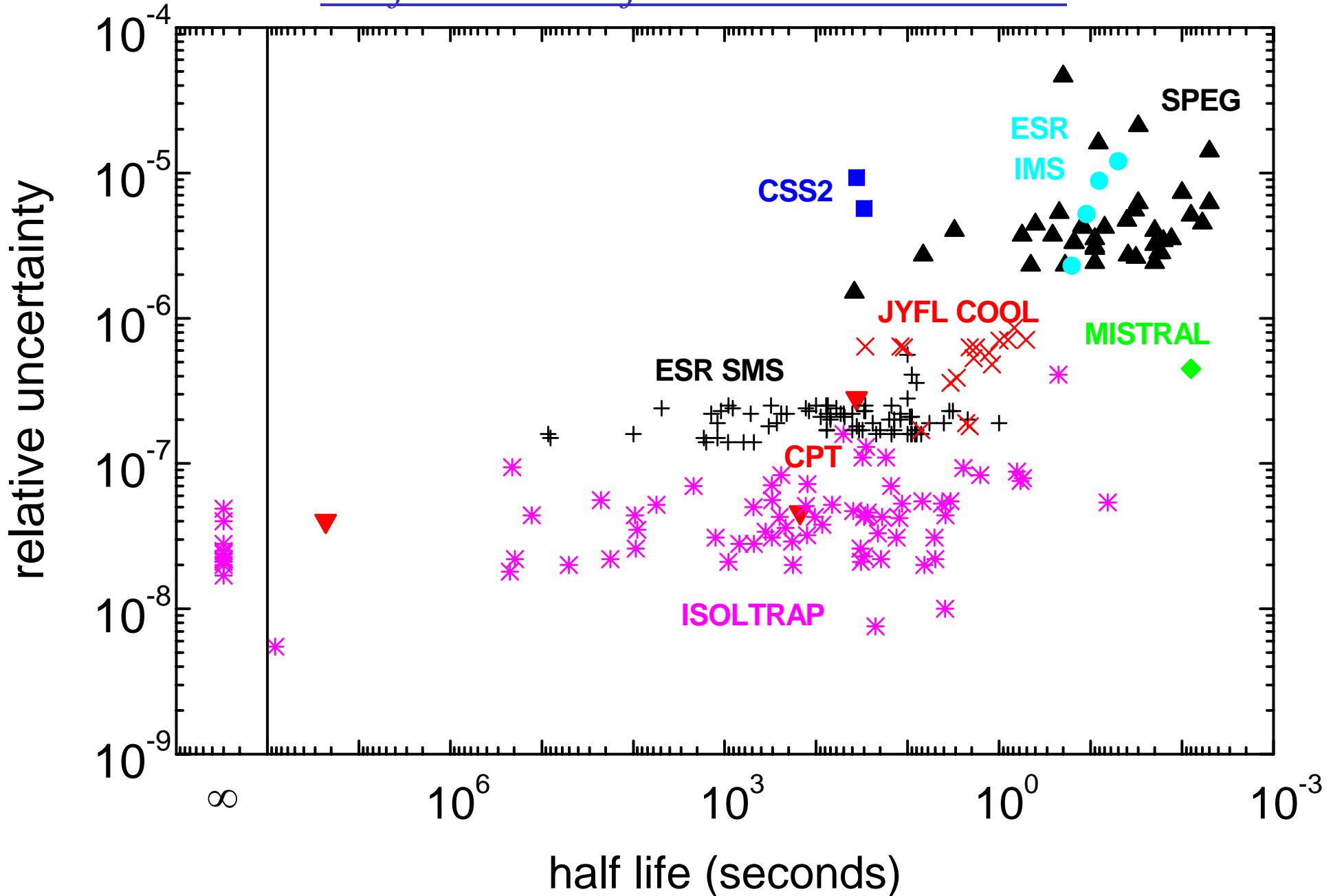
	SPEG	ESR	MISTRAL	ISOLTRAP
<i>resolution</i>	10^4	10^6	10^5	10^7
<i>precision</i>	$10^{-5} - 10^{-6}$	$1-5 \times 10^{-7}$	$3-6 \times 10^{-7}$	$1-5 \times 10^{-8}$
<i>sensitivity</i>	$10^{-1}/s$	1	$10^3/s$	$10^2/s$
<i>half-life</i>	$1 \mu s$	$10 s$	$1 ms$	$50 ms$
<i>applicability</i>	$A < 70$	<i>universal</i>	<i>universal</i> <i>(ISOLDE)</i>	<i>universal</i> <i>(ISOLDE)</i>
<i>forte</i>	<i>exotic species</i>	<i>life-times</i>	<i>short $T_{1/2}$</i> <i>& accuracy</i>	<i>highest</i> <i>accuracy</i>
<i>Achilles heel</i>	<i>μs-isomers</i>	<i>calibration</i>	<i>sys. error</i>	<i>meas. time</i>
<i>future</i>	<i>better timing</i> <i>CIME</i>	<i>isochronous</i> <i>mode $\rightarrow \mu s$</i>	<i>cooler</i>	<i>ICR</i> <i>detection</i>



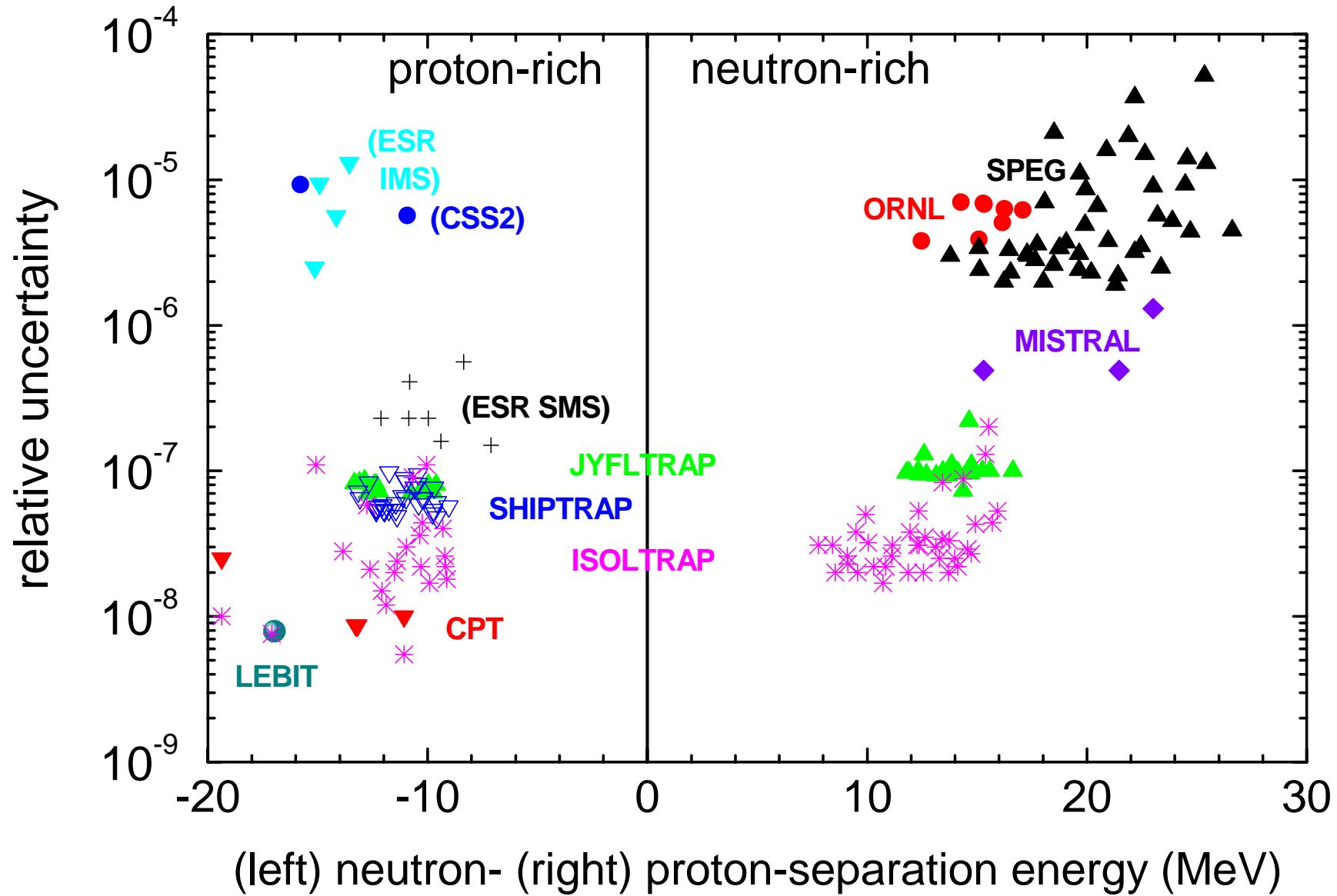


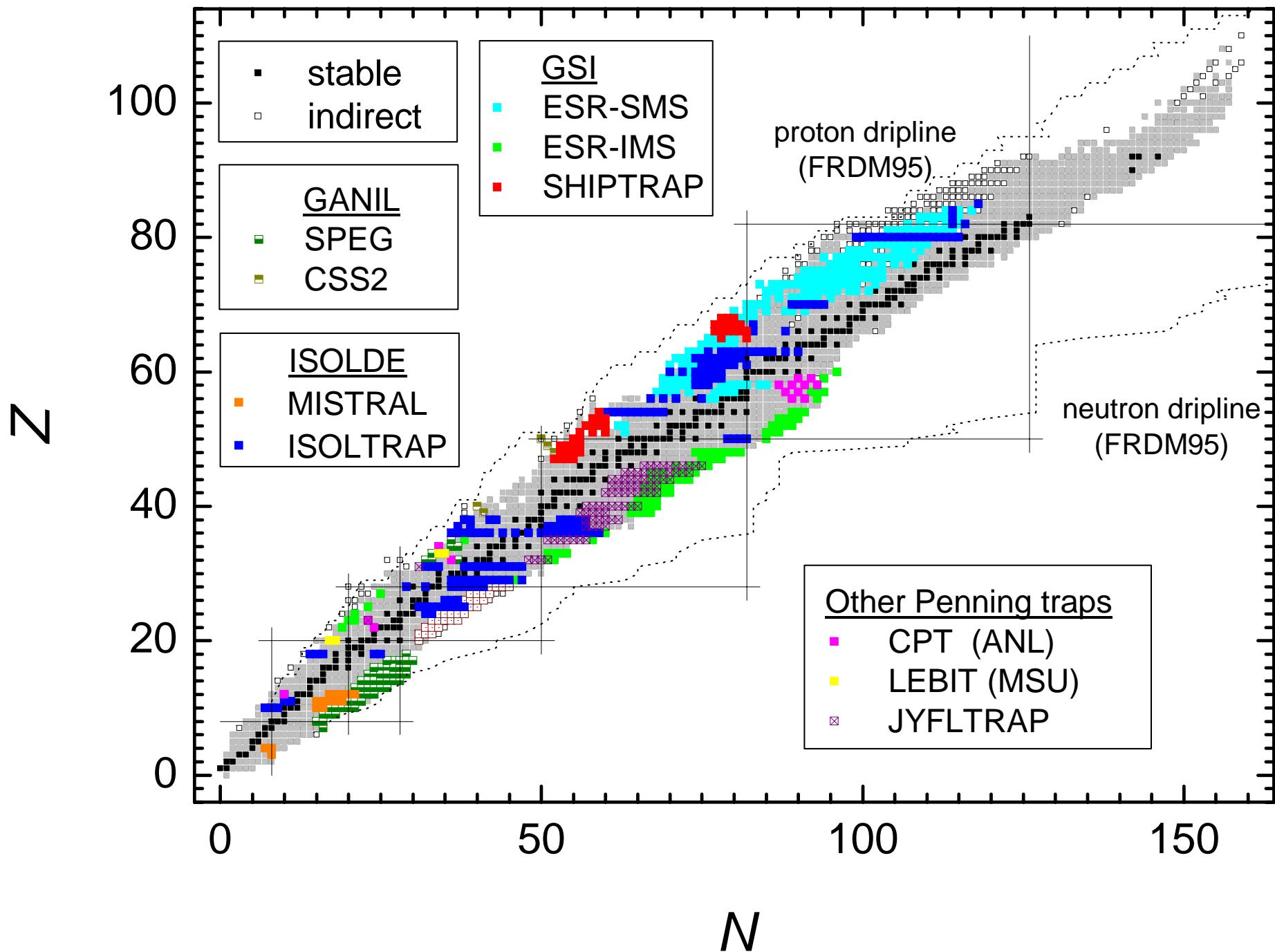


Performance of the various methods



See: Lunney, Pearson & Thibault, Rev. Mod. Phys. 75 (2003) 1021





I. General concepts – binding energy; the mass unit; resolution; precision; accuracy

II. Physics motivation

- a nuclear structure – shells, deformation, pairing, halos (the mass scale)
- b weak interaction – superallowed beta decay and the CKM matrix
- c astrophysics – stellar nucleosynthesis

III. Production of radionuclides – methods of FIFS (fragmentation) et ISOL;
(ion manipulation using traps and gas cells)

IV. Mass measurement techniques

- i. indirect methods – reactions et decays
- ii. direct methods – time of flight (SPEG et CSS2 au GANIL;
ESR isochronous mode at GSI); revolution (cyclotron) frequency
(ESR Schottky mode; ISOLTRAP and MISTRAL at ISOLDE)

V. Comparisons of the different methods

VI. The atomic mass evaluation (demonstration of the program *NUCLEUS*)

VII. Mass models and comparisons; chaos on the mass surface?

VIII. A look into the future

IX. Conclusions